Calcium-driven regulation of voltage-sensing domains in BK channels

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Abstract

Allosteric interactions between the voltage-sensing domain (VSD), the Ca\(^{2+}\)-binding sites, and the pore domain govern the mammalian Ca\(^{2+}\)- and voltage-activated K\(^{+}\) (BK) channel opening. However, the functional relevance of the crosstalk between the Ca\(^{2+}\)- and voltage-sensing mechanisms on BK channel gating is still debated. We examined the energetic interaction between Ca\(^{2+}\) binding and VSD activation by investigating the effects of internal Ca\(^{2+}\) on BK channel gating currents. Our results indicate that Ca\(^{2+}\) sensor occupancy has a strong impact on VSD activation through a coordinated interaction mechanism in which Ca\(^{2+}\) binding to a single α-subunit affects all VSDs equally. Moreover, the two distinct high-affinity Ca\(^{2+}\)-binding sites contained in the C-terminus domains, RCK1 and RCK2, contribute equally to decrease the free energy necessary to activate the VSD. We conclude that voltage-dependent gating and pore opening in BK channels is modulated to a great extent by the interaction between Ca\(^{2+}\) sensors and VSDs.
Introduction

Diverse cellular events involve calcium ions as a primary mediator in the signal transduction pathways triggering, among other signaling processes, Ca$^{2+}$-activated conductances. Since the BK channels are regulated by cytosolic Ca$^{2+}$ and depolarizing voltages (Marty, 1981; Pallotta et al., 1981; Latorre et al., 1982), they are integrators of physiological stimuli involving intracellular Ca$^{2+}$ elevation and membrane excitability. BK channels are modular proteins in which each module accomplishes a specific function. Thus, different modules harbor voltage and Ca$^{2+}$ sensors that communicate allosterically with the channel gate (Cox et al., 1997; Horrigan and Aldrich, 1999, 2002; Horrigan et al., 1999; Rothberg and Magleby, 1999, 2000; Cui and Aldrich, 2000). Functional BK channels are formed by homotetramers of α-subunits (Shen et al., 1994), each comprising a transmembrane voltage-sensing domain (VSD) and an intracellular Ca$^{2+}$-sensing C-terminal domain (CTD) that can independently modulate the ion conduction gate in the pore domain (PD) (Latorre et al., 2017). The CTDs consist of two non-identical regulators of the conductance of K$^+$ domains (RCK1 and RCK2) arranged in a ring-like tetrameric structure dubbed the gating ring (Wu et al., 2010; Yuan et al., 2010, 2012; Hite et al., 2017; Tao et al., 2017). Each RCK domain contains distinct ligand-binding sites capable of detecting Ca$^{2+}$ in the micromolar range (Schreiber and Salkoff, 1997; Bao et al., 2002; Xia et al., 2002).

In the absence of Ca$^{2+}$, the activation of the VSD decreases the free energy necessary to fully open the BK channels in an allosteric fashion (Horrigan and Aldrich, 1999; Horrigan et al., 1999). With 0 Ca$^{2+}$, very positive membrane potentials are required to drive all voltage sensors to their active conformations (Cui et al., 1997; Stefani et al., 1997; Horrigan et al., 1999; Contreras et al., 2012), ultimately leading to near-maximal BK activation. Thus, in cells such as neurons, an appreciable open probability of BK channels...
at physiologically relevant voltages necessarily requires the activation of the Ca\textsuperscript{2+} sensors on the gating ring. The allosteric interplays established between the functional and structural modules (VSD-PD, CTD-PD, and CTD-VSD) are key for enabling BK channels to operate over a wide dynamic range of internal Ca\textsuperscript{2+} and voltage, thereby fine-tuning the channel’s gating machinery. Therefore, understanding the structure-functional bases that underlie the Ca\textsuperscript{2+} and voltage activation mechanisms interrelationship becomes essential to unveil how the channel behaves under different physiological conditions.

The voltage dependence of Ca\textsuperscript{2+}-dependent gating ring rearrangements (Miranda et al., 2013, 2018) and RCK1 site occupancy (Sweet and Cox, 2008; Savalli et al., 2012; Miranda et al., 2018) as well as the perturbation of VSD movements by Ca\textsuperscript{2+} binding (Savalli et al., 2012) support the idea that the energetic interaction between both specialized sensors may be crucial for BK channel activation. The physical CTD-VSD interface has been suggested to provide the structure capable of mediating the crosstalk between these sensory modules and their synergy in activating the pore domain (Yang et al., 2007; Sun et al., 2013; Tao et al., 2017; Zhang et al., 2017). However, the strength of the interaction between voltage and Ca\textsuperscript{2+} sensors and their relevance to BK channel activation is still debated (cf. Horrigan and Aldrich, 2002; Carrasquel-Ursulaez et al., 2015). Also, the functional role that each of the high-affinity Ca\textsuperscript{2+}-binding sites plays in the CTD-VSD allosteric interaction is an open question. The RCK1 and RCK2 Ca\textsuperscript{2+}-binding sites have distinct functional properties conferred by their different molecular structures and relative positions within the gating ring (Wu et al., 2010; Yuan et al., 2010, 2012; Hite et al., 2017; Tao et al., 2017). Thus, the RCK sites differ in their Ca\textsuperscript{2+} binding affinities (Bao et al., 2002; Xia et al., 2002; Sweet and Cox, 2008), divalent cations selectivity (Oberhauser et al., 1988; Schreiber and Salkoff, 1997; Zeng et al., 2005; Zhou et al., 2012), voltage dependence (Sweet and Cox, 2008; Savalli et al., 2012; Miranda et al., 2018) and in their...
contribution to allosteric gating mechanisms (Yang et al., 2010, 2015). In particular, only
the RCK1 site appears to be involved in communicating the Ca\textsuperscript{2+}-dependent
conformational changes towards the membrane-spanning VSD (Savalli et al., 2012;
Miranda et al., 2018). Recently, the Aplysia BK structure has revealed that the N-lobe of
the RCK1 domain is in a non-covalent contact with the VSD and the S4-S5 linker that
connects the voltage sensor to the pore domain. This RCK1-VSD interaction surface is
rearranged when comparing the liganded and Ca\textsuperscript{2+}-free structures (Hite et al., 2017; Tao
et al., 2017). In fact, it has been hypothesized that any Ca\textsuperscript{2+}-induced rearrangements of
the gating ring should ultimately be transmitted to the pore domain via the VSD (Hite et
al., 2017; Zhou et al., 2017). Thereby, defining the extent to which Ca\textsuperscript{2+} binding influences
to VSD is central for determining the importance of the crosstalk between sensors in
decreasing the free energy necessary to open the BK channel.

Here, we examined the Ca\textsuperscript{2+}-dependence of the VSD activation by estimating the allosteric
coupling between the Ca\textsuperscript{2+} and voltage sensors. By analyzing gating currents under
unliganded and Ca\textsuperscript{2+}-saturated conditions, we found a strong energetic influence of Ca\textsuperscript{2+}-
binding on voltage sensor equilibrium in a manner that is independent of channel opening.
These findings show that a major component in the synergistic Ca\textsuperscript{2+} and voltage activation
of BK channels resides in the strong coupling between Ca\textsuperscript{2+} binding and the voltage
sensor activation. We also found that the Ca\textsuperscript{2+}-dependence of voltage sensor activation is
consistent with a CTD-VSD allosteric coupling that occurs through a concerted interaction
scheme in which each Ca\textsuperscript{2+} bound to one subunit affects all voltage sensors in the BK
tetramer equally. Notably, we found that the two distinct RCK1 and RCK2 Ca\textsuperscript{2+} sensors
contribute equally to the VSD activation via independent allosteric pathways.
Results

Allosteric coupling between Ca\(^{2+}\)-binding and voltage sensor activation is strong.

We characterized the effects of Ca\(^{2+}\)-binding on voltage sensor activation in BK channels by analyzing the gating currents measured in inside-out patches of *Xenopus laevis* oocyte membrane. The amount of gating charge displaced \((Q_C)\) at each Ca\(^{2+}\) concentration was obtained by integrating the initial part of the decay of the ON-gating current \((I_G-\text{ON})\), which was fitted to a single exponential (fast ON-gating; see Methods). As we show below, we determined only the gating charge displaced before the opening of the BK channel. Figure 1A-B show representative \(I_G\)-ON records in response to 160 mV voltage step in the nominal absence of Ca\(^{2+}\) ("zero" Ca\(^{2+}\)) and in saturating Ca\(^{2+}\) concentration (100 µM Ca\(^{2+}\)). In Figures 1A-B, we also show the initial time courses of the corresponding macroscopic K\(^+\) current \((I_K)\) activation at the same voltage and internal Ca\(^{2+}\) conditions. The \(I_G\)-ON relaxation exhibits an almost complete decay before the \(I_K\) achieves an exponential time course in 0 Ca\(^{2+}\) conditions (Figure 1A). Thus, the time constant of the \(I_K\) activation (~3.4 ms at 160 mV) following a delay of ~160 µs is consistent with the movement of the voltage sensors preceding channel opening. Under saturating internal Ca\(^{2+}\) conditions, the \(I_G\)-ON time course develops 20 times faster than the exponential kinetic of the \(I_K\) activation \((\tau_{I_G-\text{ON}} = 30 \mu s \text{ and } \tau_{I_K} = 660 \mu s \text{ at 160 mV})\) and is also almost complete within the time interval comprised by the \(I_K\) delay \((\Delta t_{I_K} (100 \mu M) = 84 \mu s)\) (Figure 1B). Thus, the fast \(I_G\)-ON relaxation reflects the movement of the gating charge in the channel’s closed conformation, regardless of internal Ca\(^{2+}\) concentration.

The \(Q_C\) was determined over a wide range of membrane potentials at low and high internal (100 µM) Ca\(^{2+}\) concentration. Increasing the Ca\(^{2+}\) concentration promoted a large leftward shift \((\Delta V_H = -142.6 \pm 4.5 \text{ mV})\) of the normalized \(Q_C\) \((Q_C(V)/Q_{C,MAX\text{ curves}}))\) (Figure 1C). In
spite of with the large leftward shift of the $Q_C$ at high $\text{Ca}^{2+}$ concentrations, we found no appreciable slow component in $I_G$-ON (cf. Horrigan and Aldrich, 2002; see also **Figure 2—figure supplement 1A**). As expected, a large $\text{Ca}^{2+}$-dependent leftward shift was also observed in the time constants of the exponential decays of $I_G$-ON ($\tau_{I_{G-ON}}(V)$) curves were fitted to a two state model ($\tau(V) = 1/(\alpha(V) + \beta(V))$ where the forward ($\alpha$) and backward ($\beta$) rate constants represent the resting-active (R-A) transitions of the voltage sensors, that determine the equilibrium constant of the VSD activation ($J(V) = \alpha(V)/\beta(V)$). The predominant effect of $\text{Ca}^{2+}$-binding on VSD activation appears to cause a decrease in the backward rate constant at zero voltage ($\beta_0$; see **Methods**). $\beta_0$ decreases from 76 ms$^{-1}$ at 0 $\text{Ca}^{2+}$ to 7 ms$^{-1}$ at 100 $\mu$M $\text{Ca}^{2+}$, which results in a shift in the equilibrium of the voltage sensors towards their active conformation. Such a large shift ($\Delta V_H = -142.6 \pm 4.5$ mV) implies that $\text{Ca}^{2+}$ binding to the RCK $\text{Ca}^{2+}$-binding sites alters the VSD equilibrium, which in consequence causes a decrease in the free energy ($\Delta \Delta G_{V_C}^{\text{Ca}}$) that defines the voltage sensor R-A equilibrium ($J$) by $\sim$8 kJ/mol ($\Delta \Delta G_{V_C}^{\text{Ca}} = -7.98 \pm 0.27$ kJ/mol). In terms of the allostERIC gating scheme (Horrigan and Aldrich, 2002), this result means that the $J$ equilibrium constant of VSD becomes amplified by an allostERIC factor $E$ equal to 26.4 at $\text{Ca}^{2+}$-saturated conditions (**Figure 1D**), revealing a strong allostERIC coupling between $\text{Ca}^{2+}$-binding sites and voltage sensors.

Families of gating currents ($I_G$) were evoked at different intracellular $\text{Ca}^{2+}$ concentrations ([Ca$^{2+}$]) ranging from 0.1 to 100 $\mu$M in K$^+$-free solution (**Figure 2A**). For all experiments, we first measured $I_G$ in “zero” $\text{Ca}^{2+}$ condition and then perfused the internal side with solutions containing different concentrations of $\text{Ca}^{2+}$. The increase in internal $\text{Ca}^{2+}$ promoted a leftward shift of the $Q_C$ versus voltage ($Q_C(V)$) curves (**Figure 2B-C**), which indicates that $\text{Ca}^{2+}$-binding facilitates the activation of the voltage sensor, being more prominent as $\text{Ca}^{2+}$-binding site occupancy increases.
Figure 2A shows that the OFF-gating current was dramatically modified becoming smaller in amplitude and with slower kinetics as the internal Ca\textsuperscript{2+} concentration was increased (see also Figure 2—figure supplement 1A and Figure 2—figure supplement 2A). At least two components (fast and slow components) could be resolved in the OFF gating current decay in "zero" and 10 µM internal Ca\textsuperscript{2+} conditions (Figure 2—figure supplement 1B-C). In Figure 2—figure supplement 1D, we fitted \( \tau_{I_{g-ON}}(V) \) data for 0 and 10 µM internal Ca\textsuperscript{2+} to a two-state R-A model. Figure 2—figure supplement 1D shows that the time constants of the fast relaxation of the \( I_{g-OFF} \) evoked at -90 mV (open and closed orange circles) are in reasonable agreement with the time constants values extrapolated to the same voltage from the two-state model of the \( I_{g-ON} \) kinetic. The change in the time constant of the fast component of OFF-gating current detected at 10 µM Ca\textsuperscript{2+} relative to "zero" Ca\textsuperscript{2+} condition agrees with a Ca\textsuperscript{2+}-induced effect primarily on the backward rate of the R-A transition (\( \beta_0 \) decreases from 76 ms\textsuperscript{-1} at 0 Ca\textsuperscript{2+} to 10.6 ms\textsuperscript{-1} at 10 µM Ca\textsuperscript{2+}, see Figure 2—figure supplement 1D), which is consistent with the large \( Q_C(V) \) shift observed (\( \Delta V_H(10 \mu\text{M}) = -107.1 \pm 17.1 \text{ mV} \)). On the other hand, the relative contribution of the slower component increasing as internal Ca\textsuperscript{2+} is increased, reflecting an increase in the open probability of the channel (Figure 2—figure supplement 1E-F). This kinetic behavior recapitulates the effect described on gating charge displacement as a function of the depolarizing pulse duration (Horrigan and Aldrich, 2002; Contreras et al., 2012; Carrasquel-Ursulaelz et al., 2015), and confirms that this phenomenon is associated with the time course of channel opening revealing the allosteric interaction between voltage sensors and the pore gate (Horrigan and Aldrich, 2002).

Since the OFF gating charge cannot be accurately estimated from the OFF gating current recorded at -90 mV, we performed two experiments using 100 µM internal Ca\textsuperscript{2+} concentration and recorded the OFF gating currents at -150 mV and -200 mV (Figure 2—...
figure supplement 2A). At these applied voltages, the charge displaced in the ON is recovered in the OFF (Figure 2—figure supplement 2B). As expected from the large shift to the left along the voltage axis of \( Q_C \) at saturating internal Ca\(^{2+} \) concentrations, there was no difference between the \( Q_C \) curve and the gating charge-voltage curves obtained from the OFF gating currents 2 ms after the onset of the voltage pulse, for applied voltages of -150 or -200 mV (Figure 2—figure supplement 2C).

Ca\(^{2+} \) binding to a single \( \alpha \)-subunit affects the R-A voltage sensor equilibrium of all four subunits equally. Taking advantage of the dose-dependent effect of Ca\(^{2+} \) on voltage sensor activation we investigated the underlying mechanism of the communication between the Ca\(^{2+} \) binding and voltage sensors in the context of the well-established Horrigan-Aldrich (HA) allosteric gating model (Horrigan and Aldrich, 2002). Two different mechanisms were proposed by Horrigan and Aldrich for the interaction between the Ca\(^{2+} \)-binding sites and voltage sensors. The first mechanism proposes that Ca\(^{2+} \) binding to one \( \alpha \)-subunit only affects the VSD in the same subunit (Scheme I) (Figure 3A), whereas the second mechanism proposes that the Ca\(^{2+} \) binding affects all four VSD equally (Scheme II) (Figure 3B). It should be noted that the standard HA model makes two simplifying assumptions. First, the model considers that there is a single Ca\(^{2+} \)-binding site per \( \alpha \)-subunit. Second, the model assumes the Scheme I as the Ca\(^{2+} \) binding-VSD interaction scheme underlying the general gating mechanism of BK channel (Horrigan and Aldrich, 2002).

We simulated the normalized \( Q_C(V) \) curves over a wide range of Ca\(^{2+} \) concentrations (from 0 to 10 mM) for each Ca\(^{2+} \)-VSD interaction scheme (Figure 3C-D). We assumed that the fast gating currents measured correspond to the charge displaced by the R-A transitions and does not include the charge associated with the transition between the activated states (see Figure 3—figure supplement 1B-C). In other words, Equations 4 and 6 given
in the Appendix describing the $Q_C(V)$ relationships for Schemes I and II are based on the assumption that channels equilibrate between Ca$^{2+}$-bound states while the channel is closed and voltage sensors are not activated. We further assume that this distribution is not altered when gating current is measured because Ca$^{2+}$ binding is slower than voltage-sensor activation. These assumptions are reasonable since the Ca$^{2+}$-binding rate constant estimated for BK is $1.8 \times 10^8$ M$^{-1}$s$^{-1}$ (Hou et al., 2016) implying that at 10 μM internal Ca$^{2+}$ (the highest non-saturating Ca$^{2+}$ concentration tested) the time constant of the Ca$^{2+}$ binding is ~300 μs, while the VSD activates with a time constant of ~60 μs at $V = V_H$ (see the Appendix for details of the simulations).

At extreme conditions of low (0.03 to 0.1 μM) and high (≥100 μM) internal Ca$^{2+}$, VSD activation behaves in a mechanism-independent manner since all voltage sensors are in the same functional state (unliganded or saturated). However, the distinctive effects on $Q_C(V)$ curves at intermediate Ca$^{2+}$ concentrations (1-10 μM) provide useful signatures to distinguish between the two mechanisms. Indeed, Scheme I predicts two functional states of the VSD depending on the occupancy status of the Ca$^{2+}$ site (Ca$^{2+}$ bound and unbound) such that the $Q_C(V)$ curve is described by the fractional distribution of the unliganded and Ca$^{2+}$-saturated functional states like an all-or-none allostERIC effect (Figure 3C; Figure 3—figure supplement 1B and Equation 4 in Appendix). By contrast, the Ca$^{2+}$-binding effect on the VSD activation according to Scheme II is characterized by a five-component Boltzmann function (Figure 3—figure supplement 1C and Equation 6 in Appendix). Each component represents a single functional state determined by the number of Ca$^{2+}$ bound to the channel (from 0 to 4). In such a case, the $Q_C(V)$ curves resulting from a distribution of functional states are equivalent to a single Boltzmann function, leftward shifted by an incremental allostERIC effect (from $E$ to $E^4$) as the number of Ca$^{2+}$ bound to the channel increases (Figure 3D). The experimental leftward shift of the $Q_C(V)$ curves occur with
constant slope \((z_Q)\) (Figure 2B), which is consistent with Model II. It can be argued that Scheme I can produce single Boltzmann curves without a change in \(z_Q\) if \(\text{Ca}^{2+}\) re-equilibration is fast enough. However, Figure 3-figure supplement 2 demonstrates that to recover the experimental \(z_Q\) requires a \(\text{Ca}^{2+}\) binding rate constant that is 100-fold faster than the one reported by Hou et al. (2016) exceeding the diffusion limit constraint. Therefore, we can conclude that \(\text{Ca}^{2+}\)-binding is slow enough to safely ignore calcium re-equilibration during the 100 \(\mu\)s it takes to measure the gating charges.

To further elucidate the mechanism by which \(\text{Ca}^{2+}\) and voltage sensors interact, we performed fits of the \(Q_C(V)\) data using the two different models represented by Scheme I and Scheme II (Figure 4A-B). The allosteric factor \(E\) that accounts for the coupling between the \(\text{Ca}^{2+}\)-binding sites and the voltage sensors was constrained to values calculated from the experimental data for the \(Q_C(V)\) shift at \(\text{Ca}^{2+}\) saturating conditions (100 \(\mu\)M) in relation to the same curve in the absence of \(\text{Ca}^{2+}\). The \(z_f, J_0\) and \(K_D\) parameters obtained during the fitting procedure were very similar for each model (Table 1). The fitted values for the affinity constant \((K_D = 6 \ \mu\text{M})\) agree with previous reports (Cox et al., 1997; Horrigan and Aldrich, 2002) although they are slightly smaller than those estimated for the closed conformation of the channel \((K_D = 11 \ \mu\text{M})\). Based on the Akaike Information Criterion (AIC) (Akaike, 1974), the model that fits to the \(Q_C(V,[\text{Ca}^{2+}])\) data best is Model II, whereas the probability of the Model I being the best model is negligible \((w_i = 10^{-47})\) (Table 1). Both models generates a \(V_H\text{-log}[\text{Ca}^{2+}]\) curve that accounts reasonably well for the dose-response experimental data (Figure 4C). However, Model I predicts a pronounced decrease in the \(z_Q\) parameter of the \(Q_C(V)\) curves at intermediate \(\text{Ca}^{2+}\) conditions which differs markedly from the experimental values (Figure 4D). This prediction is a consequence of the fractional distribution of two very distinctive functional states of the voltage sensors (unliganded and \(\text{Ca}^{2+}\)-saturated, see above). Additionally, the
behavior of $Q_C(V)$ curves at intermediate Ca$^{2+}$ concentrations (1-10 µM) is qualitatively consistent with the phenotype exhibited by the Ca$^{2+}$-VSD scheme II (Figure 3D and Figure 4B). Thus, the experimental dose-dependent effect of Ca$^{2+}$ on voltage sensor activation suggests that Ca$^{2+}$-binding to a single α-subunit of BK channels increases $E$-fold the equilibrium constant $J$ that defines the equilibrium between resting and active conformations of the voltage sensors in all four subunits.

High-affinity Ca$^{2+}$-binding sites in RCK1 and RCK2 domains contribute equally to the allosteric coupling between Ca$^{2+}$ and voltage sensors. Under physiological conditions, the RCK1 and RCK2 high-affinity Ca$^{2+}$-binding sites are responsible for all the calcium sensitivity of the activation of BK channel (Schreiber and Salkoff, 1997; Bao et al., 2002, 2004; Xia et al., 2002). However, distinct physiological roles of the RCK1 Ca$^{2+}$-sensor and Ca$^{2+}$ bowl may be based on their functionally and structurally distinctive properties (Zeng et al., 2005; Sweet and Cox, 2008; Yang et al., 2010; Savalli et al., 2012; Tao et al., 2017). We next asked what the energetic contribution to VSD equilibrium was of the two high-affinity Ca$^{2+}$-binding sites contained in the RCK1 and RCK2 domains.

To elucidate the effect of each Ca$^{2+}$-sensor on the VSD activation we used mutations that selectively and separately abolish the function of the two different RCK Ca$^{2+}$-sites. Disruption of the RCK1 Ca$^{2+}$-sensor by the double mutant D362A/D367A (Xia et al., 2002) significantly reduced (48%, $\Delta V_H^{(D362A/D367A)} = -74.9 \pm 4.7$ mV) the leftward shift of the $Q_C(V)$ curves at 100 µM Ca$^{2+}$ compared with that for the wild-type (WT) BK channel (Figure 5A,C). We also examined the effect of the mutant M513I (Bao et al., 2002) which has been shown to eliminate the Ca$^{2+}$ sensitivity mediated by the RCK1 site (Bao et al., 2002, 2004; Zhang et al., 2010). In this mutant, the 100 µM Ca$^{2+}$-induced shift in $V_H$ of the VSD activation curve was also considerably smaller compared to that for the WT channel (about 54%, $\Delta V_H^{(M513I)} = -65.4 \pm 2.6$ mV) (Figure 6). Therefore, both mutations affect the Ca$^{2+}$-
induced enhancement of the activation of the voltage sensor very similarly through the
RCK1 site (Figure 6C), although their mechanisms of action could be quite different. The
M513 residue appears to participate in the stabilization of the proper conformation of the
RCK1 Ca\(^{2+}\)-site whereas D367 is a key residue in the coordination of Ca\(^{2+}\) ions (Wu et al.,
2010; Zhang et al., 2010; Tao et al., 2017). On the other hand, neutralization of the
residues forming part of the Ca\(^{2+}\) bowl (Schreiber and Salkoff, 1997) (5D5A mutant, see
Methods) on the RCK2 domain decreased the leftward shift of the \(Q_C(V)\) curve by
approximately 54\% (\(\Delta V_H\) (5D5A) = -65.7 ± 4.7 mV) when Ca\(^{2+}\) was increased up to 100 μM
(Figure 5B,D). The effect of Ca\(^{2+}\) binding on \(\Delta V_H\) contributed by each high-affinity Ca\(^{2+}\)
site is roughly half that for WT channels with both sites intact (Figure 5E). Therefore, both
high-affinity Ca\(^{2+}\)-binding sites contribute approximately equally to the decrease in free
energy that is necessary to activate the VSD. Indeed, the change of free energy of the
resting-active equilibrium of the voltage sensor in response to Ca\(^{2+}\)-binding at RCK2 site
is ~ -4 kJ/mol (\(\Delta\Delta G^{Ca}_V\) (D362A/D367A) = -4.2 ± 0.3 kJ/mol and \(\Delta\Delta G^{Ca}_V\) (M513I) = -3.6 ± 0.5 kJ/mol)
(Figure 5C and Figure 6C). Similarly, the occupation of the RCK1 Ca\(^{2+}\)-binding site
decreased the free energy necessary to activate the VSD in -3.8 ± 0.4 kJ/mol (\(\Delta\Delta G^{Ca}_V\) (5D5A)).
Remarkably, these findings reveal an additive effect of Ca\(^{2+}\)-binding to the RCK1 and Ca\(^{2+}\)
bowl sites on the VSD activation, which suggest independent allosteric pathways through
which they exert their modulation on the VSD.

Taking these results into account, we expanded the Ca\(^{2+}\)-VSD interaction models
considering the energetic contribution of the two kinds of Ca\(^{2+}\) sensors on the VSD per α-
subunit (\(E_{WT} = E_{S1} \ast E_{S2}\) (Figure 3—figure supplement 1D). As described in the above
model fittings, the allosteric factors \(E\) for each one RCK1 and RCK2 sites (\(E_{S1}\) and \(E_{S2}\))
were constrained to values equivalent to the Ca\(^{2+}\)-induced energetic perturbations of the
voltage sensor equilibrium for the 5D5A and D362A/D367A mutants, respectively. The
inclusion of two Ca\[^{2+}\] sites per subunit in the Ca\[^{2+}\]-VSD interaction schemes increases the functional states of the VSD for both models (Figure 3—figure supplement 1E). Therefore, it becomes difficult to discriminate between different models based on the phenotype of the $Q_C(V)$ curves at intermediate Ca\[^{2+}\] concentrations (Figure 4—figure supplement 1A-B). However, according to the AIC criteria (compare AICs for the models in Table 1), Model II - Two Ca\[^{2+}\] sites is the model that best describes the $Q_C(V, [Ca^{2+}])$ data ($w_i = 0.99$). As mentioned when describing the one Ca\[^{2+}\] site models, the goodness of the different models can be better appreciated by the Ca\[^{2+}\]-dependence of the $z_Q$ parameter (Figure 4—figure supplement 1C-D). The fractional distribution of the distinct functional states of the VSDs defined by Model I - Two Ca\[^{2+}\] sites (unliganded, RCK1 site occupied, RCK2 site occupied, and the two sites occupied; see Figure 3—figure supplement 1E) produce a $z_Q \log[Ca^{2+}]$ curve with a pronounced minimum when the Ca\[^{2+}\] concentration is close to the $K_D$ value (Figure 4—figure supplement 1C). Thus, Model I - Two Ca\[^{2+}\] sites predicts a prominent Ca\[^{2+}\]-dependence of the $z_Q$ whereas as we found experimentally, the $z_Q$ predicted by Model II is essentially independent of the Ca\[^{2+}\] concentration. The slight apparent increase in $z_Q$ data observed in Figure 4—figure supplement 1C as the Ca\[^{2+}\] concentration is increased is not statistically significant.

We note here that when the intrasubunit cooperativity factor ($G$) is allowed to vary freely, Model II produces estimates of the $K_D$ parameters that are out the range relative to the apparent Ca\[^{2+}\] affinities previously reported in the literature for the Ca\[^{2+}\]-binding sites ($K_{D\text{(RCK1)}} = 13 - 24 \ \mu M$ and $K_{D\text{(RCK2)}} = 3 - 5 \ \mu M$) (Bao et al., 2002; Xia et al., 2002; Sweet and Cox, 2008). In addition, Model II reaches better estimates of the $K_D$ parameters (Table 1) if we consider non cooperative interactions between the Ca\[^{2+}\]-binding sites. However, although the $K_D$ value for the RCK2 Ca\[^{2+}\]-binding site is in agreement with previous reports, Model II underestimates the value for $K_{D\text{(RCK1)}}$. 
Recent functional and structural studies have revealed the existence of a major interplay between voltage- and Ca\(^{2+}\)-sensing modules in the BK channel (Yuan et al., 2010; Savalli et al., 2012; Miranda et al., 2013, 2016, 2018; Carrasquel-Ursulaez et al., 2015; Hite et al., 2017; Tao et al., 2017; Zhang et al., 2017), which offer a new perspective on our understanding of its multimodal gating mechanism. However, the details of the CTD-VSD allosteric coupling as well its molecular nature have yet to be firmly established since their direct assessment is experimentally challenging. Based on the functional independence of the distinct structural domains involved (PD, CTD, and VSD), the energetic relationship between the sensory modules can be directly defined by comparing the change in the equilibrium of the voltage sensor under two extreme Ca\(^{2+}\) conditions: unliganded and saturated (Horrigan and Aldrich, 2002).

Thus, by characterizing the voltage dependence of charge movement in the virtual absence of internal Ca\(^{2+}\) and at Ca\(^{2+}\) concentrations that saturate the Ca\(^{2+}\) high-affinity sites, this work directly establishes that Ca\(^{2+}\)-binding significantly facilitates VSD activation through direct energetic contribution to the R-A equilibrium (\(\Delta V_H = -142.6 \pm 4.5\) mV and \(\Delta \Delta G_V^{Ca} = -7.98 \pm 0.27\) kJ/mol). Although this result is in agreement with previous reports from our laboratory (\(\Delta V_H = -140\) mV and \(\Delta \Delta G_V^{Ca} = -7.9\) kJ/mol; at [Ca\(^{2+}\)] = 100 µM) (Carrasquel-Ursulaez et al., 2015), it is at odds with the smaller leftward shift obtained by Horrigan and Aldrich (2002) at saturating Ca\(^{2+}\) concentration (\(\Delta V_H = -33\) mV and \(\Delta \Delta G_V^{Ca} = -1.9\) kJ/mol; at [Ca\(^{2+}\)] = 70 µM). The reason for the contradictory findings is not clear to us. At this stage, we can only identify two differences between the experimental procedures followed by Horrigan and Aldrich (2002) and by us. First, there is a difference in the BK channel clones used (\(hSlo1\) vs \(mSlo1\)). Since mBK channels share a high degree of identity with hBKs (96%), it seems unlikely that the differences in Ca\(^{2+}\) binding and voltage
sensor coupling are due to different BK clones. Second, Horrigan and Aldrich did all their experiments at 0 and 70 μM Ca^{2+} in HEK cells. Here, one can argue that the strength of coupling between Ca^{2+} binding and the voltage sensor may be different in distinct expression systems (e.g., differential modulation) but this is something that is outside the scope of the present paper. Moreover, even if we assume that the calcium effect on VSD is underestimated at 70 μM Ca^{2+} (Horrigan and Aldrich, 2002) compared to 100 μM (our work), we observed a significantly greater effect of Ca^{2+} concentrations (1, 5 and 10 μM, Figure 2C) when less than 50% of the Ca^{2+} sensors are occupied (κ_D = 11 μM (Cox et al., 1997; Horrigan and Aldrich, 2002)).

Fluorescence studies that optically track the motion of the voltage sensor or of the gating ring provide two lines of evidence that support the present findings. First, conformational rearrangements of the voltage sensors detected using voltage-clamp fluorometry can be provoked by Ca^{2+}-binding to the high-affinity sites. A sudden rise in intracellular [Ca^{2+}] caused by a UV flash induced-photolysis of caged Ca^{2+} prompts a leftward shift in both conductance-voltage (G(V)) and fluorescence-voltage (F(V)) relationships. These results suggest that functional activation of the gating ring is propagated to the VSD, leading to structural perturbations of voltages sensors, thereby favoring its active conformation (Savalli et al., 2012). Second, the structural rearrangement of the gating ring in response to Ca^{2+} has a voltage dependence (Miranda et al., 2013, 2018) attributable to the operation of the voltage sensor. The origin of these voltage-dependent motions has recently been established via modifications of the voltage-sensing function of the BK channel using the patch-clamp fluorometry technique (Miranda et al., 2018). Both mutations of the charged residue on the S4 transmembrane segment (R210, R213, and E219) and the co-expression of the β1-subunit with BKα channel, modify the conformational changes of the gating ring triggered by depolarization in correspondence to the observed G(V) shift.
measured for these channel constructs. In contrast, perturbations of pore opening
equilibrium (e.g. through the F315A mutation or the assembly of BKα channel with γ1-
subunit) does not modify the voltage-dependent reorganization of the gating ring (Miranda
et al., 2018).

Mechanistically, how might the CTD-VSD coupling occur in manner that is independent of
channel opening? Taking into account the homotetrameric configuration of the BK
channel, Horrigan and Aldrich (2002) defined the general gating scheme of BK channel
considering the simplest CTD-VSD interaction model in which voltage sensors and Ca²⁺-
binding sites interact solely within the same subunit. However, the VSD movement at non-
saturating Ca²⁺ conditions observed here, which entail distinct functional states of the
Ca²⁺-binding sites (unliganded and liganded), unveiled that the standard HA model is
unable to explain the mechanistic interaction governing the allosteric coupling between
the Ca²⁺ and voltage sensors. Assuming that Ca²⁺-sensors are independent and they
modify the voltage sensor in the same subunit only, Scheme I would predict $Q_C(V)$ curves
characteristic of an all-or-none model showing two well-distinguishable Boltzmann
components corresponding to the fractions of unliganded and Ca²⁺-saturated BK channels
(Figure 4A). Conversely, an energetic effect of each Ca²⁺-site on all the voltage sensors
of the tetramer would lead to an equivalent functional status of each VSD, so that the
$Q_C(V)$ curves would shift as the occupancy of the Ca²⁺ sites increased. Proposing that the
VSD and Ca²⁺ sites interact in the manner described by Scheme II reproduces reasonably
well the behavior of the Ca²⁺-dependent gating charge movement observed in our
experiments (Figure 4B-D). This concerted CTD-VSD communication may underlie a
mechanism analogous to the mechanical strategy of interaction between the
homooctameric ring of RCK domains and the pore module described for bacterial K⁺
channels (Jiang et al., 2002; Ye et al., 2006; Lingle, 2007; Pau et al., 2011; Smith et al.,
In both MthK and BK channels the Ca\textsuperscript{2+}-site occupancy triggers a conformational change corresponding to a symmetric overall rearrangement of the cytosolic tetrameric structure that is ultimately propagated to the transmembrane regions (TMD) via C-linker and in the BK channel, also via the protein-protein interfaces between the gating ring and the TMD (Jiang et al., 2002, 2003; Ye et al., 2006; Yuan et al., 2010, 2012; Pau et al., 2011; Smith et al., 2012; Tao et al., 2017). Thus, we can speculate that each Ca\textsuperscript{2+}-binding event produces a gradual conformational expansion of the gating ring affecting the four voltage sensors in each step through the progressive perturbations within the protein-protein interfaces.

As mentioned above, the communication pathway through which the Ca\textsuperscript{2+}-driven conformational changes are propagated to the voltage sensors appears to reside on the CTD-VSD interface that involves non-covalent interactions between RCK1 N-lobe and S0-S4 transmembrane segments (Yang et al., 2007, 2008, 2010; Sun et al., 2013; Hite et al., 2017; Tao et al., 2017). Although it is not possible at present to dismiss the possibility that the Ca\textsuperscript{2+} binding effect on the VSD workings is, at least in part, mediated by the covalent pulling of the C-linker, we recall that the VSDs are domain-swapped with RCK domains in the gating ring (Tao et al., 2017). Therefore, binding of Ca\textsuperscript{2+} makes the RCK1 N-lobe pull on the S6 helix from its subunit whereas the modification of the contact surface between the RCK1 N-lobe with the voltage sensor of an adjacent subunit induces an outward displacement of the voltage sensor (Hite et al., 2017). These structural arguments make us favor the non-covalent interaction between the CTD and the VSD as the source of the coupling between these two structures. Scanning mutagenesis of RCK1-N terminal subdomain indicates that residues on the \( \beta A-\alpha C \) region are involved in the allosteric connection of the Ca\textsuperscript{2+}-dependent activation mediated by RCK1 site occupancy (Yang et al., 2010). In line with this study, the selective activation of the RCK1 domain was identified.
as being responsible for the Ca$^{2+}$-induced VSD rearrangement (Savalli et al., 2012) and the voltage dependence of the Ca$^{2+}$-driven motions of gating ring (Miranda et al., 2016, 2018), suggesting that CTD-VSD allosteric coupling is primarily determined by the RCK1 site (Sweet and Cox, 2008). However, our results are inconsistent with this picture. The constructs D362A/D367A and 5D5A (D894A-D898A) selectively impair the Ca$^{2+}$-sensitivity of the RCK1- and RCK2-sensors, respectively, by neutralizing the residues that are involved in contributing to Ca$^{2+}$-coordination (Zhang et al., 2010; Tao et al., 2017).

Comparing the fast gating charge movement at 0 Ca$^{2+}$ and saturating Ca$^{2+}$ conditions reveals that the energetic effect of Ca$^{2+}$-binding on voltage sensor equilibrium is practically identical (~ -4 kJ/mol) for both the D362A/D367A and the 5D5A mutations (Figure 5). Thus, our findings establish that the RCK2-driven contribution to CTD-VSD energetic coupling is quite similar to the RCK1-driven contribution. The functional role of the RCK2-sensor on Ca$^{2+}$-sensitivity of VSD activation was further corroborated using the M513I mutation (Figure 6). This point mutation hinders the Ca$^{2+}$-dependent activation associated with the RCK1-sensor, presumably by disrupting the structural integrity of the binding site and the transduction pathway through the βA-αC region (Zhang et al., 2010). Thus, another residue involved in the BK Ca$^{2+}$-dependent activation mediated by the RCK1 Ca$^{2+}$-binding site but not forming part of the site itself, decreases the $Q_c(V)$ leftward shift almost in the same amount as does the D362A/D367A mutant.

We found that the energetic contribution of each RCK site to the voltage sensor equilibrium is the same and its combination mimics the VSD Ca$^{2+}$-sensitivity of the fully occupied sites. These findings remind us of early reports showing that mutations in each RCK site shift the Ca$^{2+}$-dependent $G(V)$ by approximately one-half relative to the effect seen for WT channels (Bao et al., 2002; Xia et al., 2002). Thus, our results suggest that the two RCK-sensors contribute independently to the modulation on the VSD, although we cannot
eliminate the possibility of some cooperativity between them. Indeed, various lines of
evidence indicate that there is some, albeit modest, cooperativity between the two high-
affinity Ca\(^{2+}\)-binding sites although its nature is still unclear (Qian et al., 2006; Sweet and
Cox, 2008; Savalli et al., 2012). Intra and intersubunit structural connectivity supports the
putative cooperative interactions between the Ca\(^{2+}\) sensors at the gating ring (Yuan et al.,
2012; Hite et al., 2017). In fact, a recent functional study of the intrasubunit connections
between the RCK1 site and Ca\(^{2+}\) bowl (R514-Y904/E902 interactions) has shown that
such connections are potential candidates for the structural determinants underlying a
cooperative mechanism between the RCK1- and RCK2-sensor. These interactions are
involved in either the preservation of the integrity of RCK1 Ca\(^{2+}\)-binding site or define the
allostERIC propagation pathway of the chemical energy induced by Ca\(^{2+}\) binding towards
transmembrane domains (Kshatri et al., 2018). On the basis of the cryo-EM structure of
Aplysia californica BK channel, Hite et al. (Hite et al., 2017) proposed that there should be
a positive cooperativity between the Ca\(^{2+}\)-binding at RCK1 site and the Ca\(^{2+}\) bowl since
the Ca\(^{2+}\)-induced conformational change of the RCK1-N lobes from closed to open
configuration depends on the functional state (unliganded and liganded) of both RCK sites.
Our analysis based on the CTD-VSD interaction model can not specify likely cooperative
relations among the two high-affinity Ca\(^{2+}\) sites within the same α-subunit. In fact, the
analysis of our gating current data when using cooperativity between the two high-affinity
sites (Table 1) produced a result at odds with previous reports. Based on the structural
information of the BK channels, it could be considered that cooperative interactions
between the Ca\(^{2+}\) sensors of the different α-subunits (Hite et al., 2017) can also account,
in part, for the Ca\(^{2+}\)-dependent behavior of the VSDs. However, functional studies point
out a more relevant role of the intrasubunit cooperativity (albeit modest) than the
intersubunit cooperativity between the RCK Ca\(^{2+}\) sites (Niu and Magleby, 2002; Qian et
al., 2006). Thus, although a concerted CTD-VSD model (Scheme II) gives better
explanation than an independent CTD-VSD model (Scheme I) to the allosteric
communication of the calcium and voltage sensors, more work is required to explore
improved models able to reproduce more accurately the properties of the interaction CTD-
VSD mechanism in BK channel.

In conclusion, our results depict a remarkable, and direct energetic interplay between the
specialized sensory modules (VSD and CTD) of the BK channel. Our findings together
with the emerging structural-functional information establish a new paradigm about how
stimuli integration (depolarization and intracellular Ca\(^{2+}\)) modulates this channel’s
activation and its relevance within a physiological context. Notable and unexpected is the
equivalent contribution of the distinct ligand-binding sites in the cytosolic domain to the
allosteric regulation of voltage sensing. Additional studies to discern the molecular bases
underlying the Ca\(^{2+}\) and voltage propagation pathways and the cooperative interactions of
the RCK1 and RCK2 regulatory domains may provide new clues about the dual gating
mechanism of BK channel.
Methods

Channel Expression.

*Xenopus laevis* oocytes were used as a heterologous system to express BK channels. The cDNA coding for the human BK α-subunit (U11058) was provided by L. Toro (University of California, Los Angeles, CA). The cDNA coding for independent mutants of each two high-affinity Ca\(^{2+}\) site from BK channel, the double mutant D362A/D367A (Xia et al., 2002), the mutant M513I (Bao et al., 2002) in the RCK1 Ca\(^{2+}\)-binding site, and the mutant 5D5A (Schreiber and Salkoff, 1997) (D894A/D895A/D896A/D897A/D898A) in the RCK2 Ca\(^{2+}\)-binding site or calcium bowl, were kindly provided by M. Holmgren (National Institutes of Health, Bethesda, MD). The cRNA was prepared using mMESSAGE mMACHINE (Ambion) for *in vitro* transcription. *Xenopus laevis* oocytes were injected with 50 ng of cRNA and incubated in an ND96 solution (in mM: 96 NaCl, 2 KCl, 1.8 CaCl\(_2\), 1 MgCl\(_2\), 5 HEPES, pH 7.4) at 18°C for 4–8 days before electrophysiological recordings.

Electrophysiological recordings.

All recordings were made by using the patch-clamp technique in the inside-out configuration. Data were acquired with an Axopatch 200B (Molecular Devices) amplifier and the Clampex 10 (Molecular Devices) acquisition software. Gating current (\(I_G\)) records were elicited by 1-ms voltage steps from −90 to 350 mV in increments of 10 mV. Both the voltage command and current output were filtered at 20 kHz using an 8-pole Bessel low-pass filter (Frequency Devices). Current signals were sampled with a 16-bit A/D converter (Digidata 1550B; Molecular Devices), using a sampling rate of 500 kHz. Linear membrane capacitance and leak subtraction were performed based on a P/4 protocol (Armstrong and Bezanilla, 1974).
Borosilicate capillary glasses (1B150F-4, World Precision Instruments) were pulled in a horizontal pipette puller (Sutter Instruments). After fire-polishing, pipette resistance was 0.5-1 MΩ. The external (pipette) solution contained (in mM): 110 tetraethylammonium (TEA)-MeSO₃, 10 HEPES, 2 MgCl₂; pH was adjusted to 7.0. The internal solution (bath) contained (in mM): N-methyl-D-glucamine (NMDG)-MeSO₃, 10 HEPES, and 5 EGTA for “zero Ca²⁺” solution (∼0.8 nM, based on the presence of ∼10 μM contaminant [Ca²⁺] (Cui et al., 1997). An agar bridge containing 1 M NaMES connected the internal solution to a pool of the external solution grounded with an Ag/AgCl electrode. The calculated bridge/bath junction potential was ∼0.8 mV. For test solutions at different Ca²⁺ concentrations (0.1-100 μM), CaCl₂ was added to reach the desired free [Ca²⁺], and 5 mM EGTA (0.1-0.5 μM) or HEDTA (1-10 μM) was used as calcium buffer. No Ca²⁺ chelator was used in 100 μM Ca²⁺ solutions. Free calcium concentration was estimated using the WinMaxChelator Software and checked with a Ca²⁺-electrode (Hanna Instruments). All experiments were performed at room temperature (20-22 °C). To measure I$_G$ at different Ca²⁺ concentrations in the same oocyte, the patch was excised and washed with an appropriate internal solution using at least 10 times the chamber volume.

**Data Analysis.**

All data analysis was performed using Clampfit 10 (Molecular Devices, RRID:SCR_011323), Matlab (MathWorks, RRID:SCR_001622) and Excel 2007 (Microsoft, RRID:SCR_016137). The first 50-100 μs of the ON-gating currents were fitted to a single exponential function and the area under the curve (Figure 1A-B) was integrated to obtain the charge displaced between closed states ($Q_C$) (Horrigan and Aldrich, 1999, 2002; Contreras et al., 2012; Carrasquel-Ursulaez et al., 2015). $Q_C(V)$ data for each [Ca²⁺] were fitted using a Boltzmann function:
\[ Q_C(V) = \frac{Q_{C, \text{MAX}}}{1 + e\left(\frac{-z_Q F (V - V_H)}{RT}\right)} \]

where \( Q_{C, \text{MAX}} \) is the maximum charge, \( z_Q \) is the voltage dependence of activation, \( V_H \) is the half-activation voltage, \( T \) is the absolute temperature (typically 295 K), \( F \) is the Faraday's constant, and \( R \) is the universal gas constant. \( Q_{C, \text{MAX}}, V_H, \) and \( z_Q \) were determined using least square minimization. \( Q_C(V) \) curves were aligned by shifting them along the voltage axis by the mean \( \Delta V = (\langle V_H \rangle - V_H) \) to generate a mean curve that did not alter the voltage dependence (Horrigan and Aldrich, 1999). All error estimates are SEM.

For each experiment, the time constants obtained from exponential fits to ON-gating currents were shifted along the voltage axis by \( \Delta V \) to determine the mean \( \tau_{I_G-O\text{N}}(V) \) relationships. \( \tau_{I_G-O\text{N}}(V) \) data were fitted to a two-states process described by

\[ \tau(V) = \frac{1}{(\alpha(V) + \beta(V))} \]

where \( \alpha(V) = \alpha_0 e^{(z_J \delta F V / RT)} \) and \( \beta(V) = \beta_0 e^{(z_J (\delta - 1) F V / RT)} \) are, respectively, the forward and backward rate constants which determine the equilibrium constant \( J \) of the voltage sensor (see below). The parameter \( \delta \) is the electrical distance at which the peak of the energy barrier that separates the two resting (R)-active (A) states of the voltage sensor is located, and \( z_J \) is the number of gating charges displaced during the R-A transition.

The Ca\(^{2+}\)-induced effect on VSD activation was quantified as the \( V_H \) shift relative to “zero” Ca\(^{2+}\) condition: \( \Delta V_H = V_H\left([\text{Ca}^{2+}]_i\right) - V_H\left(0\right) \). For wild-type (WT) BK channel and the RCK Ca\(^{2+}\)-sensor mutants (D362A/D367A, M513I and 5D5A), the energetic contribution of Ca\(^{2+}\)-binding on resting-active (R-A) equilibrium of the voltage sensor was calculated as changes in Gibbs free energy of VSD activation induced by 100 µM Ca\(^{2+}\):
\[ \Delta \Delta G_{V}^{Ca} = F \left( Z_Q (100 \, \mu M [Ca^{2+}]) V_H (100 \, \mu M [Ca^{2+}]) - Z_Q (0 [Ca^{2+}]) V_H (0 [Ca^{2+}]) \right) \]

**Model fitting.**

We fit the \( Q_C(V, [Ca^{2+}]) \) experimental data using two distinct interaction mechanisms between Ca\(^{2+}\)-binding sites and voltage sensor (see Scheme I and Scheme II in the Figure 3A-B) within the framework of Horrigan-Aldrich (HA) general allosteric model (Horrigan and Aldrich, 2002). Assumptions and considerations for the equations that describe each one of the Ca\(^{2+}\)-VSD interaction schemes are given in the Appendix. In terms of the HA allosteric mechanisms, the voltage sensor R-A equilibrium is defined by the equilibrium constant \( J \) according to the relation:

\[ J = e^{z_jF(V-V_H)} = J_0 e^{z_jFV} \]

where \( J_0 \) is the zero voltage equilibrium constant and \( z_j \) the gating charge displacement per voltage sensor. Thus, the fraction of the total charge displaced essentially between closed states, \( (Q_C(V)/Q_{CMAX}) \) in the absence of calcium can be written as:

\[ Q_C(V)/Q_{CMAX} (Ca^{2+} \ll K_D) = \frac{1}{1 + J^{-1}} \]

where \( K_D \) is the dissociation constant of the high-affinity calcium-binding site with all voltage sensors at rest and the channel closed. In the presence of saturating Ca\(^{2+}\) (100 \( \mu M \)), the equilibrium of the R-A transition \( J \) becomes amplified by the allosteric factor \( E \), which defines the coupling between Ca\(^{2+}\)-binding sites and voltage sensors, being

\[ Q_C(V)/Q_{CMAX} (Ca^{2+} \gg K_D) = \frac{1}{1 + (JE)^{-1}} \]

and
The $Q_C(V)/Q_{C,\text{MAX}}$ measured in the presence of high [Ca$^{2+}$] and “zero Ca$^{2+}$” condition at the same voltage (so that $J$ be canceled out) but in the limit where $(JE)^{-1} \gg 1$ is:

$$\frac{Q_C(V)/Q_{C, \text{MAX}} \left(\text{Ca}^{2+} \gg K_D\right)}{Q_C(V)/Q_{C, \text{MAX}} \left(\text{Ca}^{2+} \ll K_D\right)_{(\lim_{JE^{-1} \gg 1})}} = \frac{JE}{J} = E$$

Thus, the Gibbs free energy perturbation of the voltage sensor R-A equilibrium when the high-affinity binding sites are approximately 100% occupied by Ca$^{2+}$ (100 µM) is a straightforward measure of the allosteric factor: $E = e^{-\Delta G^G \alpha / RT}$.

Based on these conditions, the values of the allosteric parameter $E$ were calculated and introduced in each of the two Ca$^{2+}$-VSD interaction models as a fixed parameter. Once $E$ was obtained, the families of $Q_C(V, [\text{Ca}^{2+}])$ curves were simultaneously fitted to Equation 4 and Equation 6 (see Appendix) and estimating the $z_j$, $J_0$ and $K_D$ parameters for each model by minimizing least-square values. To select the best Ca$^{2+}$-VSD interaction scheme that describes the experimental data, the fits provided by each model were compared according to their Akaike Information Criterion (AIC) values (Akaike, 1974), calculated as $AIC_i = 2p_i - 2 \ln(L_i)$, where $p_i$ is the number of free parameters and $\ln(L_i)$ is the maximum log-likelihood of the model $i$. The best fit being the one that achieves the lowest $AIC_i$ value.

Minimum $AIC_i$ ($AIC_{\text{MIN}}$) values were used as model selection criteria. Using the $AIC_i$ weights ($w_i$), we estimated the probability of model $i$ is the best model given the data and the set of candidate models. $w_i$ are based on the relative likelihood of each tested model $i$ which is a function of the difference in $AIC_i$ score and the best model: $\Delta AIC_i = AIC_i - AIC_{\text{MIN}}$ (Anderson and Burnham, 2002). From the $\Delta AIC_i$ we obtained an estimate of the relative likelihood of model $i$ ($L_i$) by the simple transform: $L_i = exp \left(-\frac{1}{2} \Delta AIC_i\right)$. $w_i$ is
calculated normalizing the $L_i$ for each model: $w_i = \frac{L_i}{\sum_{k=1}^{K} L_k}$, where $K$ is the number of candidate models.

The models for the Ca$^{2+}$-VSD interaction schemes were extended including two high-affinity Ca$^{2+}$-binding sites per $\alpha$-subunit (Figure 3—figure supplement 1D-E). The contribution of each Ca$^{2+}$-binding site to the free energy of the voltage sensor equilibrium may be split in two, such as $E = E_{S1} * E_{S2} = e^{-(\Delta \Delta G^{a}(S1) + \Delta \Delta G^{a}(S2))/RT}$, where $E_{S1}$ and $E_{S2}$ are the allosteric factors $E$ for the RCK1 and RCK2 sites. Thus, for the global fit of the $Q_C(V, [Ca^{2+}])$ curves, we constrained the allosteric parameter $E_{S1}$ and $E_{S2}$ obtained experimentally for the RCK2 Ca$^{2+}$-sensor mutant (5D5A) and RCK1 Ca$^{2+}$-sensor mutant (D362A/D367A), respectively, as described above. The rest of the parameters $z_j, J_0, K_D1, K_D2,$ and $G$, where $K_D1$ and $K_D2$ are the dissociation constants of the RCK1 and RCK2 sites and $G$ is a cooperativity factor between the two sites within the same $\alpha$-subunit of the BK channel, were allowed to vary freely.
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Competing interests

The authors declare no competing financial interests.
Figures

Figure 1.
Figure 2.
Figure 3.

A. Scheme I

B. Scheme II

C. Model I

D. Model II
Figure 4.

A) Model I

B) Model II

C) $V_H$ (mV) vs. $[Ca^{2+}]$ (μM)

D) $z_Q$ vs. $[Ca^{2+}]$ (μM)
Figure 5

A. D362A/D367A
- 0 Ca\(^{2+}\) 400 pA, 0.2 ms
- 100 μM Ca\(^{2+}\) 200 pA, 0.2 ms

B. 5D5A
- 0 Ca\(^{2+}\) 300 pA, 0.2 ms
- 100 μM Ca\(^{2+}\) 200 pA, 0.2 ms

C. 
\[ \frac{Q_C}{Q_{C,MAX}} \]
- Voltage (mV) vs. [Ca\(^{2+}\)] μM
- 0, 100 μM

D. 
\[ \frac{Q_C}{Q_{C,MAX}} \]
- Voltage (mV) vs. [Ca\(^{2+}\)] μM
- 0, 100 μM

E. 
\[ \Delta V_H \] (mV)
- WT, D362A/D367A, 5D5A

\[ \Delta \Delta G \] (kJ/mol)
- ns, ***
Figure 6.

A

M513I

0 Ca\(^{2+}\) 400 pA 0.2 ms

100 μM Ca\(^{2+}\) 200 pA 0.2 ms

B

\[ \frac{Q_c}{Q_{c,\text{MAX}}} \]

Voltage (mV)

[Ca\(^{2+}\)] μM

0

100

C

ΔV_H (mV)

ΔΔG (kJ/mol)

WT

D362A/
D367A

M513I

ns

***
Table 1. Parameters for the best fits of the $Q_C(V)$ data using different Ca$^{2+}$-VSD interaction models.

<table>
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* Fixed parameters in the model fitting. AIC values correspond to Akaike Information Criterion to select the best fit model. $L_i$ and $w_i$ are the relative likelihood and the weight of each model within the set of candidate models.
Figure 1. $\text{Ca}^{2+}$ binding strongly affects the activation of VSD in BK channels. (A-B)

Fast component of the ON-gating current ($I_{G-ON}$) at 0 and 100 μM internal $\text{Ca}^{2+}$ concentration, respectively. The representative $I_{G-ON}$ records were evoked by applying a 160-mV voltage step of 1 ms duration. The first 100 μs of the $I_{G-ON}$ were fitted to a single exponential function (red line; $\tau_{I_{G-ON}}(0 \text{Ca}^{2+}) = 58 \mu s$ and $\tau_{I_{G-ON}}(100 \mu M) = 30 \mu s$). The area under the curve described by the monoexponential fit (grey areas) was integrated to obtain the charge displaced between closed states ($Q_C$). For comparison, the initial time course of the macroscopic $\text{K}^+$ current ($I_K$) activation (solid black line) obtained at 0 and 100 μM $\text{Ca}^{2+}$ were superimposed on the $I_{G-ON}$ under the same internal $\text{Ca}^{2+}$ conditions. The $I_K$ were evoked by a 15 ms pulse to 160 mV. The $I_K$ is described by an exponential function with initial delay: $\Delta t_{I_K}(0 \text{Ca}^{2+}) = 0.16 \text{ ms}$ and $\tau_{I_K}(0 \text{Ca}^{2+}) = 3.37 \text{ ms}$ at 0 $\text{Ca}^{2+}$; and $\Delta t_{I_K}(100 \mu M) = 0.08 \text{ ms}$ and $\tau_{I_K}(100 \mu M) = 0.66 \text{ ms}$ at 100 μM $\text{Ca}^{2+}$. After 1 ms, the $I_K$ increased to about 20% and 80% of its steady-state amplitude in 0 $\text{Ca}^{2+}$ and 100 μM $\text{Ca}^{2+}$, respectively. (C) Voltage-dependence of the $Q_C$ and of the gating current time constants ($\tau_{I_{G-ON}}$) at 0 $\text{Ca}^{2+}$ (open circles) and 100 μM $\text{Ca}^{2+}$ (filled circles). Gating charge-voltage relationships ($Q_C(V)/Q_{C,MAX}$) were obtained by integrating the fast component for each ON $I_G$ trace (from -90 mV to 350 mV). Boltzmann fitting to the experimental data (mean ± SEM) is indicated by solid line at “zero” $\text{Ca}^{2+}$ ($V_H = 174.5 \pm 2.4 \text{ mV}$, $z_Q = 0.60 \pm 0.01$, $n = 25$) and by a dashed line at 100 μM $\text{Ca}^{2+}$ ($V_H = 31.9 \pm 4.5 \text{ mV}$, $z_Q = 0.66 \pm 0.01$, $n = 7$). Right ordinate shows the time constants data (mean ± SEM) of the exponential decays of $I_{G-ON}$ ($\tau_{I_{G-ON}}$) plotted against the voltage. The best fit to a two-state model of the VSD activation where the $z_j$ was constrained to the values found for the $Q_C(V)$ relation ($z_Q$) is indicated by solid lines at “zero” $\text{Ca}^{2+}$ ($\alpha_0 = 3.73 \text{ ms}^{-1}$, $\beta_0 = 76.10 \text{ ms}^{-1}$ and $\delta = 0.29$) and dashed line at 100 μM $\text{Ca}^{2+}$ ($\alpha_0 =$
7.28 ms\(^{-1}\), \(\beta_0 = 6.98\) ms\(^{-1}\) and \(\delta = 0.36\). The corresponding \(V_H\) at each internal Ca\(^{2+}\) concentration is indicated by a vertical line. (D) Semi-logarithmic plot of the \(Q_C(V)/Q_{C,\text{MAX}}\) curves at 0 Ca\(^{2+}\) and saturating Ca\(^{2+}\) concentration (100 µM). The allosteric parameter \(E\) determines the vertical displacement of the 0 mV intercept (dashed vertical line) of the \(Q_C(V)/Q_{C,\text{MAX}}\) curve at 100 µM Ca\(^{2+}\) relative to the 0 Ca\(^{2+}\) condition.

**Figure 2. Ca\(^{2+}\)-dependent effects on VSD activation in BK channels.** (A) Representative gating current \((I_G)\) recordings at different internal Ca\(^{2+}\) concentrations (from 0 to 100 µM). \(I_G\) was evoked by the indicated voltage protocol of 1 ms duration. Representative gating current records are from different patches with the exception of 0 and 100 µM Ca\(^{2+}\). (B) Gating charge-voltage relationships \((Q_C(V))\) were obtained by integrating the fast component for each ON \(I_G\) trace. Normalized gating charge data \((Q_C(V)/Q_{C,\text{MAX}})\) (mean ± SEM) were fitted using a single Boltzmann function (solid lines). The fit parameters are as follows: “zero” Ca\(^{2+}\) \((V_H = 174.5 ± 2.4\) mV, \(z_Q = 0.60 ± 0.01, n = 25\)); 0.1 µM Ca\(^{2+}\) \((V_H = 162.4 ± 4.2\) mV, \(z_Q = 0.59 ± 0.01, n = 5\)); 0.5 µM Ca\(^{2+}\) \((V_H = 151.6 ± 1.3\) mV, \(z_Q = 0.60 ± 0.01, n = 5\)); 1 µM Ca\(^{2+}\) \((V_H = 137.1 ± 5.1\) mV, \(z_Q = 0.61 ± 0.01, n = 5\)); 5 µM Ca\(^{2+}\) \((V_H = 121.9 ± 3.8\) mV, \(z_Q = 0.63 ± 0.01, n = 5\)); 10 µM Ca\(^{2+}\) \((V_H = 67.3 ± 17.1\) mV, \(z_Q = 0.64 ± 0.08, n = 4\)); 100 µM Ca\(^{2+}\) \((V_H = 31.9 ± 4.5\) mV, \(z_Q = 0.66 ± 0.01, n = 7\)). (C) \(V_H\) obtained from the \(Q_C(V)\) curves as a function of Ca\(^{2+}\) concentration (mean ± SEM). Ca\(^{2+}\) binding produces a leftward shift in \(V_H\) \((\Delta V_H): 0.1 \mu\text{M Ca}^{2+}\) \((\Delta V_H = -12.1 ± 3.5\) mV); 0.5 µM Ca\(^{2+}\) \((\Delta V_H = -22.9 ± 1.8\) mV); 1 µM Ca\(^{2+}\) \((\Delta V_H = -37.1 ± 3.5\) mV); 5 µM Ca\(^{2+}\) \((\Delta V_H = -50.3 ± 4.7\) mV); 10 µM Ca\(^{2+}\) \((\Delta V_H = -107.1 ± 17.1\) mV); 100 µM Ca\(^{2+}\) \((\Delta V_H = -142.6 ± 4.5\) mV). One-way ANOVA followed by Dunnett’s post-hoc test
analysis was used to assess statistical significance of the Ca\(^{2+}\)-induced shifts in \(V_H\) (**\(p<0.001\)).

**Figure 3.** Model-dependent behavior of the \(Q_C(V)\) curves based on the CTD-VSD interaction mechanisms according to the fractional occupancy of Ca\(^{2+}\)-binding sites. 

(A-B) Cartoons representing two interaction schemes between voltage sensors and Ca\(^{2+}\)-binding sites (modified from Horrigan and Aldrich (2002)). Scheme I (A) assumes that Ca\(^{2+}\)-binding only affects the voltage sensor of one \(\alpha\)-subunit (\(E_{M1}\)), whereas Scheme II (B) predicts that binding of Ca\(^{2+}\) to one \(\alpha\)-subunit will affect VSD in all subunits equally, increasing the voltage sensor equilibrium constants (\(J\)) \(E_{M2}\)-fold in all four subunits (\(E_{M2}\), when the four Ca\(^{2+}\) sites are occupied). In both schemes, a single Ca\(^{2+}\)-binding site is considered in each \(\alpha\)-subunit. (C-D) Predictions of \(Q_C(V)\) relationships at different internal calcium concentration (from 0 to 10 mM) by two distinctive interaction mechanisms between Ca\(^{2+}\)-binding sites and voltage sensors (Scheme I and Scheme II), respectively. \(Q_C(V)\) curves were generated using Equation 4 (blue: Model I) or Equation 6 (red: Model II), and the following set of parameters: \(z_J = 0.58, J_0 = 0.018, K_D = 11\ \mu M\) and \(E_{M1} = E_{M2}^4 = 25\).

**Figure 4.** Dose-dependent effect of Ca\(^{2+}\) on voltage sensor activation is predicted by a Ca\(^{2+}\)-VSD interaction mechanism in which Ca\(^{2+}\)-binding affects equally the VSD in all four \(\alpha\)-subunits. (A-B) The experimental \(Q_C(V)\) data were fitted using the two possible allosteric interaction mechanisms between voltage and calcium sensors described by Scheme I and Scheme II. The blue and red lines represent the global fits by Model I and Model II, respectively. The allosteric factor \(E\) (\(E_{M1}\) and \(E_{M2}\)) was constrained to the value obtained from the individual fitting of the \(Q_C(V)/Q_{C,MAX}\) curves at 0 and 100 \(\mu M\) Ca\(^{2+}\) (experimental \(E\) (\(E_{exp}\)) equal to 26.4, see Table 1). The \(z_J, J_0\) and \(K_D\) parameters were allowed to vary freely. Note that the allosteric factor \(E\) for Model I (\(E_{M1}\)) and Model II (\(E_{M2}\))
have different interpretations, since $E_{M1} = E_{exp}$ whereas $E_{M2} = \sqrt{E_{exp}}$ given that the four voltage sensor will be altered in 2.3-fold ($E_{M2} = 2.27$) with each additional Ca$^{2+}$ bound. (C-D) The Ca$^{2+}$-dependence of $z_Q Q_C(V)$ (C) and $V_H Q_C(V)$ (D) curves are superimposed with the $z_Q$ and $V_H$ values predicted by Model I (blue line) and Model II (red line).

**Figure 5.** The high-affinity Ca$^{2+}$-binding sites contribute equally to the allosteric coupling between calcium and voltage sensors in BK channels. (A-B) Representative gating current ($I_G$) recordings at 0 and 100 μM of [Ca$^{2+}$], for the RCK1 site mutant (D362A/D367A) and the RCK2 site mutant (5D5A), respectively. (C-D) Gating charge-voltage curves ($Q_C(V)$) were obtained at 0 Ca$^{2+}$ (open symbols) and 100 μM Ca$^{2+}$ (filled symbols) for D362A/D367A and 5D5A mutants, respectively. Boltzmann fitting to the experimental data (mean ± SEM) is indicated by solid lines ($V_H(D362A/D367A) = 178.0 ± 2.7$ mV, $z_Q = 0.58 ± 0.01$, $n = 12$ and $V_H(5D5A) = 176.4 ± 4.6$ mV, $z_Q = 0.58 ± 0.01$, $n = 17$ at “zero” Ca$^{2+}$; $V_H(D362A/D367A) = 104.2 ± 7.3$ mV, $z_Q = 0.56 ± 0.02$, $n = 7$ and $V_H(5D5A) = 110.8 ± 6.7$ mV, $z_Q = 0.58 ± 0.02$, $n = 6$ at 100 μM Ca$^{2+}$). For comparison, all $Q_C(V)$ plots include the Boltzmann fit of the $Q_C(V)$ curves for WT at 0 Ca$^{2+}$ (dashed black line) and 100 μM Ca$^{2+}$ (solid black line). (E) Quantification of the $V_H$ shift ($\Delta V_H$) in the $Q_C(V)$ curves and the free energy change ($\Delta \Delta G^C_V$) induced by 100 μM Ca$^{2+}$. The non-parametric $t$-test was used to evaluate statistical significances between WT BK channel and the RCK sites mutants (**p<0.001).

**Figure 6.** Mutations abolishing Ca$^{2+}$-sensing by the RCK1 binding-site reduce the Ca$^{2+}$-induced effect on voltage sensors activation similarly. (A) Representative gating current ($I_G$) recordings at 0 and 100 μM [Ca$^{2+}$], for the RCK1 site mutant M513I. (B) Gating charge-voltage curves $Q_C(V)$ were obtained at 0 Ca$^{2+}$ and 100 μM Ca$^{2+}$ (open and filled symbols) for the M513I mutant. Boltzmann fit to the experimental data (mean ± SEM) is
indicated by solid lines ($V_{H(M513I)} = 170.4 \pm 4.4$ mV, $z_Q = 0.58 \pm 0.01, n = 17$ at “zero” Ca$^{2+}$ and $V_{H(M513I)} = 105.0 \pm 6.3$ mV, $z_Q = 0.62 \pm 0.03, n = 4$ at 100 µM Ca$^{2+}$). For comparison, the $Q_C(V)$ plot includes the Boltzmann fit of the $Q_C(V)$ curves for WT at 0 Ca$^{2+}$ and 100 µM Ca$^{2+}$ (dashed and solid black line). (C) Quantification of the $V_H$ ($\Delta V_H$) shift in the $Q_C(V)$ curves and the free energy change induced by 100 µM Ca$^{2+}$ ($\Delta \Delta G^{Ca}_V$). A non-parametric t-test was used to compare WT and RCK1-site mutants BK channels (**p<0.001).
Appendix

Assumptions and model testing. We assumed that the four voltage sensors act independently, transiting between two states, resting (R) and active (A), governed by the voltage-dependent equilibrium constant $J$. The R–A equilibrium is displaced toward the active state by membrane depolarization, generating a fast gating charge movement ($Q_C$) before channel opening. Additionally, the Ca$^{2+}$-binding to high-affinity sites shifts the voltage sensor equilibrium toward its active configuration through an allosteric coupling described by the factor $E$ (Figure 3—figure supplement 1A). By assuming the simplified standard model for the BK channels (Horrigan and Aldrich, 2002), where each $\alpha$-subunit has a single Ca$^{2+}$-binding site, we established the possible states and their connections through which each voltage sensor transits in the presence of Ca$^{2+}$ (Figure 3—figure supplement 1B-C) following the CTD-VSD interaction mechanisms described by Scheme I and II (Figure 3A-B).

For Scheme I, in which Ca$^{2+}$-binding sites and voltage sensors interact within the same $\alpha$-subunit, the activation of each VSD can occur through the $R_0$-$A_0$ or $R_1$-$A_1$ transitions according to the functional state of the Ca$^{2+}$ site (unbound or Ca$^{2+}$ bound). The equilibrium of such transitions is governed by $J$ and $J E_{M1}$, respectively (Figure 3—figure supplement 1B). In the case of Scheme II, in which binding of Ca$^{2+}$ to a single $\alpha$-subunit affects all four voltage sensors equally, the R-A equilibrium for each VSD would be affected by the number of Ca$^{2+}$ bound in the channel (0-4) depicted in the model (Model II) as five possible R-A transitions. According to this model, the $J$ constant increase $E_{M2}$-fold for each Ca$^{2+}$ site occupied (Figure 3—figure supplement 1C). For both schemes, the horizontal transitions $R$-$R$ and $A$-$A$ represent the Ca$^{2+}$-binding equilibrium ($K$ or $KE$) when the VSD is in the resting and active conformation, respectively. The equilibrium constant $K$ is defined as the
bound/unbound probability ratio for each Ca\(^{2+}\)-binding site and depends on Ca\(^{2+}\) concentration ([Ca\(^{2+}\)]) and the Ca\(^{2+}\) dissociation constant (K\(_D\)): K = [Ca\(^{2+}\)] / K\(_D\).

Here, we assumed that the voltage sensor movement at ON-gating currents is in equilibrium relative with the binding of Ca\(^{2+}\). The assumption is reasonable since the Ca\(^{2+}\)-binding rate constant estimated for BK channel is 1.8 x 10\(^8\) M\(^{-1}\)s\(^{-1}\) (Hou et al., 2016) implying that at 10 \(\mu\)M internal Ca\(^{2+}\) the association time constant is 340 \(\mu\)s. Thus, Ca\(^{2+}\) binding at this Ca\(^{2+}\) concentration proceeds with a time constant about six-fold longer than does the movement of the voltage sensor (~60 \(\mu\)s). Based on this consideration, the R-A transitions in the models would be predominant transitions whose proportion would be determined by the [Ca\(^{2+}\)] and K\(_D\). Therefore, predictions of the \(Q_C(V)\) curves at different Ca\(^{2+}\) concentrations for Model I and Model II were based on a given fractional occupancy of Ca\(^{2+}\) sites established by the probability of Ca\(^{2+}\) bound (b) and unbound (1 − b) for each Ca\(^{2+}\)-sensor, and the energetic contribution to VSD equilibrium.

Simulations of the \(Q_C(V)\) curves using the Scheme I (Model I) were obtained using the equation

\[
\frac{Q_C(V)}{Q_{C, \text{MAX}}} = (1 - b) \left( \frac{1}{1 + J^{-1}} \right) + b \left( \frac{1}{1 + (JE_{M1})^{-1}} \right)
\]

(1);

where

\[
b = \frac{1}{1 + K^{-1}} = \frac{1}{1 + \frac{K_D}{[Ca^{2+}]}} = \frac{[Ca^{2+}]}{[Ca^{2+}] + K_D}
\]

(2);

and

\[
J = J_0 e^{z_F V F / R T}
\]

(3)

Substituting b and J into Equation (1), the Ca\(^{2+}\)-dependent voltage sensor activation for Model I is given by the equation.
\[
\frac{Q_C(V)}{Q_{C, \text{MAX}}} = \left( \frac{K_D}{[Ca^{2+}] + K_D} \right) \left( \frac{1}{1 + e^{\frac{-z_JFV}{RT} - \frac{J_0}{J_0E_{M2}}} \frac{1}{1 + e^{\frac{-z_JFV}{RT} - \frac{J_0}{J_0E_{M2}}}} \frac{1}{1 + e^{\frac{-z_JFV}{RT} - \frac{J_0}{J_0E_{M2}}}} \right) \quad (4)
\]

Thus, the \( Q_C(V) \) curves are determined by the proportion of two functional VSD populations with a distinctive effect (unliganded effect or \( Ca^{2+} \)-saturated effect). Consequently, the \( Q_C(V) \) curves are represented by a weighted sum of two Boltzmann functions.

Meanwhile, for the concerted CTD-VSD interaction Scheme II (Model II), the \( Q_C(V,[Ca^{2+}]) \) curves would be determined using the general equation:

\[
\frac{Q_C(V)}{Q_{C, \text{MAX}}} = \sum_{x=0}^{n} \binom{n}{x} (1 - b)^{n-x} b^x \left( \frac{1}{1 + \left( JE_{M2} \right)^{-1}} \right) \quad (5)
\]

The expression in the first bracket represents the fraction of VSD belonging to a channel with \( x \) (0 to 4) \( Ca^{2+} \) bound, according to a binomial probability distribution. Thus, the \( Q_C(V) \) curves result in a weighted sum of five distinct Boltzmann functions corresponding to the five possible R-A transitions (Figure 3—figure supplement 1C). By setting \( n = 4 \) because the tetrameric symmetry of the channels, and substituting \( b \) and \( J \) into the previous equation (Equation 5) we have

\[
\frac{Q_C(V)}{Q_{C, \text{MAX}}} = \sum_{x=0}^{4} \binom{4}{x} \left( \frac{K_D}{[Ca^{2+}] + K_D} \right)^{4-x} \left( \frac{[Ca^{2+}]}{[Ca^{2+}] + K_D} \right)^{x} \left( \frac{1}{1 + e^{\frac{-z_JFV}{RT} - \frac{J_0}{J_0E_{M2}}} \frac{1}{1 + e^{\frac{-z_JFV}{RT} - \frac{J_0}{J_0E_{M2}}}} \frac{1}{1 + e^{\frac{-z_JFV}{RT} - \frac{J_0}{J_0E_{M2}}}} \right) \quad (6)
\]

It should be noted that at limiting \( Ca^{2+} \) conditions, both schemes become equivalent where the VSD activation is characterized by a single Boltzmann function. At zero \( Ca^{2+} \), the \( Q_C(V) \) curves are described by

\[
\frac{Q_C(V)}{Q_{C, \text{MAX}}} = \left( \frac{1}{1 + e^{\frac{-V}{R_T J}}} \right),
\]

whereas Ca\textsuperscript{2+} saturating concentration \( J \) is multiplied by the allostERIC factor \( E \), where \( E = E_{M1} = E_{M2} \) depending on the model (Model I or Model II):

\[
\frac{Q_C(V)}{Q_{C, \text{MAX}}} = \left( \frac{1}{1 + e^{\frac{-V}{R_T J}}} \right)
\]

Given that each \( \alpha \)-subunit has two Ca\textsuperscript{2+}-binding sites, we expanded the CTD-VSD interaction schemes (\textit{Figure 3—figure supplement 1C}) considering the existence of two Ca\textsuperscript{2+}-binding sites (\textit{Figure 3—figure supplement 1D-E}). The Model I and II include the energetic contribution of RCK1 and RCK2 Ca\textsuperscript{2+}-sites to the VSD activation. The factor \( E = E_{S1} * E_{S2} \) where \( E_{S1} \) and \( E_{S1} \) are the allostERIC coupling between the VSD and the RCK1 Ca\textsuperscript{2+}-site and RCK2 Ca\textsuperscript{2+}-site, respectively. The \( K_1 \) and \( K_2 \) constants define the bound/unbound transition for each RCK1 and RCK2 sites with \( K_1 = [Ca^{2+}] / K_{D1} \) and \( K_2 = [Ca^{2+}] / K_{D2} \).

Assuming that the Ca\textsuperscript{2+} sensors of distinct \( \alpha \)-subunit do not interact, we only consider intrasubunit cooperativity between the RCK1 and RCK2 sites defined by the factor \( G \). Thus, the occupancy of one RCK site will affect Ca\textsuperscript{2+}-binding equilibrium to the other RCK site in the \( \alpha \)-subunit (\( GK_1 \) and \( GK_2 \)) (\textit{Figure 3—figure supplement 1E}). Note that for Model II the equilibrium \( J \) of the VSD increase \( E_{S1} \)-fold and \( E_{S2} \)-fold for each Ca\textsuperscript{2+} bound to the RCK1 and RCK2 sites, respectively, reaching \( J E_{S1}^4 E_{S2}^4 \) when the eight Ca\textsuperscript{2+} sites are occupied.
Supplementary Figures

Figure 2—figure supplement 1.

A

B

C

D

E

F

-90 mV
200 mV
\Delta t 0.2 to 4 ms
0 Ca\textsuperscript{2+}
10 μM Ca\textsuperscript{2+}
t = 0.2 ms
t = 4 ms

\begin{align*}
Q_C / Q_{C,\text{MAX}} & \quad V = -90 \text{ mV} \\
V_{H1} (10 \text{ μM}) & \quad V_{H2} (0 \text{ μM}) \\
\tau_F & \quad 10 \text{ μM} \\
0 \text{ μM} & 
\end{align*}

\begin{align*}
Q_{OFF} / Q_{MAX} & \quad \text{Pulse duration (ms)} \\
Q_F & \quad Q_S
\end{align*}
Figure 3—figure supplement 1.

Scheme I

- **A**
  - VSD: $R \downarrow J \hookrightarrow U \uparrow K \hookrightarrow B \cdot Ca^{2+} \downarrow E \rightarrow CTD

- **B**
  - Scheme I
  - \( R_0 \rightarrow R_1 \rightarrow R_2 \rightarrow R_3 \rightarrow R_4 \)
  - \( J \rightarrow K \rightarrow KE_{M1} \rightarrow Ca^{2+} \)

- **C**
  - Scheme II
  - \( R_0 \rightarrow R_1 \rightarrow R_2 \rightarrow R_3 \rightarrow R_4 \)
  - \( J \rightarrow KE_{M2} \rightarrow Ca^{2+} \)

- **D**
  - Scheme I and Scheme II - Two Ca$^{2+}$-Sites
  - \( E_{S1} \rightarrow E_{S2} \rightarrow E_{S2} \rightarrow E_{S3} \)

- **E**
  - Scheme I and Scheme II - Two Ca$^{2+}$-Sites
  - \( R_{0,0} \rightarrow R_{1,0} \rightarrow R_{1,1} \rightarrow R_{0,1} \)
  - \( K_1 \rightarrow K_2 \rightarrow K_1 E_{S1} \rightarrow K_2 E_{S2} \)

*Note: x and y = 0 (VSD transitions only dependent of the functional state of the RCK1 and RCK2 sites in the same α-subunit). x and y = from 0 to 3 (number of RCK1 sites occupied and number of RCK2 sites occupied, respectively, in the other three α-subunits).*
Figure 3—figure supplement 2.
Figure 4—figure supplement 1.
Legends Supplementary Figures

Figure 2—figure supplement 1. Ca$^{2+}$ increases the slow component of the OFF gating currents. (A) Recording of gating current ($I_g$) evoked by 200 mV pulses of different durations (from 0.2 to 4 ms) at 0 and 10 μM [Ca$^{2+}$] conditions, respectively. (B-C) The top panels show the superimposed traces of the $I_g$-OFF recorded at -90 mV evidencing a decrease in amplitude and a slower decay of the OFF current as the duration of the pulse increases at 10 μM Ca$^{2+}$. The dashed line represents the baseline for each experiment. $I_g$-OFF were fitted with an exponential function of two-components (fast and slow components). $I_g$-OFF traces at 0.2 ms and 4 ms pulse duration are displayed for each Ca$^{2+}$ condition. Orange and blue lines correspond to fast and slow components of the two-exponential fits, respectively: (B) “zero” Ca$^{2+}$ ($\tau_F = 10 \mu$s and $\tau_S = 44 \mu$s) and (C) 10 μM Ca$^{2+}$ ($\tau_F = 25 \mu$s and $\tau_S = 212 \mu$s).

(D) Plots of the gating currents time constants measured at 0 Ca$^{2+}$ (open symbols, solid line) and 10 μM Ca$^{2+}$ (filled symbols, dot-dashed line). Data are well described using the equations of the two-state model (see Methods) with the following parameters: $\alpha_0 = 3.73$ ms$^{-1}$, $\beta_0 = 76.10$ ms$^{-1}$ and $\delta = 0.29$ at 0 Ca$^{2+}$ and $\alpha_0 = 3.98$ ms$^{-1}$, $\beta_0 = 10.61$ ms$^{-1}$ and $\delta = 0.37$ at 10 μM Ca$^{2+}$. The fast OFF time constants at -90 mV for 0 Ca$^{2+}$ (10 μs, orange open circles) and 10 μM Ca$^{2+}$ (25 μs, orange filled circles) from panels B and C are shown. Time constants extrapolated to -90 mV from the two-state model are close to the experimental measurements: 3 μs and 21 μs for 0 Ca$^{2+}$ and 10 μM Ca$^{2+}$, respectively. Boltzmann fit of the $Q_C(V)$ curves for 0 Ca$^{2+}$ (solid line) and 10 μM Ca$^{2+}$ are also drawn (dot-dashed line). (E-F) The relative amplitude of the OFF-charge components, the fast ($Q_F$, orange symbols) and slow ($Q_S$, blue symbols) charge components were plotted against the pulse duration and fitted with an exponential function representing the time course of the opening of the
channel: (E) “zero” Ca\(^{2+}\) (open circles, \(\tau_{0\text{Ca}^{2+}} = 1.8\) ms) and (F) 10 \(\mu\text{M}\) Ca\(^{2+}\) (filled circles, \(\tau_{10\mu\text{M}} = 536\) \(\mu\text{s}\)).

**Figure 2**—figure supplement 2. Voltage-dependent movement of the ON and OFF gating charge has a similar behavior at saturating Ca\(^{2+}\) conditions. (A) Normalized gating current \((I_g)\) trace at 160-mV voltage step for three different experiments recordings in 100 \(\mu\text{M}\) of internal Ca\(^{2+}\) conditions. The \(I_g\)-160 mV trace represented by the black dashed line corresponds to the representative \(I_g\) at 100 \(\mu\text{M}\) Ca\(^{2+}\) in **Figure 2A**. In this record, the \(I_g\)-ON was evoked by 1 ms voltage steps of 10 mV, going from -90 to 350 and the OFF-gating currents (\(I_g\)-OFF) recorded at -90 mV of 1 ms duration. For the \(I_g\) represented by the purple and pink lines, the \(I_g\)-ON was evoked by 2 ms voltage steps of 10 mV, going from -90 to 350 and the \(I_g\)-OFF recorded at -200 mV (Experiment 1) and -150 mV (Experiment 2) of 2 ms duration, respectively. For comparison, only was shown the \(I_g\) trace at 160-mV voltage step of each experiment. (B) \(Q_{ON}\) plotted against \(Q_{OFF}\) are linearly related in Experiment 1 (Exp 1: purple symbols) and Experiment 2 (Exp 2: pink symbols). \(Q_{ON}\) was obtained by integrating the fast component for each ON \(I_g\) trace \((Q_{ON} = Q_c)\), and the \(Q_{OFF}\) was determined by integrating \(I_g\)-OFF for each pulse. (C) Normalized ON gating charge data (open symbols: \(Q_c(V)/Q_{c,\text{MAX}}\)) and OFF gating charge data (filled symbols: \(Q_{OFF}(V)/Q_{OFF,\text{MAX}}\)) were fitted using a single Boltzmann function for each experiment: \(Q_c(V)/Q_{c,\text{MAX}} (V_H = 44.5\) mV, \(z_Q = 0.59)\) and \(Q_{OFF}(V)/Q_{OFF,\text{MAX}} (V_H = 52.8\) mV, \(z_Q = 0.62)\) for the Exp 1 (\(V_{OFF} = -200\) mV); and \(Q_c(V)/Q_{c,\text{MAX}} (V_H = 29.5\) mV, \(z_Q = 0.53)\) and \(Q_{OFF}(V)/Q_{OFF,\text{MAX}} (V_H = 35.3\) mV, \(z_Q = 0.62)\) for the Exp 2 (\(V_{OFF} = -150\) mV).

**Figure 3**—figure supplement 1. Kinetic models of the VSD activation according to the CTD-VSD interaction schemes. (A) Sub-scheme describing calcium and voltage allosteric interaction for closed channels. The VSD transit between two resting (R) and active (A)
configuration governed by the equilibrium constant $J$, where each Ca$^{2+}$ site undergoes unbound (U) - Ca$^{2+}$ bound (B) transitions governed by the equilibrium constant $K$. The allosteric factor $E$ accounts for the coupling between the calcium and voltage sensors (CTD-VSD). (B-C) VSD kinetic models in the presence of Ca$^{2+}$ according to CTD-VSD interaction schemes I and II (Figure 3A-B), respectively, where the vertical transitions (R-A) represent the VSD movement and the horizontal transitions (R-R and A-A) are Ca$^{2+}$-binding reactions when the VSD is in the resting or active conformation. For Scheme I (B), each VSD can undergo $R_0$-$A_0$ or $R_1$-$A_1$ transitions depending on the unbound or bound state of the Ca$^{2+}$ site in the $\alpha$-subunit, respectively. Thus, the $R_1$-$A_1$ equilibrium is defined by $J$ increased $E_{M1}$-fold ($J E_{M1}$). For Scheme II (C), the $R_0$-$A_0$ to $R_4$-$A_4$ transitions represent the VSD equilibrium with 0, 1, 2, 3, and 4 occupied Ca$^{2+}$ sites in the channel. Thus, for each Ca$^{2+}$ bound the equilibrium constant $J$ increase $E_{M2}$-fold reaching to $J E_{M2}^4$ when the four Ca$^{2+}$ sites are occupied. The thickness of the arrows indicates the probability of transitions. (D) General sub-scheme of the CTD-VSD interaction including two Ca$^{2+}$ sites for each CTD (RCK1 and RCK2 sites). For each RCK1 and RCK2 site the unbound-Ca$^{2+}$ bound transitions are governed by the equilibrium constants $K_1$ and $K_2$. The factor $G$ describes the cooperativity between the sites within the same $\alpha$-subunit; and the $E_{S1}$ and $E_{S2}$ factors define the allosteric coupling between the RCK1 and RCK2 sites and the VSD, respectively. (E) Schematic representation of VSD kinetic model according to the extended version of the Scheme I and Scheme II (C) accounting for both RCK1 and RCK2 Ca$^{2+}$-sites on each $\alpha$-subunit. The VSD transitions in Scheme I only depend on the unbound or bound state of the RCK sites within the same $\alpha$-subunit: unliganded ($R_{0,0}$-$A_{0,0}$), RCK1 site occupied ($R_{1,0}$-$A_{1,0}$), RCK2 site occupied ($R_{0,1}$-$A_{0,1}$) and both sites occupied ($R_{1,1}$-$A_{1,1}$). For sake simplicity, Scheme II, only depicts VSD transitions described for the Scheme I. In this case, $x$ and $y$ represent the
number of RCK1 sites occupied and number of RCK2 sites occupied, respectively, in the other three α-subunits (x = from 0 to 3 and y = from 0 to 3).

**Figure 3**—figure supplement 2. The resting-active transition of the voltage sensor is fast enough to assume no Ca\textsuperscript{2+} re-equilibration during gating currents measurements. Simulation of \( z_Q \), as a function of the time constant ratios of Ca\textsuperscript{2+} binding and gating currents are shown. Gating currents were simulated for a BK Scheme I ([Figure 3A](#)). The Ca\textsuperscript{2+} binding rate constant was \( k_b = 1.81 \cdot 10^8 \) M\textsuperscript{-1}s\textsuperscript{-1} (Hou et al. 2016) and the unbinding rate constant \( k_u = 1150. \) s\textsuperscript{-1} was calculated using a \( K_D = 6.4 \cdot 10^{-6} \) M ([Table 1](#)). Voltage-dependent rates for the voltage sensor activation were taken from [Figure 1](#). Gating current were simulated using different calcium-binding time constants: \( \tau_{\text{Ca binding}} = \frac{1}{x} (k_b [Ca^{2+}] + k_u) \) scaled with different x-factors ranging from 0.01 to 1000. We fitted the simulated gating current at 10 μM Ca\textsuperscript{2+} to a single exponential using the first 100 μs of the gating current decay. The maximum gating current time constant was used to calculate the time constant ratios shown in the horizontal axis of the figure. The vertical dashed line marks the time constant ratio calculated for x = 1.

The \( Q_C(V) \) data obtained by integration of the area under the exponential function were fitted using a Boltzmann function. The sum of the residuals squared, SMSQ, was used as an indication of the goodness of the fit. The figure shows that the fit was good (low SMSQ) and the experimental \( z_Q \) value (0.61) was recovered for calcium-binding/gating current time constant ratio 0.04 or less; i.e. fast calcium re-equilibration, which is obtained for a calcium-binding rated constant one hundred times faster than the reported by Hou et al. (2016). We conclude that the good fit to a single Boltzmann sigmoidal function to our experimental \( Q_C(V) \) curves is not due to fast calcium re-equilibration but due to the failure of Model I to describe...
our data. This conclusion is the same for analysis based on the first 30 μs of the simulated gating currents.

Figure 4—figure supplement 1. Fitting of experimental $Q_C(V)$ data by the Ca$^{2+}$-VSD interaction mechanisms including two Ca$^{2+}$-binding sites per α-subunit. (A-B) The blue and red lines represent the global fits to the experimental $Q_C(V)$ curves by Model I (A) and Model II (B), respectively, with two Ca$^{2+}$ sites in each α-subunit. For each model a cooperativity factor between the Ca$^{2+}$ sites within the same subunit ($G \neq 1$) (Upper) or no cooperative interactions between the Ca$^{2+}$ sites ($G = 1$) (Bottom) was introduced. The estimated parameters for each model are shown in Table 1. The Ca$^{2+}$-dependence of $z_Q$-$Q_C(V)$ data are superimposed with the $z_Q$ values predicted by Model I (C) and Model II (D). The statistical analysis using one-way ANOVA followed by Dunnett’s post-hoc test showed no significant effect of Ca$^{2+}$ on $z_Q$ ($p > 0.05$).