

Brian 2, an intuitive and efficient neural simulator

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Abstract Brian 2 allows scientists to simply and efficiently simulate spiking neural network models. These models can feature novel dynamical equations, their interactions with the environment, and experimental protocols. To preserve high performance when defining new models, most simulators offer two options: low-level programming or description languages. The first option requires expertise, is prone to errors, and is problematic for reproducibility. The second option cannot describe all aspects of a computational experiment, such as the potentially complex logic of a stimulation protocol. Brian addresses these issues using runtime code generation. Scientists write code with simple and concise high-level descriptions, and Brian transforms them into efficient low-level code that can run interleaved with their code. We illustrate this with several challenging examples: a plastic model of the pyloric network, a closed-loop sensorimotor model, a programmatic exploration of a neuron model, and an auditory model with real-time input.

Introduction

Neural simulators are increasingly used to develop models of the nervous system, at different scales and in a variety of contexts (*Brette et al., 2007*). These simulators generally have to find a trade-off between performance and the flexibility to easily define new models and computational experiments. Brian 2 is a complete rewrite of the Brian simulator designed to solve this apparent dichotomy using the technique of code generation. The design is based around two fundamental ideas. Firstly, it is equation based: defining new neural models should be no more difficult than writing down their equations. Secondly, the computational experiment is fundamental: the interactions between neurons, environment and experimental protocols are as important as the neural model itself. We cover these points in more detail in the following paragraphs.

Popular tools for simulating spiking neurons and networks of such neurons are NEURON (*Carnevale and Hines, 2006*), GENESIS (*Bower and Beeman, 1998*), NEST (*Gewaltig and Diesmann, 2007*), and Brian (*Goodman and Brette, 2008, 2009, 2013*). Most of these simulators come with a library of standard models that the user can choose from. However, we argue that to be maximally useful for research, a simulator should also be designed to facilitate work that goes beyond what is known at the time that the tool is created, and therefore enable the user to investigate new mechanisms. Simulators take widely different approaches to this issue. For some simulators, adding new mechanisms requires specifying them in a low-level programming language such as C++, and integrating them with the simulator code (e.g. NEST). Amongst these, some provide domain-specific languages, e.g. NMODL (*Hines and Carnevale, 2000*, for NEURON) or NESTML (*Plotnikov et al., 2016*, for NEST), and tools to transform these descriptions into compiled modules that can then be used in simulation scripts. Finally, the Brian simulator has been built around mathematical model descriptions that are part of the simulation script itself.

Another approach to model definitions has been established by the development of simulator-

43 independent markup languages, for example NeuroML/LEMS (*Gleeson et al., 2010; Cannon et al.,*
 44 *2014*) and NineML (*Raikov et al., 2011*). However, markup languages address only part of the
 45 problem. A computational experiment is not fully specified by a neural model: it also includes a
 46 particular experimental protocol (set of rules defining the experiment), for example a sequence of
 47 visual stimuli. Capturing the full range of potential protocols cannot be done with a purely declara-
 48 tive markup language, but is straightforward in a general purpose programming language. For this
 49 reason, the Brian simulator combines the model descriptions with a procedural, computational
 50 experiment approach: a simulation is a user script written in Python, with models described in
 51 their mathematical form, without any reference to predefined models. This script may implement
 52 arbitrary protocols by loading data, defining models, running simulations and analysing results.
 53 Due to Python’s expressiveness, there is no limit on the structure of the computational experiment:
 54 stimuli can be changed in a loop, or presented conditionally based on the results of the simulation,
 55 etc. This flexibility can only be obtained with a general-purpose programming language, and is
 56 necessary to specify the full range of computational experiments that scientists are interested in.

57 While the procedural, equation-oriented approach addresses the issue of flexibility for both
 58 the modelling and the computational experiment, it comes at the cost of reduced performance,
 59 especially for small-scale models that do not benefit much from vectorization techniques (*Brette*
 60 *and Goodman, 2011*). The reduced performance results from the use of an interpreted language to
 61 implement arbitrary models, instead of the use of pre-compiled code for a set of previously defined
 62 models. Thus, simulators generally have to find a trade-off between flexibility and performance, and
 63 previous approaches have often chosen one over the other. In practice, this makes computational
 64 experiments that are based on non-standard models either difficult to implement or slow to
 65 perform. We will describe four case studies in this article: exploring unconventional plasticity rules
 66 for a small neural circuit (case study 1, *Figure 1, Figure 2*); running a model of a sensorimotor loop
 67 (case study 2, *Figure 3*); determining the spiking threshold of a complex model by bisection (case
 68 study 3, *Figure 4, Figure 5*); and running an auditory model with real-time input from a microphone
 69 (case study 4, *Figure 6, Figure 7*).

70 Brian 2 solves the performance-flexibility trade-off using the technique of code generation
 71 (*Goodman, 2010; Stimberg et al., 2014; Blundell et al., 2018*). The term code generation here refers
 72 to the process of automatically transforming a high-level user-defined model into executable code
 73 in a computationally efficient low-level language, compiling it in the background and running it
 74 without requiring any actions from the user. This generated code is inserted within the flow of
 75 the simulation script, which makes it compatible with the procedural approach. Code generation
 76 is not only used to run the models but also to build them, and therefore also accelerates stages
 77 such as synapse creation. The code generation framework has been designed to be extensible on
 78 several levels. On a general level, code generation targets can be added to generate code for other
 79 architectures, e.g. graphical processing units, from the same simulation description. On a more
 80 specific level, new functionality can be added by providing a small amount of code written in the
 81 target language, e.g. to connect the simulation to an input device. Implementing this solution in a
 82 way that is transparent to the user requires solving important design and computational problems,
 83 which we will describe in the following.

84 **Methods**

85 **Design and Implementation**

86 We will explain the key design decisions by starting from the requirements that motivated them.
 87 Note that from now on we will use the term “Brian” as referring to its latest version, i.e. Brian 2, and
 88 only use “Brian 1” and “Brian 2” when discussing differences between them.

89 Before discussing the requirements, we start by motivating the choice of programming language.
 90 Python is a high-level language, that is, it is abstracted from machine level details and highly
 91 readable (indeed, it is often described as “executable pseudocode”). In this sense, it is higher

92 level than C++, for example, which in this article we will refer to as a low-level language (since
 93 we will not need to refer to even lower level languages such as assembly language). The use of
 94 a high-level language is important for scientific software because the majority of scientists are
 95 not trained programmers, and high-level languages are generally easier to learn and use, and
 96 lead to shorter code that is easier to debug. This last point, and the fact that Python is a very
 97 popular general purpose programming language with excellent built-in and third party tools, is
 98 also important for reducing development time, enabling the developers to be more efficient. It is
 99 now widely recognised that Python is well suited to scientific software, and it is commonly used
 100 in computational neuroscience (*Davison et al., 2009; Muller et al., 2015*). Note that expert level
 101 Python knowledge is not necessary for using Brian or the Python interfaces for other simulators.

102 We now move on to the major design requirements.

- 103 1. Users should be able to easily define non-standard models, which may include models of
 104 neurons and synapses but also of other aspects such as muscles and environment. This is
 105 made possible by an equation-oriented approach, i.e., models are described by mathematical
 106 equations. We first focus on the design at the *mathematical level*, and we illustrate with two
 107 unconventional models: a model of intrinsic plasticity in the pyloric network of the crustacean
 108 stomatogastric ganglion (case study 1, *Figure 1, Figure 2*), and a closed-loop sensorimotor
 109 model of ocular movements (case study 2, *Figure 3*).
- 110 2. Users should be able to easily implement a complete computational experiment in Brian.
 111 Models must interact with a general control flow, which may include stimulus generation
 112 and various operations. This is made possible by taking a procedural approach to defining a
 113 complete computational experiment, rather than a declarative model definition, allowing users
 114 to make full use of the generality of the Python language. In the section on the *computational*
 115 *experiment level*, we demonstrate the interaction between a general control flow expressed in
 116 Python and the simulation run in a case study that uses a bisection algorithm to determine
 117 a neuron's firing threshold as a function of sodium channel density (case study 3, *Figure 4,*
 118 *Figure 5*).
- 119 3. Computational efficiency. Often, computational neuroscience research is limited more by the
 120 scientist's time spent designing and implementing models, and analysing results, rather than
 121 the simulation time. However, there are occasions where high computational efficiency is
 122 necessary. To achieve high performance while preserving maximum flexibility, Brian generates
 123 code from user-defined equations and integrates it into the simulation flow.
- 124 4. Extensibility: no simulator can implement everything that any user might conceivably want,
 125 but users shouldn't have to discard the simulator entirely if they want to go beyond its built-in
 126 capabilities. We therefore provide the possibility for users to extend the code either at a
 127 high or low level. We illustrate these last two requirements at the *implementation level* with a
 128 case study of a model of pitch perception using real-time audio input (case study 4, *Figure 6,*
 129 *Figure 7*).

130 In this section, we give a high level overview of the major decisions. A detailed analysis of the
 131 case studies and the features of Brian they use can be found in Appendix 1. Source code for the
 132 case studies has been deposited in a repository at [https://github.com/brian-team/brian2_paper_](https://github.com/brian-team/brian2_paper_examples)
 133 [examples](https://github.com/brian-team/brian2_paper_examples) (*Stimberg et al., 2019a*).

134 Mathematical level

135 Case study 1: Pyloric network

136 We start with a case study of a model of the pyloric network of the crustacean stomatogastric
 137 ganglion (*Figure 1a*), adapted and simplified from earlier studies (*Golowasch et al., 1999; Prinz et al.,*
 138 *2004; Prinz, 2006; O'Leary et al., 2014*). This network has a small number of well characterized
 139 neuron types – anterior burster (AB), pyloric dilator (PD), lateral pyloric (LP), and pyloric (PY) neurons
 140 – and is known to generate a stereotypical triphasic motor pattern (*Figure 1b–c*). Following previous

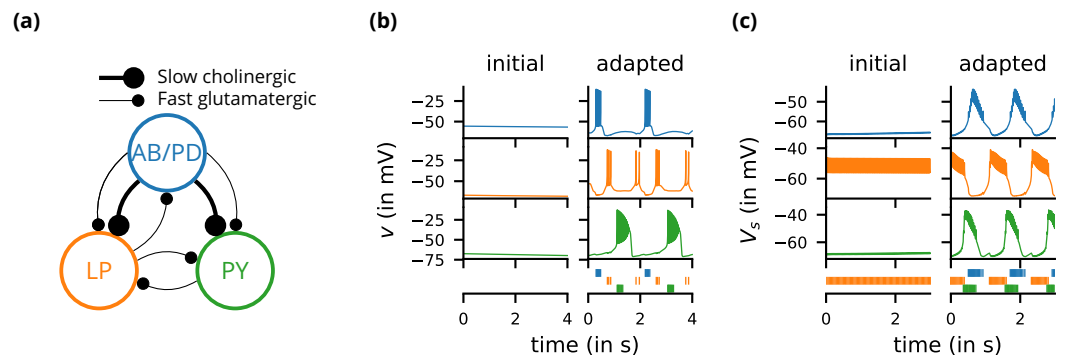


Figure 1. Case study 1: A model of the pyloric network of the crustacean stomatogastric ganglion, inspired by several modeling papers on this subject (Golowasch *et al.*, 1999; Prinz *et al.*, 2004; Prinz, 2006; O’Leary *et al.*, 2014) (a) Schematic of the modeled circuit (after Prinz *et al.*, 2004). The pacemaker kernel is modeled by a single neuron representing both anterior burster and pyloric dilator neurons (AB/PD, blue). There are two types of follower neurons, lateral pyloric (LP, orange), and pyloric (PY, green). Neurons are connected via slow cholinergic (thick lines) and fast glutamatergic (thin lines) synapses. (b) Activity of the simulated neurons. Membrane potential is plotted over time for the neurons in (a), using the same colour code. The bottom row shows their spiking activity in a raster plot, with spikes defined as excursions of the membrane potential over -20 mV. In the left column (“initial”), activity is shown for 4 s after an initial settling time of 2.5 s. The right column (“adapted”) shows the activity with fully adapted conductances (see text for details) after an additional time of 49 s. (c) Activity of the simulated neurons of a biologically detailed version of the circuit shown in (a), following Golowasch *et al.* (1999). All conventions as in (b), except for showing 3 s of activity after a settling time of 0.5 s (“initial”), and after an additional time of 24 s (“adapted”). Also note that the biologically detailed model consists of two coupled compartments, but only the membrane potential of the somatic compartment (V_s) is shown here.

141 studies, we lump AB and PD neurons into a single neuron type (AB/PD) and consider a circuit with
 142 one neuron of each type. The neurons in this circuit have rebound and bursting properties. We
 143 model this using a variant of the model proposed by Hindmarsh and Rose (1984), a three-variable
 144 model exhibiting such properties. We make this choice only for simplicity: the biophysical equations
 145 originally used in Golowasch *et al.* (1999) can be used instead (see Figure 2–Figure Supplement 1).

146 Although this model is based on widely used neuron models, it has the unusual feature that
 147 some of the conductances are regulated by activity as monitored by a calcium trace. One of the
 148 first design requirements of Brian, then, is that non-standard aspects of models such as this should
 149 be as easy to implement in code as they are to describe in terms of their mathematical equations.
 150 We briefly summarise how it applies to this model (see appendix 1 and Stimberg *et al.* (2014) for
 151 more detail). The three-variable underlying neuron model is implemented by writing its differential
 152 equations directly in standard mathematical form (Figure 2, l. 8–10). The calcium trace increases at
 153 each spike (l. 21; defined by a discrete event triggered after a spike, `reset='Ca += 0.1'`) and then
 154 decays (l. 13; again defined by a differential equation). A slow variable z tracks the difference of this
 155 calcium trace to a neuron-type-specific target value (l. 14) which then regulates the conductances s
 156 and g (l. 11–12).

157 Not only the neuron model but also their connections are non-standard. Neurons are connected
 158 together by nonlinear graded synapses of two different types, slow and fast (l. 29–54). These are
 159 unconventional synapses in that the synaptic current has a graded dependence on the pre-synaptic
 160 action potential and a continuous effect rather than only being triggered by pre-synaptic action
 161 potentials (Abbott and Marder, 1998). A key design requirement of Brian was to allow for the same
 162 expressivity for synaptic models as for neuron models, which led us to a number of features that
 163 allow for a particularly flexible specification of synapses in Brian. Firstly, we allow synapses to have
 164 dynamics defined by differential equations in precisely the same way as neurons. In addition to
 165 the usual role of triggering instantaneous changes in response to discrete neuronal events such as
 166 spikes, synapses can directly and continuously modify neuronal variables allowing for a very wide

```

1  from brian2 import *
2  defaultclock.dt = 0.01*ms;
3  Delta_T = 17.5*mV      ; v_T = -40*mV      ; tau = 2*ms      ; tau_adapt = .02*second
4  tau_Ca = 150*ms      ; tau_x = 2*second  ; v_r = -68*mV   ; tau_z = 5*second
5  a = 1/Delta_T**3    ; b = 3/Delta_T**2  ; c = 1.2*nA     ; d = 2.5*nA/Delta_T**2
6  C = 60*pF          ; S = 2*nA/Delta_T  ; G = 28.5*nS
7  eqs = '''
8  dv/dt = (Delta_T*g*(-a*(v - v_T)**3 + b*(v - v_T)**2) + w - x - I_fast - I_slow)/C : volt
9  dw/dt = (c - d*(v - v_T)**2 - w)/tau : amp
10 dx/dt = (s*(v - v_r) - x)/tau_x : amp
11 s = S*(1 - tanh(z)) : siemens
12 g = G*(1 + tanh(z)) : siemens
13 dCa/dt = -Ca/tau_Ca : 1
14 dz/dt = tanh(Ca - Ca_target)/tau_z : 1
15 I_fast : amp
16 I_slow : amp
17 Ca_target : 1 (constant)
18 label : integer (constant)
19 '''
20 ABPD, LP, PY = 0, 1, 2
21 circuit = NeuronGroup(3, eqs, threshold='v > -20*mV', refractory='v > -20*mV',
22                      reset='Ca += 0.1', method='rk2')
23 circuit.label = [ABPD, LP, PY]
24 circuit.v = v_r
25 circuit.w = '-5*nA*rand()'
26 circuit.z = 'rand()*0.2 - 0.1'
27 circuit.Ca_target = [0.048, 0.0384, 0.06]
28
29 s_fast = 0.2/mV; V_fast = -50*mV; E_syn = -75*mV
30 eqs_fast = '''
31 g_fast : siemens (constant)
32 I_fast_post = g_fast*(v_post - E_syn)/(1+exp(s_fast*(V_fast-v_pre))) : amp (summed)
33 '''
34 fast_synapses = Synapses(circuit, circuit, model=eqs_fast)
35 fast_synapses.connect('label_pre != label_post and not (label_pre == PY and label_post == ABPD)')
36 fast_synapses.g_fast['label_pre == ABPD and label_post == LP'] = 0.015*uS
37 fast_synapses.g_fast['label_pre == ABPD and label_post == PY'] = 0.005*uS
38 fast_synapses.g_fast['label_pre == LP and label_post == ABPD'] = 0.01*uS
39 fast_synapses.g_fast['label_pre == LP and label_post == PY'] = 0.02*uS
40 fast_synapses.g_fast['label_pre == PY and label_post == LP'] = 0.005*uS
41
42 s_slow = 1/mV; V_slow = -55*mV; k_1 = 1/ms
43 eqs_slow = '''
44 k_2 : 1/second (constant)
45 g_slow : siemens (constant)
46 I_slow_post = g_slow*m_slow*(v_post-E_syn) : amp (summed)
47 dm_slow/dt = k_1*(1-m_slow)/(1+exp(s_slow*(V_slow-v_pre))) - k_2*m_slow : 1 (clock-driven)
48 '''
49 slow_synapses = Synapses(circuit, circuit, model=eqs_slow, method='exact')
50 slow_synapses.connect('label_pre == ABPD and label_post != ABPD')
51 slow_synapses.g_slow['label_post == LP'] = 0.025*uS
52 slow_synapses.k_2['label_post == LP'] = 0.03/ms
53 slow_synapses.g_slow['label_post == PY'] = 0.015*uS
54 slow_synapses.k_2['label_post == PY'] = 0.008/ms
55
56 run(59.5*second)

```

Figure 2. Case study 1: A model of the pyloric network of the crustacean stomatogastric ganglion. Simulation code for the model shown in *Figure 1a*, producing the circuit activity shown in *Figure 1b*.

Figure 2-Figure supplement 1. Simulation code for the more biologically detailed model of the circuit shown in *Figure 1a*, producing the circuit activity shown in *Figure 1c*

167 range of synapse types. To illustrate this, for the slow synapse, we have a synaptic variable (`m_slow`)
 168 that evolves according to a differential equation (l. 47) that depends on the pre-synaptic membrane
 169 potential (`v_pre`). The effect of this synapse is defined by setting the value of a post-synaptic neuron
 170 current (`I_slow`) in the definition of the synapse model (l. 46; referred to there as `I_slow_post`). The
 171 keyword (`summed`) in the equation specifies that the post-synaptic neuron variable is set using the
 172 summed value of the expression across all the synapses connected to it. Note that this mechanism
 173 also allows Brian to be used to specify abstract rate-based neuron models in addition to biophysical
 174 graded synapse models.

175 The model is defined not only by its dynamics, but also the values of parameters and the connec-
 176 tivity pattern of synapses. The next design requirement of Brian was that these essential elements
 177 of specifying a model should be equally flexible and readable as the dynamics. In this case, we have
 178 added a label variable to the model that can take values ABPD, LP or PY (l. 18, 20, 23) and used this la-
 179 bel to set up the initial values (l. 36–40, 51–54) and connectivity patterns (l. 35, 50). Human readability
 180 of scripts is a key aspect of Brian code, and important for reproducibility (which we will come back to
 181 in the Discussion). We highlight line 35 to illustrate this. We wish to have synapses between all neu-
 182 rons of different types but not of the same type, except that we do not wish to have synapses from
 183 PY neurons to AB/PD neurons. Having set up the labels, we can now express this connectivity pattern
 184 with the expression `'label_pre!=label_post and not (label_pre==PY and label_post==ABPD)'`.
 185 This example illustrates one of the many possibilities offered by the equation-oriented approach to
 186 concisely express connectivity patterns (for more details see Appendix 1 and *Stimberg et al. (2014)*).

187 **Comparison to other approaches** In this case study, we have shown how a non-standard
 188 neural network, with graded synapses and adapting conductances, can be described in the Brian
 189 simulator. How could such a model be implemented with one of the other approaches described
 190 previously? We will briefly discuss this by focussing on implementations of the graded synapse
 191 model. One approach is to directly write an implementation of the model in a programming
 192 language like C++, without the use of any simulation software. While this requires significant
 193 technical skill, it allows for complete freedom in the definition of the model itself. This was
 194 the approach taken for a study that ran 20 million parametrized instances of the same pyloric
 195 network model (*Günay and Prinz, 2010*). The increased effort of writing the simulation was offset
 196 by reusing the same model an extremely large number of times. An excerpt of this code is shown in
 197 Appendix 3 *Figure 1c*. Note that unless great care is taken, this approach may lead to a very specific
 198 implementation of the model that is not straightforward to adapt for other purposes. With such
 199 long source code (3,510 lines in this case) it is also difficult to check that there are no errors in the
 200 code, or implicit assumptions that deviate from the description (as in, for example *Hathway and*
 201 *Goodman, 2018; Pauli et al., 2018*).

202 Another approach for describing model components such as graded synapses is to use a
 203 description language such as LEMS/NeuroML2. If the specific model has already been added
 204 as a “core type”, then it can be readily referenced in the description of the model (Appendix 3
 205 *Figure 2d*). If not, then the LEMS description can be used to describe it (Appendix 3 *Figure 2d*).
 206 Such a description is on a similar level of abstraction as the Brian description, but somewhat more
 207 verbose (although this may be reduced by using a library such as PyLEMS to create the description;
 208 *Vella et al., 2014*).

209 If the user chooses to use the NEURON simulator to simulate the model, then a new synaptic
 210 mechanism can be added using the NMODL language (Appendix 3 *Figure 2e*). However, for the
 211 user this requires learning a new, idiosyncratic language, and detailed knowledge about simulator
 212 internals, e.g. the numerical solution of equations. Other simulators, such as NEST, are focussed
 213 on discrete spike-based interactions and currently do not come with models of graded synapses,
 214 and such models are not yet supported by its description language NESTML. Leveraging the
 215 infrastructure added for gap-junctions (*Hahne et al., 2015*) and rate models (*Hahne et al., 2017*),
 216 the NEST simulator could certainly integrate such models in principle but in practice this may not

217 be feasible without direct support from the NEST team.

218 Case study 2: Ocular model

219 The second example is a closed-loop sensorimotor model of ocular movements (used for illustration
220 and not intended to be a realistic description of the system), where the eye tracks an object
221 (*Figure 3a, b*). Thus, in addition to neurons, the model also describes the activity of ocular muscles
222 and the dynamics of the stimulus. Each of the two antagonistic muscles is modelled mechanically
223 as an elastic spring with some friction, which moves the eye laterally.

224 The next design requirement of Brian was that it should be both possible and straightforward to
225 define non-neuronal elements of a model, as these are just as essential to the model as a whole,
226 and the importance of connecting with these elements is often neglected in neural simulators. We
227 will come back to this requirement in various forms over the next few case studies, but here we
228 emphasise how the mechanisms for specifying arbitrary differential equations can be re-used for
229 non-neuronal elements of a simulation.

230 The position of the eye follows a second order differential equation, with resting position x_0 , the
231 difference in resting positions of the two muscles (*Figure 3c*, l. 4–5). The stimulus is an object that
232 moves in front of the eye according to a stochastic process (l. 7–8). Muscles are controlled by two
233 motoneurons (l. 11–13), for which each spike triggers a muscular “twitch”. This corresponds to a
234 transient change in the resting position x_0 of the eye in either direction, which then decays back to
235 zero (l. 6, 15).

236 Retinal neurons receive a visual input, modelled as a Gaussian function of the difference
237 between the neuron’s preferred position and the actual position of the object, measured in retinal
238 coordinates (l. 21). Thus, the input to the neurons depends on dynamical variables external to
239 the neuron model. This is a further illustration of the design requirement above that we need to
240 include non-neuronal elements in our model specifications. In this case, to achieve this we link the
241 variables in the eye model with the variables in the retina model using the `linked_var` function (l. 4,
242 7, 23–24, 28–29).

243 Finally, we implement a simple feedback mechanism by having retinal neurons project onto
244 the motoneuron controlling the contralateral muscle (l. 33), with a strength proportional to their
245 eccentricity (l. 35): thus, if the object appears on the edge of the retina, the eye is strongly pulled
246 towards the object; if the object appears in the center, muscles are not activated. This simple
247 mechanism allows the eye to follow the object (*Figure 3b*), and the code illustrates the previous
248 design requirement that the code should reflect the mathematical description of the model.

249 **Comparison to other approaches** The remarks we made earlier regarding the graded synapse
250 in case study 1 mostly apply here as well. For LEMS/NeuroML2, both motor neurons and the envi-
251 ronment could be modelled with a LEMS description. Similarly, a simulation with NEURON would
252 require NMODL specifications of both models, using its `POINTER` mechanism (see Appendix 3 *Fig-
253 ure 2*) to link them together. Since NEST’s modelling language NESTML does not allow for the
254 necessary continuous interaction between a single environment and multiple neurons, implement-
255 ing this model would be a major effort and require writing code in C++ and detailed knowledge of
256 NEST’s internal architecture.

257 Computational experiment level

258 The mathematical model descriptions discussed in the previous section provide only a partial
259 description of what we might call a “computational experiment”. Let us consider the analogy to an
260 electrophysiological experiment: for a full description, we would not only state the model animal,
261 the cell type and the preparation that was investigated, but also the stimulation and analysis
262 protocol. In the same way, a full description of a computational experiment requires not only a
263 description of the neuron and synapse models, but also information such as how input stimuli are
264 generated, or what sequence of simulations is run. Some examples of computational experimental

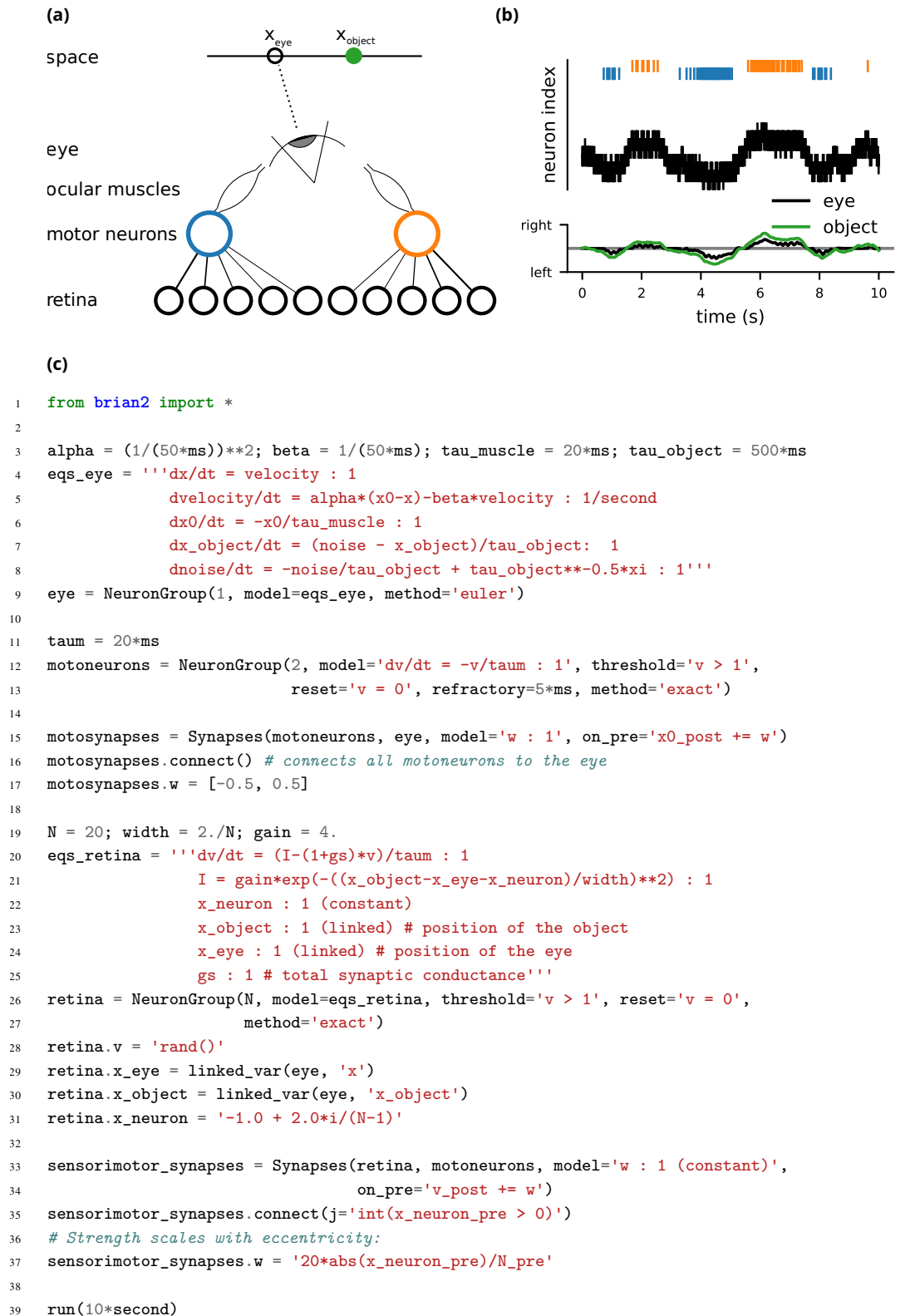


Figure 3. Case Study 2: Smooth pursuit eye movements. **(a)** Schematics of the model. An object (green) moves along a line and activates retinal neurons (bottom row; black) that are sensitive to the relative position of the object to the eye. Retinal neurons activate two motor neurons with weights depending on the eccentricity of their preferred position in space. Motor neurons activate the ocular muscles responsible for turning the eye. **(b)** Top: Simulated activity of the sensory neurons (black), and the left (blue) and right (orange) motor neurons. Bottom: Position of the eye (black) and the stimulus (green). **(c)** Simulation code.

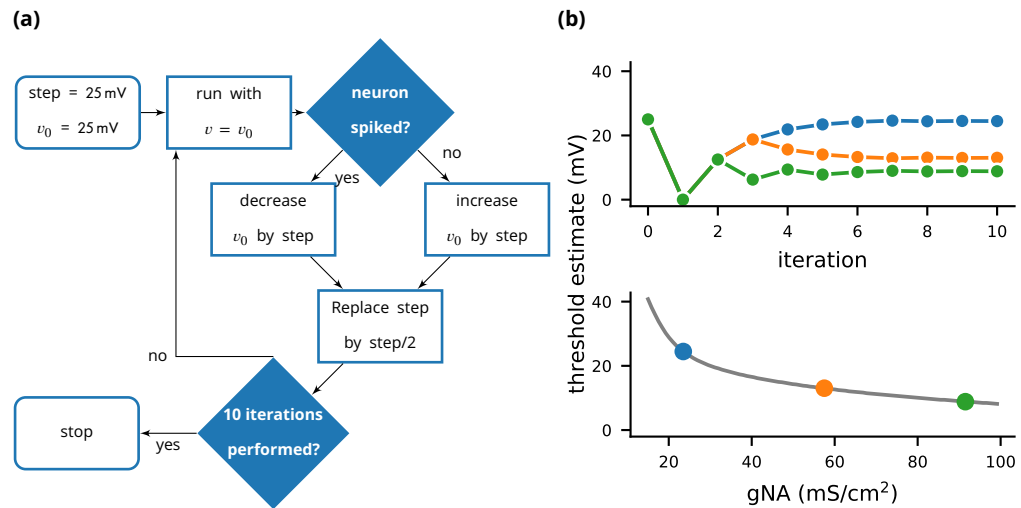


Figure 4. Case study 3: Using bisection to find a neuron’s voltage threshold. **(a)** Schematic of the bisection algorithm for finding a neuron’s voltage threshold. The algorithm is applied in parallel for different values of sodium density. **(b)** Top: Refinement of the voltage threshold estimate over iterations for three sodium densities (blue: 23.5 mS cm⁻², orange: 57.5 mS cm⁻², green: 91.5 mS cm⁻²); Bottom: Voltage threshold estimation as a function of sodium density.

265 protocols would include: threshold finding (discussed in detail below) where the stimulus on the
 266 next trial depends on the outcome of the current trial; generalisations of this to potentially very
 267 complex closed-loop experiments designed to determine the optimal stimuli for a neuron (e.g. *Edin*
 268 *et al., 2004*); models including a complex simulated environment defined in an external package
 269 (e.g. *Voegtlin, 2011*); or models with plasticity based on an error signal that depends on the global
 270 behaviour of the network (e.g. *Stroud et al., 2018; Zenke and Ganguli, 2018*). Capturing all these
 271 potential protocols in a purely descriptive format (one that is not Turing complete) is impossible by
 272 definition, but it can be easily expressed in a programming language with control structures such
 273 as loops and conditionals. The Brian simulator allows the user to write complete computational
 274 experimental protocols that include both the model description and the simulation protocol in a
 275 single, readable Python script.

276 Case study 3: Threshold finding

277 In this case study, we want to determine the voltage firing threshold of a neuron (**Figure 4**), modelled
 278 with three conductances, a passive leak conductance and voltage-dependent sodium and potassium
 279 conductances (**Figure 5** l. 4–24).

280 To get an accurate estimate of the threshold, we use a bisection algorithm (**Figure 4a**): starting
 281 from an initial estimate and with an initial step width (**Figure 5**, l. 30–31), we set the neuron’s
 282 membrane potential to the estimate (l. 35) and simulate its dynamics for 20 ms (l. 36). If the neuron
 283 spikes, i.e. if the estimate was above the neuron’s threshold, we decrease our estimate (l. 38); if the
 284 neuron does not spike, we increase it (l. 37). We then halve the step width (l. 39) and perform the
 285 same process again until we have performed a certain number of iterations (l. 33) and converged
 286 to a precise estimate (**Figure 4b** top). Note that the order of operations is important here. When
 287 we modify the variable v in lines 37–38, we use the output of the simulation run on line 36, and
 288 this determines the parameters for the next iteration. A purely declarative definition could not
 289 represent this essential feature of the computational experiment.

290 For each iteration of this loop, we restore the network state (`restore()`; l. 34) to what it was at
 291 the beginning of the simulation (`store()`; l. 27). This `store()/restore()` mechanism is a key part of
 292 Brian’s design for allowing computational experiments to be easily and flexibly expressed in Python,
 293 as it gives a very effective way of representing common computational experimental protocols.

```

1  from brian2 import *
2  defaultclock.dt = 0.01*ms
3
4  E1 = 10.613*mV; ENa = 115*mV; EK = -12*mV
5  g1 = 0.3*mS/cm**2; gK = 36*mS/cm**2; C = 1*uF/cm**2
6  gNa_min = 15*mS/cm**2; gNa_max = 100*mS/cm**2
7
8  eqs = '''dv/dt = (g1*(E1 - v) + gNa*m**3*h*(ENa - v) + gK*n**4*(EK - v)) / C : volt
9          gNa : siemens/meter**2
10         dm/dt = alphas*(1 - m) - betam*m : 1
11         dn/dt = alphan*(1 - n) - betan*n : 1
12         dh/dt = alphah*(1 - h) - betah*h : 1
13         alphas = (0.1/mV)*(-v + 25*mV)/(exp((-v + 25*mV)/(10*mV)) - 1)/ms : Hz
14         betam = 4 * exp(-v/(18*mV))/ms : Hz
15         alphah = 0.07 * exp(-v/(20*mV))/ms : Hz
16         betah = 1/(exp((-v+30*mV) / (10*mV)) + 1)/ms : Hz
17         alphan = (0.01/mV) * (-v+10*mV) / (exp((-v+10*mV) / (10*mV)) - 1)/ms : Hz
18         betan = 0.125*exp(-v/(80*mV))/ms : Hz'''
19  neurons = NeuronGroup(100, eqs, threshold='v > 50*mV',
20                       method='exponential_euler')
21  neurons.gNa = 'gNa_min + (gNa_max - gNa_min)*1.0*i/N'
22  neurons.v = 0*mV
23  neurons.m = '1/(1 + betam/alphas)'
24  neurons.n = '1/(1 + betan/alphan)'
25  neurons.h = '1/(1 + betah/alphah)'
26  S = SpikeMonitor(neurons)
27
28  store()
29
30  # We locate the threshold by bisection
31  v0 = 25*mV*ones(len(neurons))
32  step = 25*mV
33
34  for i in range(10):
35      restore()
36      neurons.v = v0
37      run(20*ms)
38      v0[S.count == 0] += step
39      v0[S.count > 0] -= step
40      step /= 2.0

```

Figure 5. Case study 3: Simulation code to find a neuron's voltage threshold, implementing the bisection algorithm detailed in [Figure 4a](#). The code simulates 100 unconnected neurons with sodium densities between 15 mS cm^{-2} and 100 mS cm^{-2} , following the model of *Hodgkin and Huxley (1952)*. Results from these simulations are shown in [Figure 4b](#).

294 Examples that can easily be implemented with this mechanism include a training/testing/validation
 295 cycle in a synaptic plasticity setting; repeating simulations with some aspect of the model changed
 296 but the rest held constant (e.g. parameter sweeps, responses to different stimuli); or simply
 297 repeatedly running an identical stochastic simulation to evaluate its statistical properties.

298 At the end of the script, by performing this estimation loop in parallel for many neurons, each
 299 having a different maximal sodium conductance, we arrive at an estimate of the dependence of the
 300 voltage threshold on the sodium conductance (*Figure 4b* bottom).

301 **Comparison to other approaches** Such a simulation protocol could be implemented in other
 302 simulators as well, since they use a general programming language to control the simulation flow
 303 (e.g. SLI or Python for NEST; HOC or Python for NEURON) in similar ways to Brian. However, general
 304 simulation workflows are not part of description languages like NeuroML2/LEMS. While a LEMS
 305 model description can include a `<Simulation>` element, this is only meant to specify the duration
 306 and step size of one or several simulation runs, together with information about what variables
 307 should be recorded and/or displayed. General workflows, e.g. deciding whether to run another
 308 simulation based on the results of a previous simulation, are beyond its scope. These could be
 309 implemented in a separate script in a different programming language.

310 Implementation level

311 Case study 4: Real-time audio

312 The case studies so far were described by equations and algorithms on a level that is independent of
 313 the programming language and hardware that will eventually perform the computation. However,
 314 in some cases this lower level cannot be ignored. To demonstrate this, we will consider the example
 315 presented in *Figure 6*. We want to record an audio signal with a microphone and feed this signal—in
 316 real-time—into a neural network performing a crude “pitch detection” based on the autocorrelation
 317 of the signal (*Licklider, 1962*). This model first transforms the continuous stimulus into a sequence
 318 of spikes by feeding the stimulus into an integrate-and-fire model with an adaptive threshold
 319 (*Figure 7*, l. 36–41). It then detects periodicity in this spike train by feeding it into an array of
 320 coincidence detector neurons (*Figure 6a*; *Figure 7*, l. 44–47). Each of these neurons receives the
 321 input spike train via two pathways with different delays (l. 49–51). This arrangement allows the
 322 network to detect periodicity in the input stimulus; a periodic stimulus will most strongly excite the
 323 neuron where the difference in delays matches the stimulus’ period. Depending on the periodicity
 324 present in the stimulus, e.g. for tones of different pitch (*Figure 6b* middle), different sub-populations
 325 of neurons respond (*Figure 6b* bottom).

326 To perform such a study, our simulator has to meet two new requirements: firstly, the simulation
 327 has to run fast enough to be able to process the audio input in real-time. Secondly, we need a way
 328 to connect the running simulation to an audio signal via low-level code.

329 The challenge is to make the computational efficiency requirement compatible with the require-
 330 ment of flexibility. With version 1 of Brian, we made the choice to sacrifice computational efficiency,
 331 because we reasoned that frequently in computational modelling, considerably more time was
 332 spent developing the model and writing the code than was spent on running it (often weeks versus
 333 minutes or hours; cf. *De Schutter, 1992*). However, there are obviously cases where simulation time
 334 is a bottleneck. To increase computational efficiency without sacrificing flexibility, we decided to
 335 make code generation the fundamental mode of operation for Brian 2 (*Stimberg et al., 2014*). Code
 336 generation was used previously in Brian 1 (*Goodman, 2010*), but only in parts of the simulation.
 337 This technique is now being increasingly widely used in other simulators, see *Blundell et al. (2018)*
 338 for a review.

339 In brief, from the high level abstract description of the model, we generate independent blocks
 340 of code (in C++ or other languages). We run these blocks in sequence to carry out the simulation.
 341 Typically, we first carry out numerical integration in one code block, check for threshold crossings in
 342 a second block, propagate synaptic activity in a third block, and finally run post-spike reset code in

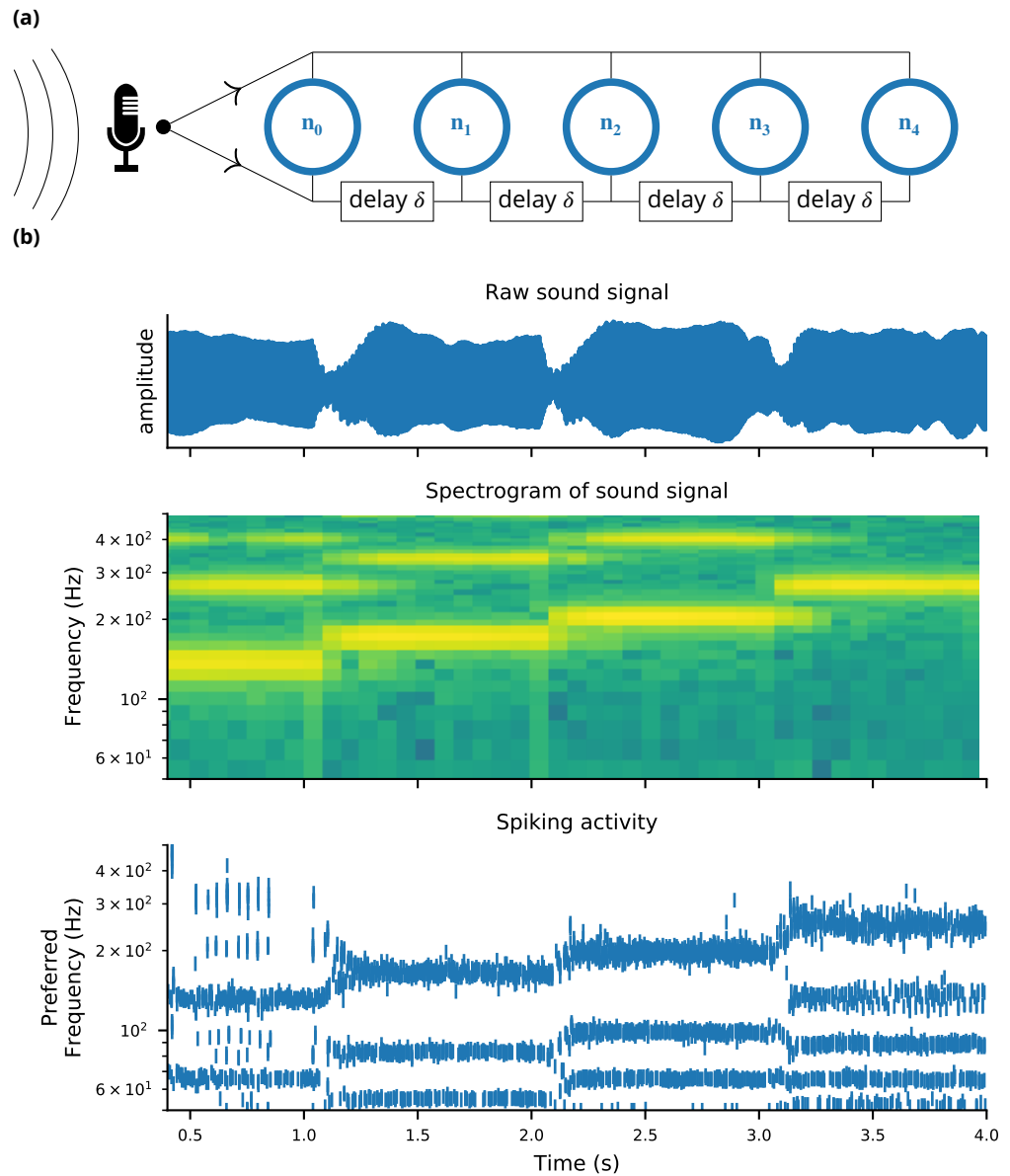


Figure 6. Case study 4: Neural pitch processing with real-time input. **(a)** Model schematic: Audio input is converted into spikes and fed into a population of coincidence-detection neurons via two pathways, one instantaneous, i.e. without any delay (top), and one with incremental delays (bottom). Each neuron therefore receives the spikes resulting from the audio signal twice, with different temporal shifts between the two. The inverse of this shift determines the preferred frequency of the neuron. **(b)** Simulation results for a sample run of the simulation code in [Figure 7](#). Top: Raw sound input (a rising sequence of tones – C, E, G, C – played on a synthesized flute). Middle: Spectrogram of the sound input. Bottom: Raster plot of the spiking response of receiving neurons (group `neurons` in the code), ordered by their preferred frequency.

```

1  from brian2 import *
2  import os
3  set_device('cpp_standalone')
4
5  sample_rate = 48*kHz; buffer_size = 128; defaultclock.dt = 1/sample_rate
6  max_delay = 20*ms; tau_ear = 1*ms; tau_th = 5*ms
7  min_freq = 50*Hz; max_freq = 1000*Hz; num_neurons = 300; tau = 1*ms; sigma = .1
8
9  @implementation('cpp', '''
10 PaStream *_init_stream() {
11     PaStream* stream;
12     Pa_Initialize();
13     Pa_OpenDefaultStream(&stream, 1, 0, paFloat32, SAMPLE_RATE, BUFFER_SIZE, NULL, NULL);
14     Pa_StartStream(stream);
15     return stream;
16 }
17
18 float get_sample(const double t) {
19     static PaStream* stream = _init_stream();
20     static float buffer[BUFFER_SIZE];
21     static int next_sample = BUFFER_SIZE;
22
23     if (next_sample >= BUFFER_SIZE)
24     {
25         Pa_ReadStream(stream, buffer, BUFFER_SIZE);
26         next_sample = 0;
27     }
28     return buffer[next_sample++];
29 }''', libraries=['portaudio'], headers=['<portaudio.h>'],
30     define_macros=[('BUFFER_SIZE', buffer_size),
31                   ('SAMPLE_RATE', sample_rate)])
32 @check_units(t=second, result=1)
33 def get_sample(t):
34     raise NotImplementedError('Use a C++-based code generation target.')
35
36 eqs_ear = '''dx/dt = (sound - x)/tau_ear: 1 (unless refractory)
37             dth/dt = (0.1*x - th)/tau_th : 1
38             sound = clip(get_sample(t), 0, inf) : 1 (constant over dt)'''
39 receptors = NeuronGroup(1, eqs_ear, threshold='x > th',
40                         reset='x = 0; th = th*2.5 + 0.01',
41                         refractory=2*ms, method='exact')
42 receptors.th = 1
43
44 eqs_neurons = '''dv/dt = -v/tau+sigma*(2./tau)**.5*xi : 1
45                 freq : Hz (constant)'''
46 neurons = NeuronGroup(num_neurons, eqs_neurons, threshold='v > 1',
47                       reset='v = 0', method='euler')
48 neurons.freq = 'exp(log(min_freq/Hz)+(i*1.0/(num_neurons-1))*log(max_freq/min_freq))*Hz'
49
50 synapses = Synapses(receptors, neurons, on_pre='v += 0.5', multisynaptic_index='k')
51 synapses.connect(n=2) # one synapse without delay; one with delay
52 synapses.delay['k == 1'] = '1/freq_post'
53
54 run(10*second)

```

Figure 7. Case study 4: Simulation code for the model shown in [Figure 6a](#). The sound input is acquired in real time from a microphone, using user-provided low-level code written in C that makes use of an Open Source library for audio input ([Bencina et al., 1999-](#)).

343 a fourth block. To generate this code, we make use of a combination of various techniques from
 344 symbolic mathematics and compilers that are available in third party Python libraries, as well as
 345 some domain specific optimisations to further improve performance (see Appendix 1 for more
 346 details, or *Stimberg et al. 2014*; *Blundell et al. 2018*). We can then run the complete simulation in
 347 one of two modes, as follows.

348 In *runtime* mode, the overall simulation is controlled by Python code, which calls out to the
 349 compiled code objects to do the heavy lifting. This method of running the simulation is the default,
 350 because despite some computational overhead associated with repeatedly switching from Python
 351 to another language, it allows for a great deal of flexibility in how the simulation is run: whenever
 352 Brian's model description formalism is not expressive enough for a task at hand, the researcher
 353 can interleave the execution of generated code with a hand-written function that can potentially
 354 access and modify any aspect of the model. This facility is widely used in computational models
 355 using Brian.

356 In *standalone* mode, additional low-level code is generated that controls the overall simulation,
 357 meaning that during the main run of the simulation it is not necessary to switch back to Python.
 358 This gives an improvement to performance, but at the cost of reduced flexibility since we cannot
 359 translate arbitrary Python code into low level code. The standalone mode can also be used to
 360 generate code to run on a platform where Python is not available or not practical (such as a GPU;
 361 *Stimberg et al. 2018*).

362 The choice of which mode to use is left to the user, and will depend on details of the simulation
 363 and how much additional flexibility is required. The performance that can be gained from using the
 364 standalone mode also depends strongly on the details of the model; we will come back to this point
 365 in the discussion.

366 The second issue we needed to address for this case study was how to connect the running
 367 simulation to an audio signal via low-level code. The general issue here is how to extend the
 368 functionality of Brian. While Brian's syntax allows a researcher to define a wide range of models
 369 within its general framework, inevitably it will not be sufficient for all computational research
 370 projects. Taking this into account, Brian has been built with extensibility in mind. Importantly, it
 371 should be possible to extend Brian's functionality and still include the full description of the model
 372 in the main Python script, i.e. without requiring the user to edit the source code of the simulator
 373 itself or to add and compile separate modules.

374 As discussed previously, the runtime mode offers researchers the possibility to combine their
 375 simulation code with arbitrary Python code. However, in some cases such as a model that requires
 376 real-time access to hardware (*Figure 6*), it may be necessary to add functionality at the target-
 377 language level itself. To this end, simulations can use a general extension mechanism: model code
 378 can refer not only to predefined mathematical functions, but also to functions defined in the target
 379 language by the user (*Figure 7*, l. 9–34). This can refer to code external to Brian, e.g. to third-party
 380 libraries (as is necessary in this case to get access to the microphone). In order to establish the
 381 link, Brian allows the user to specify additional libraries, header files or macro definitions (l. 29–31)
 382 that will be taken into account during the compilation of the code. With this mechanism the
 383 Brian simulator offers researchers the possibility to add functionality to their model at the lowest
 384 possible level, without abandoning the use of a convenient simulator and forcing them to write
 385 their model "from scratch" in a low-level language. We think it is important to acknowledge that
 386 a simulator will never have every possible feature to cover all possible models, and we therefore
 387 provide researchers with the means to adapt the simulator's behaviour to their needs at every level
 388 of the simulation.

389 **Comparison to other approaches** The NEURON simulator can include user-written C code
 390 in *VERBATIM* blocks of an NMODL description, but there is no documented mechanism to link to
 391 external libraries. Another approach to interface a simulation with external input or output is to
 392 do this on the script level. For example, a recent study (*Dura-Bernal et al., 2017*) linked a NEURON

393 simulation of the motor cortex to a virtual musculoskeletal arm, by running a single simulation
 394 step at a time, and then exchanging values between the two systems. The NEST simulator provides
 395 a general mechanism to couple a simulation to another system (e.g. another simulator) via the
 396 MUSIC interface (*Djurfeldt et al., 2010*). This framework has been successfully used to connect the
 397 NEST simulators to robotic simulators (*Weidel et al., 2016*). The MUSIC framework does support
 398 both spike-based and continuous interactions, but NEST cannot currently apply continuous-valued
 399 inputs as used here. Finally, model description languages such as NeuroML2/LEMS are not designed
 400 to capture this kind of interaction.

401 Discussion

402 Brian 2 was designed to overcome some of the major challenges we saw for neural simulators
 403 (including Brian 1). Notably: the flexibility/performance dichotomy, and the need to integrate
 404 complex computational experiments that go beyond their neuronal and network components. As a
 405 result of this work, Brian can address a wide range of modelling problems faced by neuroscientists,
 406 as well as giving more robust and reproducible results and therefore contributing to increasing
 407 reproducibility in computational science. We now discuss these challenges in more detail.

408 Brian's code generation framework allows for a solution to the dichotomy between flexibility
 409 and performance. Brian 2 improves on Brian 1 both in terms of flexibility (particularly the new,
 410 very general synapse model; for more details see appendix 5) and performance, where it performs
 411 similarly to simulators written in low-level languages which do not have the same flexibility (*Tikidji-
 412 Hamburyan et al., 2017*, also see section *Performance* below). Flexibility is essential to be useful for
 413 fundamental research in neuroscience, where basic concepts and models are still being actively
 414 investigated and have not settled to the point where they can be standardised. Performance is
 415 increasingly important, for example as researchers begin to model larger scale experimental data
 416 such as that provided by the Neuropixels probe (*Jun et al., 2017*), or when doing comprehensive
 417 parameter sweeps to establish robustness of models (*O'Leary et al., 2015*).

418 It is possible to write plugins for Brian to generate code for other platforms without modifying
 419 the core code, and there are several ongoing projects to do so. These include Brian2GeNN (*Stimberg
 420 et al., 2018*) which uses the GPU-enhanced Neural Network simulator (GeNN; *Yavuz et al. 2016*)
 421 to accelerate simulations in some cases by tens to hundreds of times, and Brian2CUDA (<https://github.com/brian-team/brian2cuda>). The modular structure of the code generation framework
 422 was designed for this in order to be ready for future trends in both high performance computing
 423 and computational neuroscience research. Increasingly, high performance scientific computing
 424 relies on the use of heterogeneous computing architectures such as GPUs, FPGAs, and even more
 425 specialised hardware (*Fidjeland et al., 2009; Richert et al., 2011; Brette and Goodman, 2012; Moore
 426 et al., 2012; Furber et al., 2014; Cheung et al., 2016*), as well as techniques such as approximate
 427 computing (*Mittal, 2016*). In addition to basic research, spiking neural networks may increasingly
 428 be used in applications thanks to their low power consumption (*Merolla et al., 2014*), and the
 429 standalone mode of Brian is designed to facilitate the process of converting research code into
 430 production code.

431 A neural computational model is more than just its components (neurons, synapses, etc.) and
 432 network structure. In designing Brian, we put a strong emphasis on the complete computational
 433 experiment, including specification of the stimulus, interaction with non-neuronal components,
 434 etc. This is important both to minimise the time and expertise required to develop computational
 435 models, but also to reduce the chance of errors (see below). Part of our approach here was to
 436 ensure that features in Brian are as general and flexible as possible. For example the equations
 437 system intended for defining neuron models can easily be repurposed for defining non-neuronal
 438 elements of a computational experiment (case study 2, *Figure 3*). However, ultimately we recognise
 439 that any way of specifying all elements of a computational experiment would be at least as complex
 440 as a fully featured programming language. We therefore simply allow users to define these aspects
 441 in Python, the same language used for defining the neural components, as this is already highly
 442

443 capable and readable. We made great efforts to ensure that the detailed work in designing and
444 implementing new features should not interfere with the goal that the user script should be a
445 readable description of the complete computational experiment, as we consider this to be an
446 essential element of what makes a computational model valuable.

447 Brian's approach to defining models leads to particularly concise code (*Tikidji-Hamburyan et al.,*
448 *2017*), as well as code whose syntax matches closely descriptions of models in papers. This is
449 important not only because it saves scientists time if they have to write less code, but also because
450 such code is easier to verify and reproduce. It is difficult for anyone, the authors of a model included,
451 to verify that thousands of lines of model simulation code match the description they have given
452 of it. An additional advantage of the clean syntax is that Brian is an excellent tool for teaching,
453 for example in the computational neuroscience textbook of *Gerstner et al. (2015)*. Expanding on
454 this point, a major issue in computational science generally, and computational neuroscience in
455 particular, is the reproducibility of computational models (*LeVeque et al., 2012; Eglon et al., 2017;*
456 *Podlaski et al., 2017; Manninen et al., 2018*). A frequent complaint of students and researchers
457 at all levels, is that when they try to implement published models using their own code, they get
458 different results. A fascinating and detailed description of one such attempt is given in *Pauli et al.*
459 *(2018)*. These sorts of problems led to the creation of the ReScience journal, dedicated to publishing
460 replications of previous models or describing when those replication attempts failed (*Rougier et al.,*
461 *2017*). A number of issues contribute to this problem, and we designed Brian with these in mind.
462 So, for example, users are required to write equations that are dimensionally consistent, a common
463 source of problems. In addition, by requiring users to write equations explicitly rather than using
464 pre-defined neuron types such as "integrate-and-fire" and "Hodgkin-Huxley", as in other simulators,
465 we reduce the chance that the implementation expected by the user is different to the one provided
466 by the simulator. We discuss this point further below, but we should note the opposing view that
467 standardization and common implementation are advantages has also been put forward (*Davison*
468 *et al., 2008; Gleeson et al., 2010; Raikov et al., 2011*). Perhaps more importantly, by making user-
469 written code simpler and more readable, we increase the chance that the implementation faithfully
470 represents the description of a model. Allowing for more flexibility and targeting the complete
471 computational experiment increases the chances that the entire simulation script can be compactly
472 represented in a single file or programming language, further reducing the chances of such errors.

473 **Comparison to other approaches**

474 We have described some of the key design choices we made for version 2 of the Brian simulator.
475 These represent a particular balance between the conflicting demands of flexibility, ease-of-use,
476 features and performance, and we now compare the results of these choices to other available
477 options for simulations.

478 There are two main differences of approach between Brian and other simulators. Firstly,
479 we require model definitions to be explicit. Users are required to give the full set of equations
480 and parameters that define the model, rather than using "standard" model names and default
481 parameters (cf. *Brette, 2012*). This approach requires a slightly higher initial investment of effort
482 from the user, but ensures that users know precisely what their model is doing and reduces the
483 risk of a difference between the implementation of the model and the description of it in a paper
484 (see discussion above). One limitation of this approach is that it makes it more difficult to design
485 tools to programmatically inspect a model, for example to identify and shut down all inhibitory
486 currents (although note that this issue remains for languages such as NeuroML and NineML that
487 are primarily based on standard models as they include the ability to define arbitrary equations).

488 The second main difference is that we consider the complete computational experiment to
489 be fundamental, and so everything is tightly integrated to the extent that an entire model can be
490 specified in a single, readable file, including equations, protocols, data analysis, etc. In Neuron and
491 NEST, model definitions are separate from the computational experiment script, and indeed written
492 in an entirely different language (see below). This adds complexity and increases the chance of

493 errors. In NeuroML and NineML, there is no way of specifying arbitrary computational experiments.
 494 One counter-argument to this approach is that clearly separating model definitions may reduce the
 495 effort in re-using models or programmatically comparing them (as in *Podlaski et al. 2017*).

496 A consequence of the requirement to make model definitions explicit, and an important feature
 497 for doing novel research, is that the simulator must support arbitrary user-specified equations.
 498 This is available in Neuron via the NMODL description format (*Hines and Carnevale, 2000*), and
 499 in a limited form in NEST using NESTML (*Plotnikov et al., 2016*). NeuroML and NineML now both
 500 include the option for specifying arbitrary equations, although the level of simulator support
 501 for these aspects of the standards is unclear. While some level of support for arbitrary model
 502 equations is now fairly widespread in simulators, Brian was the first to make this a fundamental,
 503 core concept that is applied universally. Some simulators that have since followed this approach
 504 include DynaSim (*Sherfey et al., 2018*), which is based on MATLAB, and ANNarchy (*Vitay et al., 2015*).
 505 Other new simulators have taken an alternative approach, such as Xolotl (*Gorur-Shandilya et al.,*
 506 *2018*) which is based on building hierarchical representations of neurons from a library of basic
 507 components. One aspect of the equation-based approach that is missing from other simulators is
 508 the specification of additional defining network features, such as synaptic connectivity patterns, in
 509 an equally flexible, equation-oriented way. Neuron is focused on single neuron modeling rather
 510 than networks, and only supports directly setting the connectivity synapse-by-synapse. NEST, PyNN
 511 (*Davison et al., 2008*), NeuroML, and NineML support this too, and also include some predefined
 512 general connectivity patterns such as one-to-one and all-to-all. NEST further includes a system for
 513 specifying connectivity via a “connection set algebra” (*Djurfeldt, 2012*) allowing for combinations
 514 of a few core types of connectivity. However, none have yet followed Brian in allowing the user to
 515 specify connectivity patterns via equations, as is commonly done in research papers.

516 Performance

517 Running compiled code for arbitrary equations means that code generation must be used. This
 518 requirement leads to a problem: a simulator that makes use of a fixed set of models can provide
 519 hand-optimised implementations of them, whereas a fully flexible simulator must rely on auto-
 520 mated techniques. By contrast, an advantage of automated techniques is that they can generate
 521 optimisations for specialisations of models. For example, using the CUBA benchmark (*Vogels and*
 522 *Abbott, 2005; Brette et al., 2007*) in which all neurons have identical time constants, Brian 2 is
 523 dramatically faster than Brian 1, NEURON and NEST (*Figure 8*, left). This happens because Brian
 524 2 can generate a specialised optimisation of the code since the model definition states that time
 525 constants are the same. If instead we modify the benchmark to feature heterogeneous time
 526 constants (*Figure 8*, right), then Brian 2 has to do much more work since it can no longer use these
 527 optimisations, while the run times for NEST and NEURON do not change.

528 We can make two additional observations based on this benchmark. Firstly, the benefits of
 529 parallelisation via multi-threading depend heavily on the model being simulated. For a large
 530 homogeneous population, the single threaded and multi-threaded standalone runs of Brian 2 take
 531 approximately the same time, and the single threaded run is actually faster at smaller network
 532 sizes. For the heterogeneous population, the opposite result holds: multi-threaded is always faster
 533 at all network sizes.

534 The second observation is that the advantage of running a Brian 2 simulation in standalone
 535 mode is most significant for smaller networks, at least for the single threaded case (for the moment,
 536 multi-threaded code is only available for standalone mode).

537 It should be noted, however, that despite the fact that Brian 2 is the fastest simulator at large
 538 network sizes for this benchmark, this does not mean that Brian 2 is faster than other simulators
 539 such as NEURON or NEST in general. The NEURON simulator can be used to simulate the point
 540 neuron models used in this benchmark, but with its strong focus on the simulation of biologically
 541 detailed, multi-compartment neuron models, it is not well adapted to this task. NEST, on the other
 542 hand, has been optimised to simulate very large networks, with many synapses impinging on each

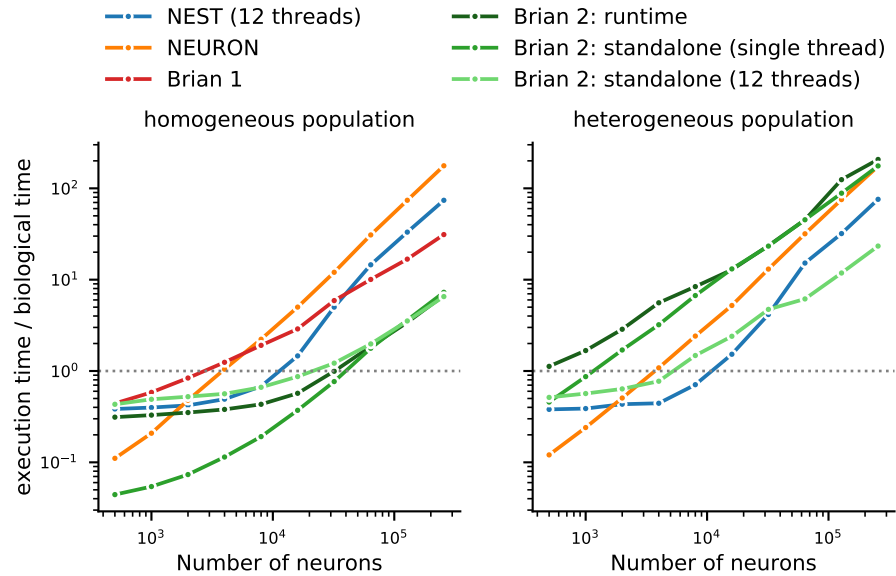


Figure 8. Benchmark of the simulation time for the CUBA network (*Vogels and Abbott, 2005; Brette et al., 2007*), a sparsely connected network of leaky-integrate and fire network with synapses modelled as exponentially decaying currents. Synaptic connections are random, with each neuron receiving on average 80 synaptic inputs and weights set to ensure ongoing asynchronous activity in the network. The simulations use exact integration, but spike spike times are aligned to the simulation grid of 0.1 ms. Simulations are shown for a homogeneous population (left), where the membrane time constant, as well as the excitatory and inhibitory time constant, are the same for all neurons. In the heterogeneous population (right), these constants are different for each neuron, randomly set between 90% and 110% of the constant values used in the homogeneous population. Simulations were performed with NEST 2.16 (blue, *Linssen et al., 2018*, RRID:SCR_002963), NEURON 7.6 (orange; RRID:SCR_005393), Brian 1.4.4 (red), and Brian 2.2.2.1 (shades of green, *Stimberg et al., 2019b*, RRID:SCR_002998). Benchmarks were run under Python 2.7.16 on an Intel Core i9-7920X machine with 12 processor cores. For NEST and one of the Brian 2 simulations (light green), simulations made use of all processor cores by using 12 threads via the OpenMP framework. Brian 2 “runtime” simulations execute C++ code via the `weave` library, while “standalone” code executes an independent binary file compiled from C++ code (see appendix 1 for details). Simulation times do not include the one-off times to prepare the simulation and generate synaptic connections as these will become a vanishing fraction of the total time for runs with longer simulated times. Simulations were run for a biological time of 10s for small networks (8000 neurons or fewer) and for 1 s for large networks. The times plotted here are the best out of 3 repetitions. Note that Brian 1.4.4 does not support exact integration for a heterogeneous population, and has therefore not been included for that benchmark.

Figure 8–source data 1. Benchmark results for the homogeneous network.

Figure 8–source data 2. Benchmark results for the heterogeneous network.

543 neuron. Most importantly, Brian's performance here strongly benefits from its focus on running
 544 simulations on individual machines where all simulation elements are kept in a single, shared
 545 memory space. In contrast, NEST and NEURON use more sophisticated communication between
 546 model elements which may cost performance in benchmarks like the one shown here, but can
 547 scale up to bigger simulations spread out over multiple machines. For a fairly recent and more
 548 detailed comparison of simulators, see *Tikidji-Hamburyan et al. (2017)*, although note that they did
 549 not test the standalone mode of Brian 2.

550 Limitations of Brian

551 The main limitation of Brian compared to other simulators is the lack of support for running large
 552 networks over multiple machines, and scaling up to specialised, high-performance clusters as
 553 well as supercomputers. While this puts a limit on the maximum feasible size of simulations, the
 554 majority of neuroscientists do not have direct access to such equipment, and few computational
 555 neuroscience studies require such large scale simulations (tens of millions of neurons). More
 556 common is to run smaller networks but multiple times over a large range of different parameters.
 557 This “embarrassingly parallel” case can be easily and straightforwardly carried out with Brian at
 558 any scale, from individual machines to cloud computing platforms or the non-specialised clusters
 559 routinely available as part of university computing services. An example for such a parameter
 560 exploration is shown in Appendix 4 *Figure 2*. This simulation strongly benefits from parallelization
 561 even on a single machine, with the simulation time reduced by about a factor of about 45 when run
 562 on a GPU.

563 Finally, let us note that this manuscript has focused exclusively on single-compartment point
 564 neuron models, where an entire neuron is represented without any spatial properties or com-
 565 partmentalisation into dendrites, soma, and axon. Such models have been extensively used for
 566 the study of network properties, but are not sufficiently detailed for studying other questions, e.g
 567 dendritic integration. For such studies, researchers typically investigate multi-compartment models,
 568 i.e. neurons modelled as a set of interconnected compartments. Currents across the membrane in
 569 each compartment are modelled in the same way as for point neurons, but there are additional
 570 axial currents with neighbouring compartments. Such models are the primary focus of simulators
 571 such as NEURON and GENESIS, but only have very limited support in simulators such as NEST. While
 572 Brian is used mostly for point neurons, it does offer support for multi-compartmental models, using
 573 the same equation-based approach (see Appendix 4, *Figure 1*). This feature is not yet as mature as
 574 those of specialised simulators such as NEURON and GENESIS, and is an important area for future
 575 development in Brian.

576 Development and availability

577 Brian is released under the free and open CeCILL 2 license. Development takes place in a public
 578 code repository at <https://github.com/brian-team/brian2> (*Brian contributors, 2012–2019*). All exam-
 579 ples in this article have been simulated with Brian 2 version 2.2.2.1 (*Stimberg et al., 2019b*). Brian
 580 has a permanent core team of three developers (the authors of this paper), and regularly receives
 581 substantial contributions from a number of students, postdocs and users (see Acknowledgements).
 582 Code is continuously and automatically checked against a comprehensive test suite run on all
 583 platforms, with almost complete coverage. Extensive documentation, including installation instruc-
 584 tions, is hosted at <http://brian2.readthedocs.org>. Brian is available for Python 2 and 3, and for the
 585 operating systems Windows, OS X and Linux; our download statistics show that all these versions
 586 are in active use. More information can be found at <http://briansimulator.org/>.

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794 **Appendix 1**795 **Design details**

796 In this appendix, we provide further details about technical design decisions behind the
 797 Brian simulator. We also more exhaustively comment on the simulation code of the four
 798 case studies. Note that the example code provided as jupyter notebooks (https://github.com/brian-team/brian2_paper_examples; *Stimberg et al. 2019a*) has extensive additional
 799 annotations as well.
 800

801 **Mathematical level**802 **Physical units**

803 Neural models are models of a physical system, and therefore variables have physical
 804 dimensions such as voltage or time. Accordingly, the Brian simulator requires quantities
 805 provided by the user, such as parameters or initial values of dynamical variables, to be
 806 specified in consistent physical units such as mV or s. This is in contrast to the approach
 807 of most other simulators, which simply define expected units for all model components,
 808 e.g. units of mV for the membrane potential. This is a common source of error because
 809 conventions are not always obvious and can be inconsistent. For example, while membrane
 810 surface area is often stated in units of μm^2 , channel densities are often given in mS cm^{-2} . To
 811 remove this potential source of error, the Brian simulator enforces explicit use of units. It
 812 automatically takes care of conversions—multiplying a resistance (dimensions of Ω) with
 813 a current (dimensions of A) will result in a voltage (dimensions of V)—and raises an error
 814 when physical dimensions are incompatible, e.g. when adding a current to a resistance. Unit
 815 consistency is also checked within textual model descriptions (e.g. *Figure 2*, l. 8–18) and
 816 variable assignments (e.g. l. 23–27). To make this possible, a dimension in SI units has to be
 817 assigned to each dimensional model variable in the model description (l. 8–18).

818 **Model dynamics**

819 Neuron and synapse models are generally hybrid systems consisting of continuous dynamics
 820 described by differential equations and discrete events (*Brette et al., 2007*).

821 In the Brian simulator, differential equations are specified in strings using mathematical
 822 notation (*Figure 2*, l. 8–18). Differential equations can also be stochastic by using the symbol
 823 ξ_i representing the noise term $\xi(t)$ (*Figure 3c*, l. 8). The numerical integration method can
 824 be specified explicitly, e.g. the pyloric circuit model chooses a second-order Runge-Kutta
 825 method (*Figure 2*, l. 22); without specification, an appropriate method is automatically
 826 chosen and reported. To this end, the user-provided equations are analysed symbolically
 827 using the Python package sympy (*Meurer et al., 2017*), and transformed into a sequence
 828 of operations to advance the system's state by a single time step (for more details, see
 829 *Stimberg et al., 2014*).

830 This approach applies both to neuron models and to synaptic models. In many models,
 831 synaptic conductances do not need to be calculated for each synapse individually, instead
 832 they can be lumped into a single post-synaptic variable that is part of the neuronal model
 833 description. In contrast, non-linear synaptic dynamics as in the pyloric network example need
 834 to be calculated for each synapse individually. Using the same formalism as for neurons, the
 835 synaptic model equations can describe dynamics with differential equations (e.g. *Figure 2*,
 836 l. 31–32/44–47). Post-synaptic conductances or currents can then be calculated individually
 837 and summed up for each post-synaptic neuron as indicated by the (`summed`) annotation
 838 (l. 32 and 46).

839 Neuron- or synapse-specific values which are not updated by differential equations are
 840 also included in the string description. This can be used to define values that are updated
 841 by external mechanisms, e.g. the synaptic currents in each neuron (l. 15–16) are updated
 842 by the respective synapses (l. 32 and l. 46). The same mechanism can also be used for
 843 neuron-specific parameters such as the calcium target value (l. 17), or the label identifying
 844 the neuron type (l. 18). For optimisation, the flag `(constant)` can be added to indicate that
 845 the value will not change during a simulation.

846 Neural simulations typically refer to two types of discrete events: production of a spike,
 847 and reception of a spike. A spike is produced by a neuron when a certain condition on its vari-
 848 ables is met. A typical case is the integrate-and-fire model, where a spike is produced when
 849 the potential reaches a threshold of a fixed value. But there are other cases when the condi-
 850 tion is more complex, for example when the threshold is adaptive (**Platkiewicz and Brette,**
 851 **2011**). To support conditions of all kind, Brian expects the user to define a mathematical
 852 expression as the `threshold`. In the case study 1, a spike is triggered whenever $v > -20\text{ mV}$
 853 (**Figure 2**, l. 21). No explicit resetting takes place, since the model dynamics describe the
 854 membrane potential trajectory during an action potential. For a simpler integrate-and-fire
 855 model as the one used in case study 2, the membrane potential is reset to a fixed value
 856 after the threshold crossing (**Figure 3**, l. 12). Such spike-triggered actions are most generally
 857 specified by providing one or more assignments and operations (`reset`) that should take
 858 place if the threshold condition is fulfilled; in the case study 1, this is mechanism is used to
 859 update the calcium trace (**Figure 2**, l. 21).

860 Once a spike is produced, it may affect variables of synapses and post-synaptic neurons
 861 (possibly after a delay). Again, this is specified generally as a series of assignments and
 862 operations. In the pyloric circuit example, this does not apply because the synaptic effect
 863 is continuous and not triggered by discrete spikes. In case study 2 (**Figure 3**) however,
 864 each spike has an instantaneous effect. For example, when a motoneuron spikes, the
 865 eye resting position is increased or decreased by a fixed amount. This is specified by
 866 `on_pre='x0_post += w'` (l. 15), where `on_pre` is a keyword for stating what operations should
 867 be executed when a pre-synaptic spike is received. These operations can refer to both local
 868 synaptic variables (here w , defined in the synaptic model) and variables of the pre- and
 869 postsynaptic neuron (here x_0 , a variable of the post-synaptic neuron). In the same way, the
 870 `on_post` keyword can be used to specify operations executed when a postsynaptic spike is
 871 received, which allows defining various types of spike-timing-dependent models.

872 This general definition scheme applies to neurons and synapses, but as case study 2
 873 (**Figure 3**) illustrates, it can also be used to define dynamical models of muscles and the
 874 environment. It also naturally extends to the modelling of non-neuronal elements of the
 875 brain such as glial cells (**Stimberg et al., 2019c**).

876 Links between model components

The equations defining the dynamics of variables can only refer to other variables within the
 same model component, e.g. within the same group of neurons or synapses. Connections
 to other components have to be explicitly modelled using synaptic connections as explained
 above. However, we may sometimes also need to directly refer to the state of variables in
 other model component. For example, in case study 2 (**Figure 3**), the input to retinal neurons
 depends on eye and object positions, which are updated in a group separate from the group
 representing the retinal neurons (**Figure 3c**, l. 3–9). This can be expressed by defining a
 “linked variable”, which refers to a variable defined in a different model component. In the
 group modelling the retinal neurons, the variables `x_object` and `x_eye` are annotated with
 the `(linked)` flag to state that they are references to variables defined elsewhere (l. 23–
 24). This link is then made explicit by stating the group and variable they refer to via the

linked_var function (l. 28–29).

Initialisation

The description of its dynamics does not yet completely define a model, we also need to define its initial state. For some variables, this initial state can simply be a fixed value, e.g. in the pyloric network model, the neurons' membrane potential is initialised to the resting potential v_r (Figure 2 l. 23). In the general case, however, we might want to calculate the initial state; Brian therefore accepts arbitrary mathematical expressions for setting the initial value of state variables. These expressions can refer to model variables, as well as to pre-defined constant such as the index of a neuron within its group (i), or the total number of neurons within a group (N), as well as to pre-defined functions such as `rand()` (providing uniformly distributed random numbers between 0 and 1). In case study 1, we use this mechanism to initialise variables w and z randomly (Figure 2, l. 25–26); in case study 2, we assign individual preferred positions to each retinal neuron, covering the space from -1 to 1 in a regular fashion (Figure 3c, l. 30).

Mathematical expressions can also be used to select a subset of neurons and synapses and make conditional assignments. In case study 1, we assign a specific value to the conductance of synapses between ABPD and LP neurons by using the selection criterion `'label_pre == ABPD and label_post == LP'` (Figure 2, l. 36), referring to the custom `label` identifier of the pre- and post-synaptic neuron that has been introduced as part of the neuron model definition (l. 18). In this example there is only a single neuron per type, but the syntax generalises to groups of neurons of arbitrary size and is therefore preferable to the explicit use of numerical indices.

Synaptic connections

The second main aspect of model construction is the creation of synaptic connections. For maximal expressivity, we again allow the use of mathematical expressions to define rules of connectivity. For example, in case study 1, following the schematic shown in Figure 1a, we would like to connect neurons with fast glutamatergic synapses according to two rules: 1) connections should occur between all groups, but not within groups of the same neuron type; 2) there should not be any connections from PY neurons to AB/PD neurons. We can express this with a string condition following the same syntax that we used to set initial values for synaptic conductances earlier (Figure 2, l. 35):

```
fast.connect('label_pre!=label_post and not (label_pre==PY and label_post==ABPD)')
```

For more complex examples, in particular connection specifications based on the spatial location of neurons, see *Stimberg et al. (2014)*.

For larger networks, it can be wasteful to check a condition for each possible connection. Brian therefore also offers the possibility to use a mathematical expression to directly specify the projections of each neuron. In the eye movement example, each retinal neuron on the left hemifield (i.e. $x_{\text{neuron}} < 0$) should connect to the first motoneuron (index 0), while neurons on the right hemifield (i.e. $x_{\text{neuron}} > 0$) should connect to the second motoneuron (index 1). We can express this connection scheme by defining j , the postsynaptic target index, for each presynaptic neuron accordingly (with the `int` function converting a truth value into 0 or 1):

```
sensorimotor_synapses.connect(j='int(x_neuron_pre > 0)')
```

This syntax can also be extended to generate more than one post-synaptic target per pre-synaptic neuron, using a syntax borrowed from Python's generator syntax (*Hettinger, 2002*, see the Brian 2 documentation at <http://brian2.readthedocs.io> for more details) These mechanisms can also be used to define stochastic connectivity schemes, either by specifying

a fixed connection probability that will be evaluated in addition to the given conditions, or by specifying a connection probability as a function of pre- and post-synaptic properties.

Specifying synaptic connections in the way presented here has several advantages over alternative approaches. In contrast to explicitly enumerating the connections by referring to pre- and post-synaptic neuron indices, the use of mathematical expressions transparently conveys the logic behind the connection pattern and automatically scales with the size of the connected groups of neurons. These advantages are shared with simulators that provide pre-defined connectivity patterns such as “one-to-one” or “all-to-all”. However, such approaches are not as general—e.g. they could not concisely define the connectivity pattern shown in *Figure 1a*—and can additionally suffer from ambiguity. For example, should a group of neurons that is “all-to-all” connected to itself form autapses or not (cf. *Crook et al., 2012*)?

Computational experiment level

The Brian simulator allows the user to write complete experiment descriptions that include both the model description and the simulation protocol in a single Python script as exemplified by the case studies in this article. In this section, we will discuss how the Brian simulator interacts with the statements and programming logic expressed in the surrounding script code.

Simulation flow

In the case study 3 we use a specific simulation workflow, an iterative approach to finding a parameter value (*Figure 4a*). Many other simulation protocols are regularly used. For example, a simulation might consist of several consecutive runs, where some model aspect such as the external stimulation changes between runs. Alternatively, several different types of models might be tested in a single script where each is run independently. Or, a non-deterministic simulation might be run repeatedly to sample its behaviour. Capturing all these potential protocols in a single descriptive framework is hopeless, we therefore need the flexibility of a programming language with its control structures such as loops and conditionals.

Brian offers two main facilities to assist in implementing arbitrary simulation protocols. Simulations can be continued at their last state, potentially after activating/deactivating model elements, or changing global or group-specific constants and variables as shown above. Additionally, simulations can revert back to a previous state using the functions `store` and `restore` provided by Brian. In the example script shown in *Figure 5*, this mechanism is used to reset the network to an initial state after each iteration. The same mechanism allows for more complex protocols by referring to multiple states, e.g. to implement a train/test/validate protocol in a synaptic plasticity setting.

Providing explicit support for this functionality is not only a question of convenience; while the user could approximate this functionality by storing and resetting the systems state variables (membrane potentials, gating variables, etc.) manually, some model aspects such as action potentials that have not yet triggered synaptic effects (due to synaptic delays) are not easily accessible to the user.

Model component scheduling

During each time step of a simulation run, several operations have to be performed. These include the numerical integration of the state variables, the propagation of synaptic activity, or the application of reset statements for neurons that emitted an action potential. All these operations have to be executed in a certain order. The Brian simulator approaches this issue in a flexible and transparent way: each operation has an associated clock with a certain time

granularity Δt , as well as a “scheduling slot” and a priority value within that slot. Together, these elements determine the order of all operations across and within time steps.

By default, all objects are associated with the same clock, which simplifies setting a global simulation timestep for all objects (**Figure 5**, l. 2). However, individual objects may choose a different timestep, e.g. to record synaptic weights only sporadically during a long-running simulation run. In the same way, Brian offers a default ordering of all operations during a time step, but allows to change the schedule that is used, or to reschedule individual objects to other scheduling slots.

This amount of flexibility might appear to be unnecessary at a first glance and indeed details of the scheduling are rarely reported when describing models in a publication. Still, subtle differences in scheduling can have significant impact on simulation results (see **Figure 1** in **Appendix 2** for an illustration). This is most obvious when investigating paradigms such as spike-timing-dependent-plasticity with a high sensitivity to small temporal differences (**Rudolph and Destexhe, 2007**).

Name resolution

Model descriptions refer to various “names”, such as variables, constants, or functions. Some of these references, such as function names or global constants, will have the same meaning everywhere. Others, such as state variables or neuron indices, will depend on the context. This context is defined by the model component, i.e. the group of neurons or the set of synapses, to which the description is attached. For example, consider the assignment to g_{Na} (the maximum conductance of the sodium channel) in **Figure 5** (l. 20). Here, $g_{\text{Na_min}}$ and $g_{\text{Na_max}}$ refer to global constants (defined in l. 6)^a, whereas i , the neuron index, is a vector of values with one value for each neuron, and N refers to the total number of elements in the respective group.

It is important to note that the context is also given by its position in the program flow. For example, if we want to set the initial value for the gating variable m to its steady value, then this value will depend on the membrane potential v via the expressions for α_m and β_m . The order in which we set the values for v and m does therefore matter:

```
neuron.v = 0*mV
neuron.m = '1/(1 + betam/alpham)'
```

While this might appear trivial, it shows how the procedural aspect of models, i.e. the order of operations, can be important. A purely descriptive approach, for example stating initial values for all variables as part of the model equations, would not always be sufficient.^b

Some Python statements are translated into code that is run immediately, for example initialising a variable or creating synapses. Others are translated into code that is run at a later time. For example, the code to numerically integrate differential equations is not run at the point where those equations are defined, but rather at the point when the simulation is run via a call to the `run()` function. In this case, any named constants referred to in the equations will use their value at the time that the `run()` function is called, and not the value at the time the equations are defined. This allows for that value to change between multiple calls to `run()`, which may be useful to switch between global behaviours. For example, a typical use case is running with no external input current for a certain time to allow a neuron to settle into its stationary state, and then running with the current switched on by just changing the value of a constant from zero to some nonzero value between two consecutive `run()` calls.

Implementation level

Code generation

In order to combine the flexibility and ease-of-use of high-level descriptions with the execution speed of low-level programming languages such as C, we employ a code generation approach (*Goodman, 2010*). This code generation consists of three steps. The textual model description will first be transformed into a “code snippet”. The generation of such a code snippet requires various transformations of the provided model description: some syntax elements have to be translated (e.g. the use of the `**` operator to denote the power operation to a call to the `pow` function for C/C++), variables that are specific to certain neurons or synapses have to be properly indexed (e.g. a reset statement $v = -70\text{mV}$ has to be translated into a statement along the lines of `v[neuron_index] = -70*mV`), and finally sequences of statements have to be expressed according to the target language syntax (e.g. by adding a semicolon to the end of each statement for C/C++). In a second step, these code snippets will then be embedded into a predefined target-code template, specific to the respective computation performed by the code. For example, the user-provided description of an integrate-and-fire neuron’s reset would be embedded into a loop that iterates over all the neurons that emitted an action potential during the current time step. Finally, the code has to be compiled and executed, giving it access to the memory location that the code has to read and modify. For further details on this approach, see *Goodman (2010)*; *Stimberg et al. (2014)*.

Code optimisation

Code resulting from the procedure described above will not necessarily perform computations in the most efficient way. Brian therefore uses additional techniques to further optimise the code for performance. Consider for example the `x` variable—representing the receptor activity—in *Figure 7*, described by the differential equation in l. 36. This equation can be integrated analytically, and the above described code generation process would therefore generate code like the following (here presented as “pseudo-code”):

```
for each neuron:
    x_new = sound + exp(-dt / tau_ear) * (sound - x_old)
```

However, the expression that is calculated for every neuron contains `exp(-dt / tau_ear)` which is not only identical for all neurons but also relatively costly to evaluate. Brian will identify such constant expressions, and calculate them only once outside of the loop:

```
c = exp(-dt / tau_ear)
for each neuron:
    x_new = sound + c * (sound - x_old)
```

In addition to this type of optimisation, the Brian simulator will also simplify arithmetic expressions, such as replacing `0 * x` by `0`, or `x / x` by `1`. While all these optimizations could in principle also be performed by the programming-language compiler (e.g. `gcc`), we have found that performing these changes before handing over the code to the compiler led to bigger and more reliable performance benefits.

Code execution: runtime mode

After the code generation process, each model component has been transformed into one or more “code objects”, each performing a specific computational task. For example, a group of integrate-and-fire neurons would typically result in three code objects. The first would be responsible for integrating the state variables over a single timestep, the second for checking the threshold condition to determine which neurons emit an action potential,

and the third for applying the reset statements to those neurons. By default, these code objects will be executed in Brian's "runtime mode", meaning that the simulation loop will be executed in Python and then call each of the code objects to perform the actual computation (in the order defined by the scheduling as described in the previous section). Note that while the code objects will typically be based on generated C++ code, they can be compiled and executed from within Python using binding libraries such as *weave* (formerly part of *scipy*; *Jones et al. 2001*–) or *Cython* (*Behnel et al., 2011*).

This "mixed" approach to model execution leaves the simulation control to the main Python process while the actual computations are performed in compiled code, operating on shared memory structures. This results in a considerable amount of flexibility: whenever Brian's model description formalism is not expressive enough for a task at hand, the researcher can interleave the execution of generated code with a hand-written function that can potentially access and modify any aspect of the model. In particular, such a function could intervene in the simulation process itself, e.g. by interrupting the simulation if certain criteria are met. The jupyter notebook at https://github.com/brian-team/brian2_paper_examples contains an interactive version of case study 2 (*Figure 3*). In this example, the aforementioned mechanism is used to allow the user to interactively control a running Brian simulation, as well as for providing a graphical representation of the results that updates continuously.

While having all these advantages, the back-and-forth between the main loop in Python and the code objects also entails a performance overhead. This performance overhead takes a constant amount of time per code object and time step and does therefore matter less if the individual components perform long-running computations, such as for large networks (*Brette and Goodman, 2011*, see also *Figure 8*). On the other hand, for simulations of small or medium-sized networks, such as the network presented in case study 4 (*Figure 6*), this overhead can be considerable and the alternative execution mode presented in the following section might provide a better alternative.

Code execution: standalone mode

As an alternative to the mode of execution presented in the previous section, the Brian simulator offers the so-called "standalone mode", currently implemented for the C++ programming language. In this mode, Brian generates code that performs the simulation loop itself and executes the operations according to the schedule. Additionally, it creates code to manages the memory for all state variables and other data structures such as the queuing mechanism used for applying synaptic effects with delays. This code, along with the code of the individual code objects, establishes a complete "standalone" version of the simulation run. When the resulting binary file is executed, it will perform the simulation and write all the results to disk. Since the generated code does not depend on any non-standard libraries, it can be easily transferred to other machines or architectures (e.g. for robotics applications). The generated code is free from any overhead related to Python or complex data structures and therefore executes with high performance.

For many models, the use of this mode only requires the researcher to add a single line to the simulation script (declaring `set_device('cpp_standalone')`), all aspects of the model descriptions, including assignments to state variables and the order of operations will be faithfully conserved in the generated code. The Python script will transparently compile and execute the standalone code, and then read the results back from disk so that the researcher does not have to adapt their analysis routines.

However, in contrast to the runtime execution mode presented earlier, it is not possible to interact with the simulation during its execution from within the Python script. In addition, certain programming logic is no longer possible, since all actions such as synapse generation

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or variable assignments are not executed when they are stated, but only as part of the simulation run.

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In this execution mode, simulations of moderate size and complexity can be run in real-time (**Figure 8**), enabling studies such as the one presented in case study 4 (**Figure 6**). Importantly, this mode does not require the researcher to be actively involved in any details of the compilation, execution of the simulation or the retrieval of the results.

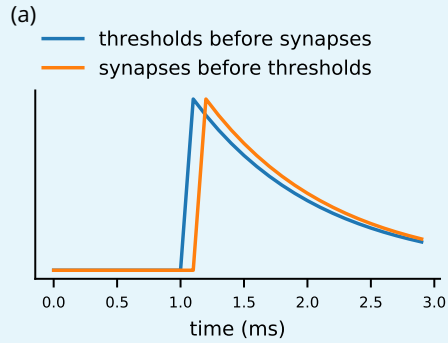
^aBrian also offers an alternative system where global constants and functions are explicitly provided via a Python dictionary instead of being deduced from values defined in the execution environment, but this system will not be further discussed here.

^bHowever, in this specific case, setting v to 0 mV is unnecessary, since Brian automatically assigns the value 0 to all uninitialised variables.

1123 **Appendix 2**

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Simulation scheduling



(b)

```
1 from brian2 import *
2
3 tau = 1*ms
4 spikes = SpikeGeneratorGroup(1, [0], [1]*ms)
5 target = NeuronGroup(1, 'dv/dt = -v/tau : 1')
6 synapses = Synapses(spikes, target,
7                     on_pre='v += 1')
8 synapses.connect()
9 mon = StateMonitor(target, 'v', record=True)
```

(c)

```
10 # thresholds before synapses (default)
11 magic_network.schedule = ['start',
12                           'groups',
13                           'thresholds',
14                           'synapses',
15                           'resets',
16                           'end']
17 run(3*ms)

# synapses before thresholds
magic_network.schedule = ['start',
                          'groups',
                          'synapses',
                          'thresholds',
                          'resets',
                          'end']
run(3*ms)
```

(d)

object	part of	Clock dt	when	order	active
mon (<i>StateMonitor</i>)	mon (<i>StateMonitor</i>)	100. us (every step)	start	0	yes
target_stateupdater (<i>StateUpdater</i>)	target (<i>NeuronGroup</i>)	100. us (every step)	groups	0	yes
spikes (<i>SpikeGeneratorGroup</i>)	spikes (<i>SpikeGeneratorGroup</i>)	100. us (every step)	thresholds	0	yes
synapses_pre (<i>SynapticPathway</i>)	synapses (<i>Synapses</i>)	100. us (every step)	synapses	-1	yes

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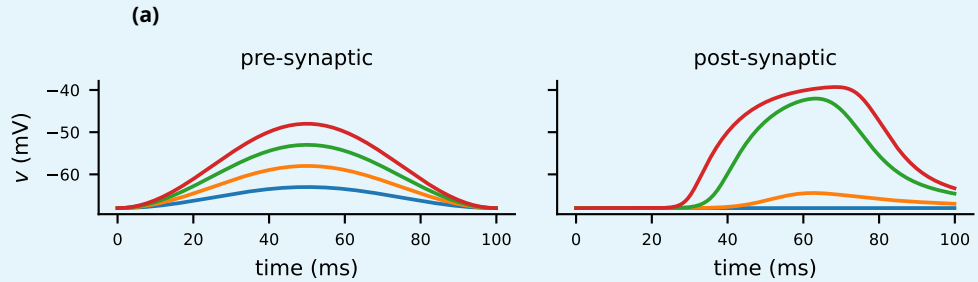
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Appendix 2 Figure 1. Demonstration of the effect of scheduling simulation elements. **(a)** Timing of synaptic effects on the post-synaptic cell for the two simulation schedules defined in (c). **(b)** Basic simulation code for the simulation results shown in (a). **(c)** Definition of a simulation schedule where threshold crossings trigger spikes and – assuming the absence of synaptic delays – their effect is applied directly within the same simulation time step (left; see blue line in (a)), and a schedule where synaptic effects are applied in the time step following a threshold crossing (right; see orange line in (a)). **(d)** Summary of the scheduling of the simulation elements following the default schedule (left code in (c)), as provided by Brian’s `scheduling_summary` function. Note that for increased readability, the objects from (b) have been explicitly named to match the variable names. Without this change, the code in (b) leads to the use of standard names for the objects (`spikegeneratorgroup`, `neurongroup`, `synapses`, and `statemonitor`).

1138 Appendix 3

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Model definitions in other simulation software



(b) Brian code:

```

eqs_slow = '''
I_slow_post = g_slow*m_slow*(v_post-E_syn) : amp (summed)
dm_slow/dt = k_1*(1-m_slow)/(1+exp(s_slow*(V_slow-v_pre)))
              - k_2*m_slow : 1 (clock-driven)
'''

slow_synapses = Synapses(circuit, circuit, model=eqs_slow, method='exact')
slow_synapses.connect('label_pre == ABPD and label_post != ABPD')

```

(c) C++ code:

```

double get_ABLPsyn_G(double deltaT){
    m_ABLPsyn_inf=lookupsigmoid((V_ABLPsyn_thresh-V_mem[0])/V_ABLPsyn_slope);
    tau_ABLPsyn=(1.0-m_ABLPsyn_inf)*tau_ABLPsyn_diss;
    m_ABLPsyn=m_ABLPsyn+(m_ABLPsyn_inf-m_ABLPsyn)*deltaT/tau_ABLPsyn;
    return G_ABLPsyn_max*m_ABLPsyn;
}
//...
void update_model_neurons(double update_T)
{
    //...
    G_ABLPsyn_now=get_ABLPsyn_G(update_T);
    V_ABLPsyn_inf=G_ABLPsyn_now*E_ABLPsyn;
    //...
}

```

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Appendix 3 Figure 1. Graded synapse model. (a) Demonstration of the effect of the graded synapse model used in case study 1 (Figure 1, Figure 2). On the left, the membrane potential excursion of a pre-synaptic neuron is modeled by a squared sinusoidal function of time with varying amplitudes from 5 mV to 20 mV. The plot on the right shows the post-synaptic membrane potential of a cell receiving graded synaptic input from the pre-synaptic cell via the graded synapse model from case study 1 (slow cholinergic synapse, cf. *Golowasch et al., 1999*). The post-synaptic cell is modeled here as a simple leaky integrator with a single synaptic input current. (b) Code excerpt showing the Brian 2 definition of the graded synapse model used in (a), taken from the code used in case study 1 (Figure 2). (c) Code excerpt defining a graded synapse model in C++ as part of “The Pyloric Network Model Simulator” (<http://www.biology.emory.edu/research/Prinz/database-sensors/>, *Günay and Prinz, 2010*). The complete code is 3,510 lines.

(d) NeuroML2:

```
<gradedSynapse id="gs" conductance="5pS" delta="5mV" Vth="-55mV"
k="0.025per_ms" erev="0mV"/>
```

LEMS:

```
<ComponentType name="gradedSynapse" extends="baseGradedSynapse">
  <Property name="weight" dimension="none" defaultValue="1"/>
  <Parameter name="conductance" dimension="conductance"/>
  <Parameter name="delta" dimension="voltage">
  <Parameter name="k" dimension="per_time">
  <Parameter name="Vth" dimension="voltage">
  <Parameter name="erev" dimension="voltage">
  <Exposure name="i" dimension="current"/>
  <Exposure name="inf" dimension="none"/>
  <Exposure name="tau" dimension="time"/>
  <Requirement name="v" dimension="voltage"/>
  <InstanceRequirement name="peer" type="baseGradedSynapse"/>
  <Dynamics>
    <StateVariable name="s" dimension="none"/>
    <DerivedVariable name="vpeer" dimension="voltage" select="peer/v"/>
    <DerivedVariable name="inf" dimension="none"
      value="1/(1 + exp((Vth - vpeer)/delta))" exposure="inf"/>
    <DerivedVariable name="tau" dimension="time"
      value="(1-inf)/k" exposure="tau"/>
    <DerivedVariable name="i" exposure="i"
      value="weight * conductance * s * (erev-v)"/>
    <TimeDerivative variable="s" value="s_rate" />
  </Dynamics>
</ComponentType>
```

(e) NEURON (NMODL):

```
INDEPENDENT {t FROM 0 TO 1 WITH 1 (ms)}
NEURON {
  POINT_PROCESS int1_lgsyn
  POINTER vpre
  RANGE gmax, g, e, i
  NONSPECIFIC_CURRENT i
}
UNITS {
  (nA) = (nanoamp)
  (mV) = (millivolt)
  (umho) = (micromho)
}
PARAMETER {
  gmax=0 (umho)
  e=0 (mV)
  v (mV)
}
STATE { synon synoff}
ASSIGNED {
  i (nA)
  g (umho)
  vpre (mV)
}
BREAKPOINT {
  SOLVE syn METHOD sparse
  g = gmax *synon
  i = g*(v - e)
}
KINETIC syn {
  ~ synoff <-> synon (syninf(vpre)/tausyn(vpre),
(1-syninf(vpre))/tausyn(vpre))
}
INITIAL {
  synon = 0.0
  synoff = 1.0
}
FUNCTION syninf(v){
  syninf = 1/(1+exp(-0.5*(v+49)))
}
FUNCTION tausyn(v){
  tausyn = 2+98/(1+exp(-0.5*(v+49)))
}
}
```

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Appendix 3 Figure 2. Graded synapse model (cont.). **(d)** Definition of a graded synapse model in NeuroML2/LEMS. The graded synapse model as described in *Prinz et al. (2004)* has been added as a “core type” to the (not yet finalized) NeuroML2 standard and can therefore be accessed under the name `gradedSynapse` (top). It is fully defined via the LEMS definition partially reproduced here. **(e)** A definition of a graded synapse in the stomatogastric system, written in the NMODL language for the NEURON simulator. This model has been implemented in *Nadim et al. (1998)*, see <https://senselab.med.yale.edu/ModelDB/showmodel.cshhtml?model=3511>.

1162 Appendix 4

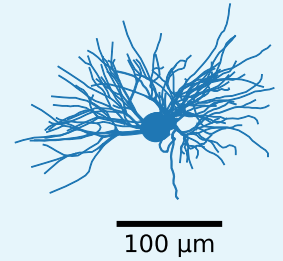
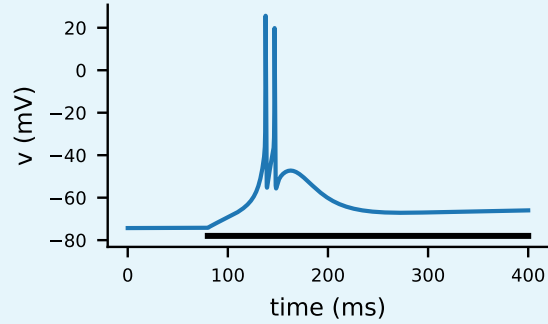
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Additional Brian examples

Multi-compartmental models

1164

(a)



(b)

```

1 # Constants
2 E1 = -76.5*mV; E_Na = 50*mV; E_K = -100*mV
3 # ...
4 eqs = Equations('''
5 Im = g1*(E1-v) - I_Na - I_K - I_T: amp/meter**2
6 I_inj : amp (point current)
7
8 # HH-type currents for spike initiation
9 g_Na : siemens/meter**2
10 I_Na = g_Na * m**3 * h * (v-E_Na) : amp/meter**2
11 v2 = v - VT : volt # shifted membrane potential (Traub convention)
12 dm/dt = (0.32*(mV**-1)*(13.*mV-v2)/
13          (exp((13.*mV-v2)/(4.*mV))-1.)*(1-m)-0.28*(mV**-1)*(v2-40.*mV)/
14          (exp((v2-40.*mV)/(5.*mV))-1.)*m) / ms * tadj_HH: 1
15 # ...
16 ''')
17 # Load morphology from SWC file
18 morpho = Morphology.from_file('tc200.CNG.swc')
19 neuron = SpatialNeuron(morpho, eqs, Cm=0.88*uF/cm**2, Ri=173*ohm*cm,
20                       method='exponential_euler')
21 # Only the soma has Na/K channels
22 neuron.main.g_Na = 100*msiemens/cm**2
23 neuron.main.g_K = 100*msiemens/cm**2
24 neuron.P_Ca = 1.7e-5*cm/second
25 # Distal dendrites
26 neuron.P_Ca['(distance + length/2) > 11*um'] = 8.5e-5*cm/second
27 neuron.v = -74*mV
28 neuron.m_T = 'm_T_inf'
29 neuron.h_T = 'h_T_inf'
30 mon = StateMonitor(neuron, ['v'], record=morpho[0]) # Record at soma

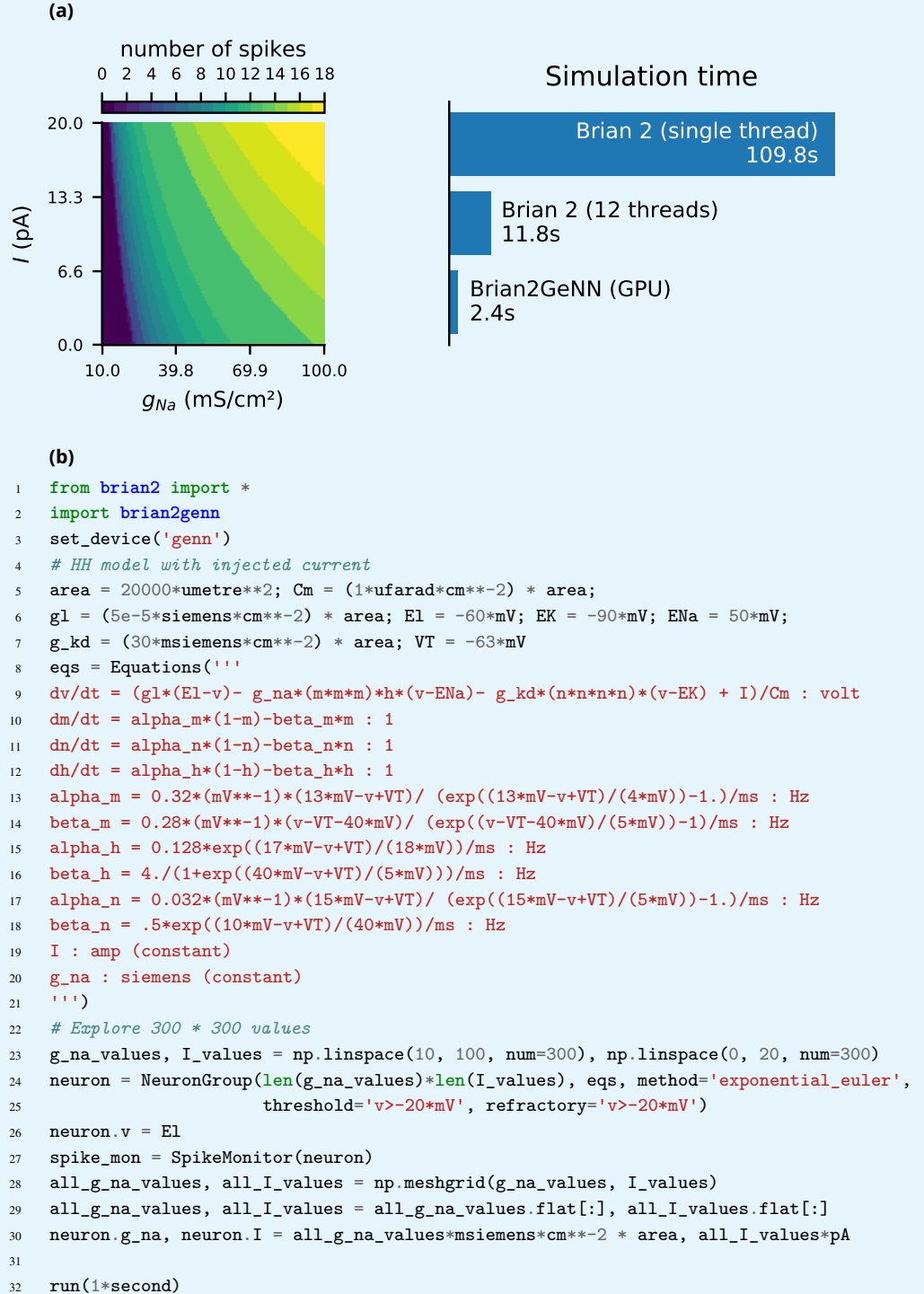
```

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1166 **Appendix 4 Figure 1.** A multi-compartment model of a thalamic relay cell. **(a)** Simulation of a thalamic
1167 relay cell with increased T-current in distal dendrites (partially reproducing Figure 9C from *Destexhe*
1168 *et al., 1998*). The plot shows the somatic membrane potential for a current injection of 75 pA during the
1169 period marked by the black line. The model consists of a total of 1291 compartments and is based on
1170 the morphology available on [NeuroMorpho.Org](https://neuro.morpho.org/) (*Ascoli et al., 2007*) under the ID NMO_00881, displayed
1171 on the right. This morphology is a reconstruction of a cell in the rat's ventrobasal complex, originally
1172 described in *Huguenard and Prince (1992)*. **(b)** Selected lines from the simulation code implementing
1173 the model shown in (a), focussing on the differences to single-compartmental models (as shown in case
1174 studies 1–4).

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Parameter exploration



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Appendix 4 Figure 2. Parameter exploration over two parameters. (a) In a single-compartment neuron model of the Hodgkin-Huxley type (following *Traub and Miles, 1991*), we record the number of spikes over 1 s while varying the strength of a constant input current I , and the density of the sodium conductance g_{Na} for a total of 300×300 values. The bars on the right show the simulation time on the same machine used for *Figure 8* when using Brian 2's C++ standalone mode with a single thread (top), with 12 threads (middle), or when simulating it on a NVIDIA GeForce RTX 2080 Ti graphics card via the Brian2GeNN (*Stimberg et al., 2018*) interface to the GeNN (*Yavuz et al., 2016*) simulator (bottom). (b) Code for the simulation shown in (a), here configured to run on the GPU via the Brian2GeNN interface (l.2-3).

1188 **Appendix 5**1189 **Comparison of Brian 1 and 2**

1190 Brian 2 was rewritten from scratch, however it was designed to match the syntax of Brian 1
 1191 as closely as possible, breaking compatibility only when essential. Upgrading scripts from
 1192 Brian 1 to Brian 2 is therefore usually straightforward. A detailed guide is available in the
 1193 online documentation at [https://brian2.readthedocs.io/en/stable/introduction/brian1_to_2/
 1194 index.html](https://brian2.readthedocs.io/en/stable/introduction/brian1_to_2/index.html).

1195 **New features**

1196 **Code generation.** The major change from Brian 1 to Brian 2 is that all simulation objects
 1197 are now based around code generation with behaviour determined by user-specified
 1198 strings in standard mathematical notation. From these strings, C++ code is generated,
 1199 compiled and run automatically. Brian 2 can be used in runtime mode (similar to Brian
 1200 1 but with individual objects accelerated using code generation), or standalone mode
 1201 (in which a complete C++ source tree is generated which can be used independently
 1202 of Brian and Python). Third party packages can extend this support to generate code
 1203 for different devices, such as GPUs (e.g. *Stimberg et al. 2018*). New features have
 1204 been added to make it easier to write code that can make use of and extend this
 1205 code generation system, including extending functions by providing their definitions
 1206 in a target language, and the `run_regularly()` method that covers much of what
 1207 was previously done with the (still existing) `@network_operation` but allowing for code
 1208 generation.

1209 **Equations.** Brian always allowed users to write equations and differential equations in
 1210 standard mathematical notation. Stochastic differential equations are now handled
 1211 in a general way. In Brian 1, only additive noise was allowed and integrated with an
 1212 Euler scheme. Brian 2 additionally supports multiplicative noise with the Heun and
 1213 Milstein integration schemes. Numerical integration schemes can be added by the
 1214 user using a general syntax. Variable time step integration using the GNU Scientific
 1215 Library was added. Flags can now be added to equations to modify their behaviour
 1216 (e.g. deactivating specific equations while the neuron is refractory, declaring values to
 1217 be constant over a time step or run to enable optimisations).

1218 **Neurons.** In addition to the new equations features above, the threshold, reset and refrac-
 1219 toriness properties of neurons have now been greatly expanded. In Brian 1, these were
 1220 handled by custom Python classes and could not easily be combined in complex ways.
 1221 In Brian 2, each is defined by a string written in standard mathematical notation, deter-
 1222 mining a condition to evaluate (for threshold or refractoriness) or series of operations
 1223 to be executed (for reset). Whether or not a neuron is refractory is stored in the (user
 1224 accessible) `not_refractory` variable that is used alongside the `unless_refractory` flag
 1225 of the differential equations to switch off dynamics for user selected variables of re-
 1226 fractory neurons. This structure allows for much greater flexibility and can be used
 1227 with code generation.

1228 **Multi-compartmental modelling.** Brian 1 had very basic support for modelling of neurons
 1229 with a small number of compartments. Brian 2 adds support for detailed morphologies
 1230 and specific integration schemes, see Appendix 4.

Synapses. In the first release of Brian, synaptic connectivity was defined by the `Connection`
 class, which only allowed a single weight variable which was added to a target neuron
 variable when a pre-synaptic neuron fired. Later, a more general `Synapses` class was
 added which greatly expanded the flexibility, but was inefficient due to the lack of

comprehensive support for code generation in Brian 1. This `Synapses` class is now the only mechanism in Brian 2, generalises the version from Brian 1 and adds code generation support. `Synapses` allows for a user-specified set of differential equations and parameters (exactly the same as for neurons) along with a specification of what operations should be calculated on the event of a pre- or post-synaptic spike. Multiple pathways with different delays are supported. `Synapses` can modify pre- or post-synaptic neurons in a discrete or continuous manner (to allow for more complex synapse models or rate-based models). `Synapses` can also target other synapses (for models of astrocytes for example, *Stimberg et al. 2019c*). Multiple synapses per neuron pair are now supported. Brian 1's `Connection` supported defining connectivity by an explicit array, or by specifying full, random, or one-to-one connectivity. Brian 2's `Synapses` generalises these with string-based arguments, and adds support for conditional connectivity (a string based expression determining which pairs to connect) and a generator-based syntax that allows you to write code similar to a for loop but that gets converted into efficient low-level code.

Events. In Brian 1, there was only one type of event. A neuron created a spike event if a variable crossed a threshold, and this spike event triggered a reset on the source neuron, as well as synaptic activity. In Brian 2, these events remain but the user can also specify arbitrary events and triggered operations.

Monitors. Brian 1 had a large collection of monitors to record different types of activity. These have been replaced by just three generalised versions that record discrete, continuous or population activity.

Store/restore. Brian 2 has a new `store()` and `restore()` mechanism that saves and loads the entire simulation state.

String-based indexing and evaluation. Brian 2 allows variables to be indexed by strings as well as numerical indices. For example, writing `G.z['x>0'] = 'sin(y)'` would set the value of variable `z` to `sin(y)` (where `y` can be a single value or neuron variable), but only for those neurons where the variable `x > 0`.

Units. In Brian 1, only scalar values could have physical dimensions. Now arrays can also have units. In addition, consistency of dimensions is now used everywhere.

Safety. A number of changes were made to minimise the chance that the user would write code that behaved differently from what was expected. This includes raising an error or warning whenever there is any ambiguity.

Python 3. Brian 1 was written only for Python 2. Brian 2 is available for Python 2 and 3.

Continuous integration. Brian 2 has a large test suite that is automatically run on multiple versions of Python, operating systems (Linux, Mac, Windows), and architectures (32/64 bit). Installation has been improved to make it easier to install, and to ensure that C++ compiler tools are installed to make sure that the most high performance generated code can be used.

Removed or replaced features

Packages. The aim of Brian 2 was to have a simpler, more flexible core package, and allow separate packages to provide extra functionality. The `brian.tools` package which provided some general purpose tools was therefore removed. The `brian.hears` package has been updated to `brian2hears` provided separately. An updated and generalised version of the `brian.modelfitting` (*Rossant et al., 2010*) package is in progress.

Library. Brian 1 featured a “library” of models that could be used instead of writing equations explicitly. In line with the design philosophy of Brian 2 described in this paper, this feature was removed. All the equations are listed in the documentation and so

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Brian 1 models using these features can easily be updated.

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STDP. Brian 1 had specific classes for STDP models. These are now obsolete as the `Synapses` class in Brian 2 covers everything they could do and more. Examples are given in the documentation of how to update code.

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Connection class. The `Connection` class of Brian 1 has been removed in favour of the new `Synapses` class (see above).

1289


```

1  from brian2 import *
2
3  defaultclock.dt = 0.01*ms
4  E_L = -68*mV; E_Na = 20*mV; E_K = -80*mV; E_Ca = 120*mV; E_proc = -10*mV
5  C_s = 0.2*nF; C_a = 0.02*nF; g_E = 10*nS; g_La = 7.5*nS; g_Na = 300*nS;
6  g_Kd = 4*uS; G_Ca = 0.2*uS; G_K = 16*uS; tau_h_Ca = 150*ms; tau_m_A = 0.1*ms;
7  tau_h_A = 50*ms; tau_m_proc = 6*ms; tau_m_Na = 0.025*ms; tau_z = 5*second
8
9  eqs = '''# somatic compartment
10 dV_s/dt = (-I_syn - I_L - I_Ca - I_K - I_A - I_proc - g_E*(V_s - V_a))/C_s : volt
11 I_L = g_Ls*(V_s - E_L) : amp
12 I_K = g_K*m_K**4*(V_s - E_K) : amp
13 I_A = g_A*m_A**3*h_A*(V_s - E_K) : amp
14 I_proc = g_proc*m_proc*(V_s - E_proc) : amp
15 I_syn = I_fast + I_slow : amp
16 I_fast : amp
17 I_slow : amp
18 I_Ca = g_Ca*m_Ca**3*h_Ca*(V_s - E_Ca) : amp
19 dm_Ca/dt = (m_Ca_inf - m_Ca)/tau_m_Ca : 1
20 m_Ca_inf = 1/(1 + exp(0.205/mV*(-61.2*mV - V_s))): 1
21 tau_m_Ca = 30*ms - 5*ms/(1 + exp(0.2/mV*(-65*mV - V_s))) : second
22 dh_Ca/dt = (h_Ca_inf - h_Ca)/tau_h_Ca : 1
23 h_Ca_inf = 1/(1 + exp(-0.15/mV*(-75*mV - V_s))) : 1
24 dm_K/dt = (m_K_inf - m_K)/tau_m_K : 1
25 m_K_inf = 1/(1 + exp(0.1/mV*(-35*mV - V_s))) : 1
26 tau_m_K = 2*ms + 55*ms/(1 + exp(-0.125/mV*(-54*mV - V_s))) : second
27 dm_A/dt = (m_A_inf - m_A)/tau_m_A : 1
28 m_A_inf = 1/(1 + exp(0.2/mV*(-60*mV - V_s))) : 1
29 dh_A/dt = (h_A_inf - h_A)/tau_h_A : 1
30 h_A_inf = 1/(1 + exp(-0.18/mV*(-68*mV - V_s))) : 1
31 dm_proc/dt = (m_proc_inf - m_proc)/tau_m_proc : 1
32 m_proc_inf = 1/(1 + exp(0.2/mV*(-55*mV - V_s))) : 1
33 # axonal compartment
34 dV_a/dt = (-g_La*(V_a - E_L) - g_Na*m_Na**3*h_Na*(V_a - E_Na)
35           -g_Kd*m_Kd**4*(V_a - E_K) - g_E*(V_a - V_s))/C_a : volt
36 dm_Na/dt = (m_Na_inf - m_Na)/tau_m_Na : 1
1290 37 m_Na_inf = 1/(1 + exp(0.1/mV*(-42.5*mV - V_a))) : 1
38 dh_Na/dt = (h_Na_inf - h_Na)/tau_h_Na : 1
39 h_Na_inf = 1/(1 + exp(-0.13/mV*(-50*mV - V_a))) : 1
40 tau_h_Na = 10*ms/(1 + exp(0.12/mV*(-77*mV - V_a))) : second
41 dm_Kd/dt = (m_Kd_inf - m_Kd)/tau_m_Kd : 1
42 m_Kd_inf = 1/(1 + exp(0.2/mV*(-41*mV - V_a))) : 1
43 tau_m_Kd = 12.2*ms + 10.5*ms/(1 + exp(-0.05/mV*(58*mV - V_a))) : second
44 # class-specific fixed maximal conductances
45 g_Ls : siemens (constant)
46 g_A : siemens (constant)
47 g_proc : siemens (constant)
48 # Adaptive conductances
49 g_Ca = G_Ca/2*(1 + tanh(z)) : siemens
50 g_K = G_K/2*(1 - tanh(z)) : siemens
51 I_diff = (I_target + I_Ca) : amp
52 dz/dt = tanh(I_diff/nA)/tau_z : 1
53 I_target : amp (constant)
54 # Neuron class
55 label : integer (constant)'''
56 circuit = NeuronGroup(3, eqs, method='rk2',
57                       threshold='m_Na > 0.5', refractory='m_Na > 0.5')
58 ABPD, LP, PY = 0, 1, 2
59 # class-specific constants
60 circuit.label = [ABPD, LP, PY]
61 circuit.I_target = [0.4, 0.3, 0.5]*nA; circuit.g_Ls = [30, 25, 15]*nS
62 circuit.g_A = [450, 100, 250]*nS; circuit.g_proc = [6, 8, 0]*nS
63 # Initial conditions
64 circuit.V_s = E_L; circuit.V_a = E_L
65 circuit.m_Ca = 'm_Ca_inf'; circuit.h_Ca = 'h_Ca_inf'; circuit.m_K = 'm_K_inf';
66 circuit.m_A = 'm_A_inf'; circuit.h_A = 'h_A_inf'; circuit.m_proc = 'm_proc_inf'
67 circuit.m_Na = 'm_Na_inf'; circuit.h_Na = 'h_Na_inf'; circuit.m_Kd = 'm_Kd_inf'

```

Figure 2-Figure supplement 1. Simulation code for the more biologically detailed model of the circuit shown in Figure 1a (based on *Golowasch et al., 1999*). The code for the synaptic model and connections is identical to the code shown in Figure 2, except for acting on V_s instead of v in the target cell.